

$$\nabla^2(\Psi+\Phi)= -\frac{\frac{d^2f}{dR^2}}{1+\frac{df}{dR}}\nabla^2(\delta R)\neq 0$$