

$$\frac{d[\ln(ap) + \Psi]}{dt} = \dot{\Psi} - \dot{\Phi}$$