

$$\delta_s = \delta_r - \frac{1}{aH} \frac{\partial v_{||}}{\partial x^3}$$