

$$ds^2 = -dt^2 + e^{2Ht} \left[e^{-2\beta(t)} dx^2 + e^{2\beta(t)} (dy^2 + dz^2) \right]$$