

$$\ln \frac{\rho_{\mathrm{de}}(z)}{\rho_{\mathrm{de}}(0)} = 3 \int_0^z \frac{dz'}{1+z'} [1 + w(z')]$$