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# Cosmic Birefringence

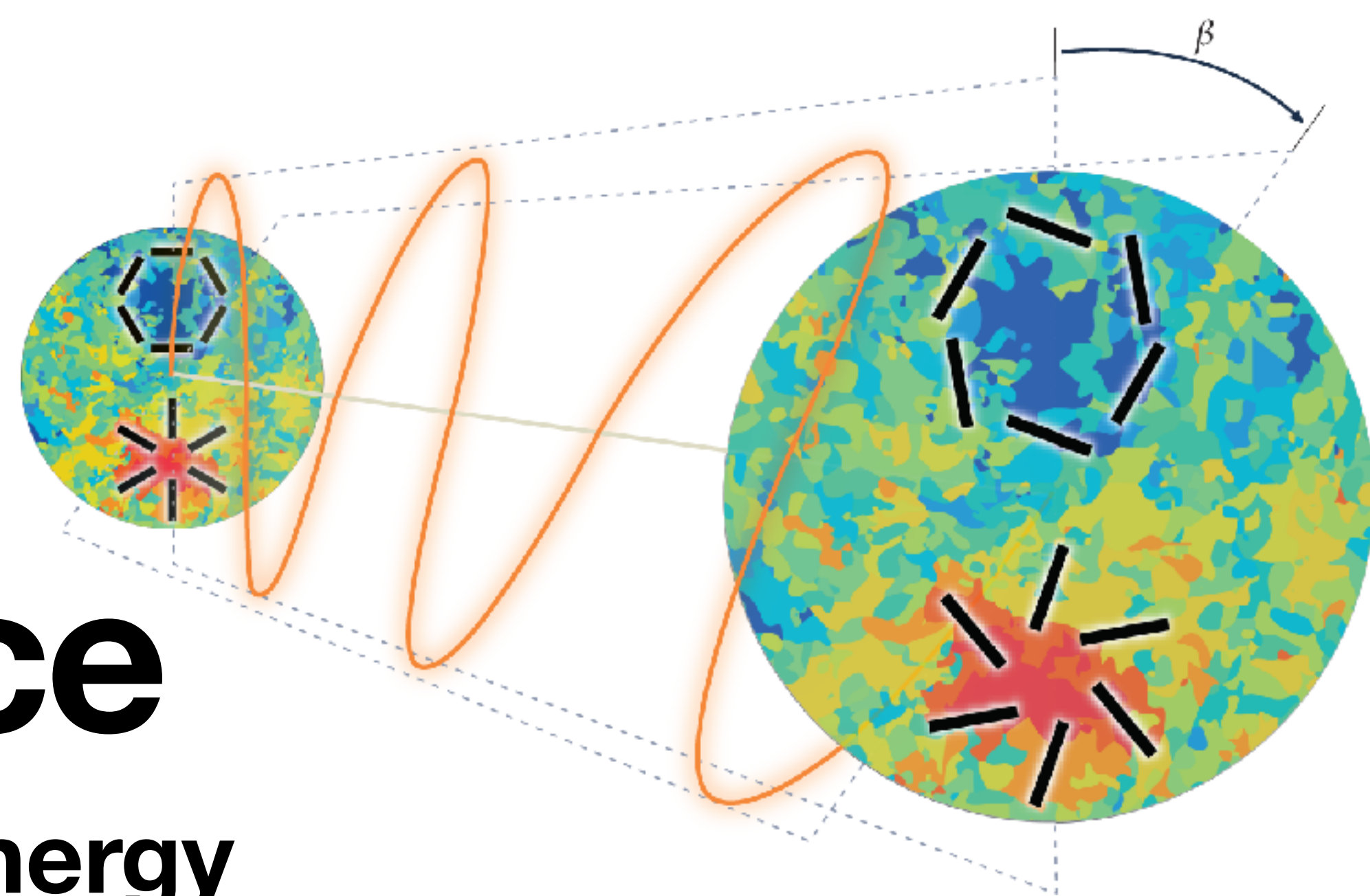
A New Probe of Dark Matter and Dark Energy

based on

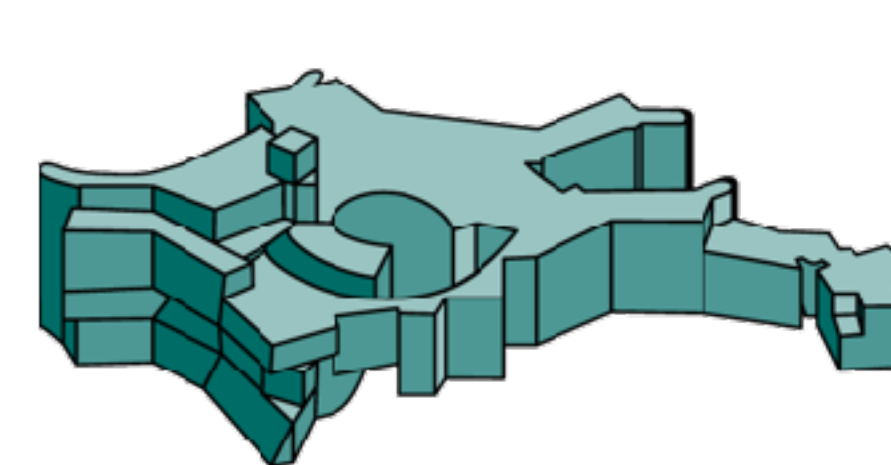
- *Minami & EK, PRL, 125, 221301 (2020)*
- *Diego-Palazuelos, Eskilt, Minami, et al., PRL, 128, 091302 (2022)*
- *EK, Nature Reviews Physics, 4 (2022)*
- *Eskilt & EK, PRD, 106, 063503 (2022)*
- *Diego-Palazuelos, et al., arXiv:2210.07644*

Eiichiro Komatsu

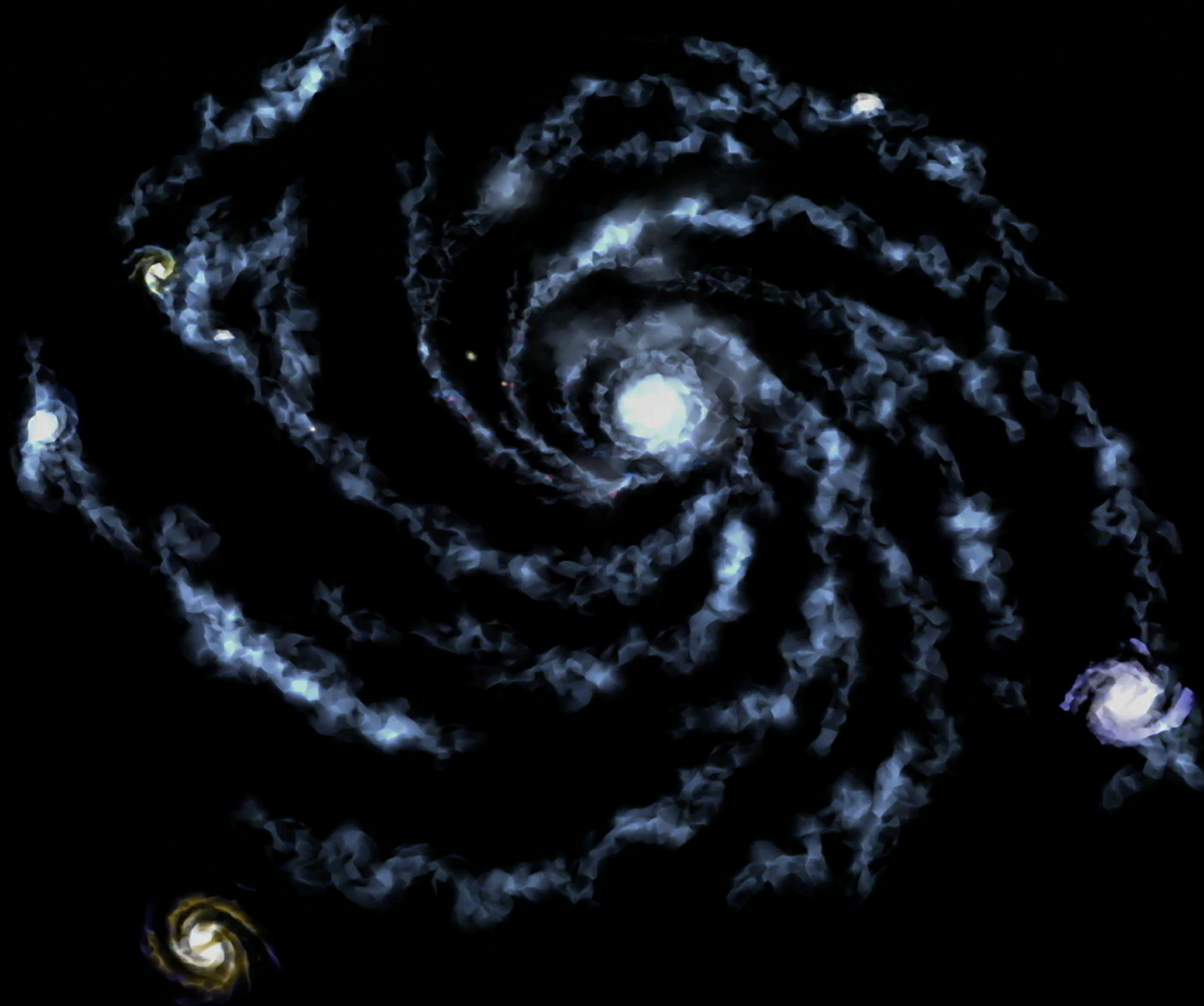
**Colloquium@WMU Münster, January 27, 2023**



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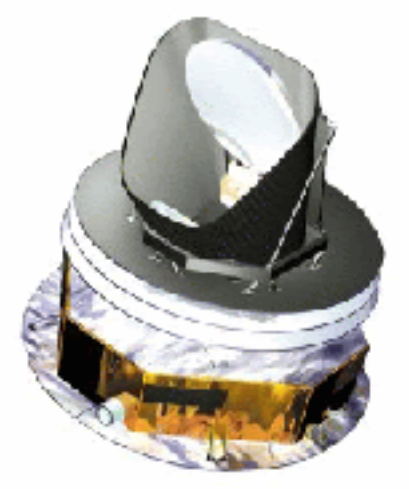
**MAX-PLANCK-INSTITUT**  
FÜR ASTROPHYSIK



# Standard Cosmological Model ( $\Lambda$ CDM) Requires New Physics

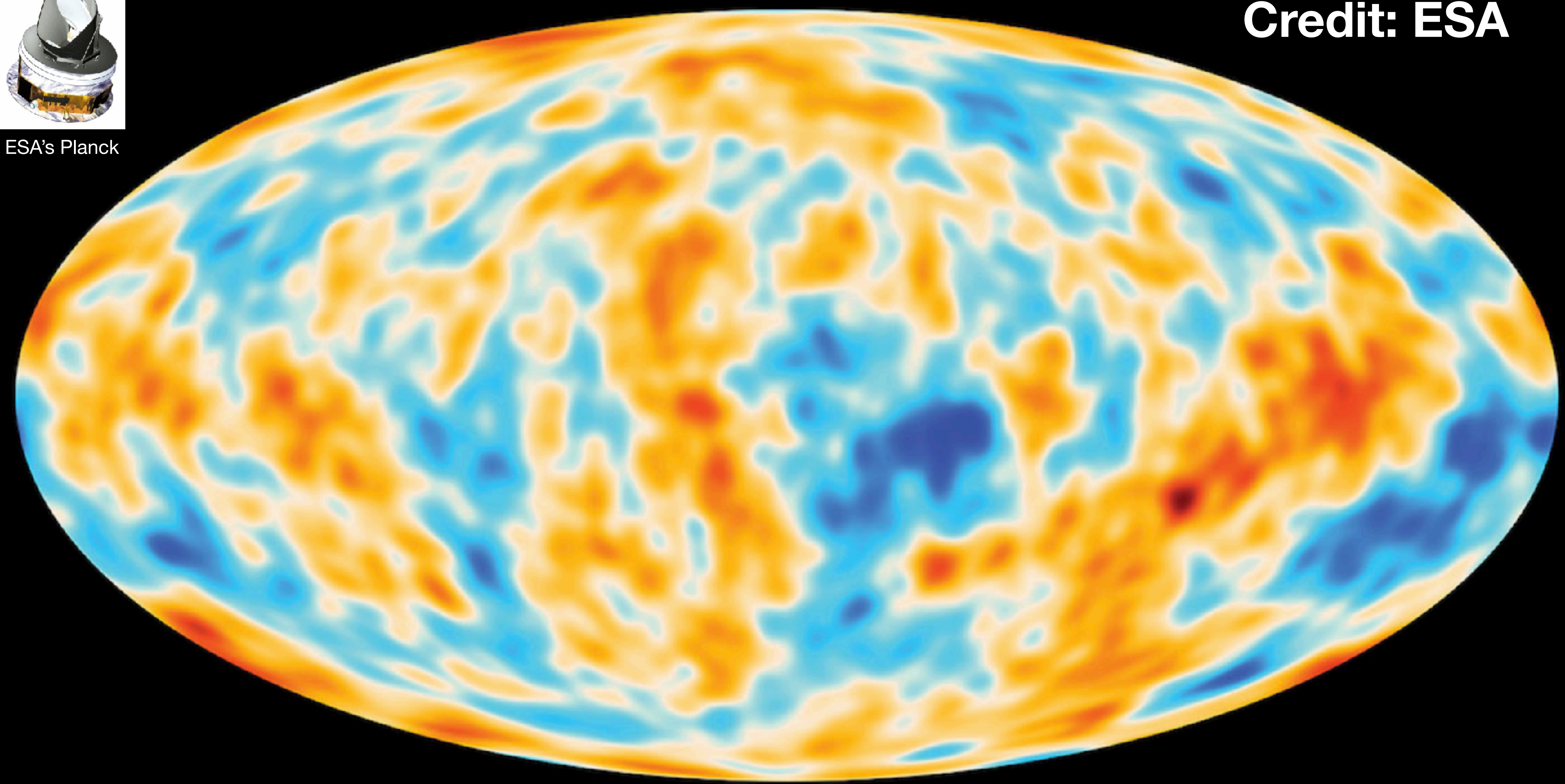
## Physics beyond Standard Model of elementary particles and fields

- **Dark Sector:** What is dark matter (*CDM*)? What is dark energy ( $\Lambda$ )?
- **Early Universe:** What powered the Big Bang? What is the fundamental physics behind cosmic inflation?
- ***Polarisation*** of the CMB may hold the key to the answers.



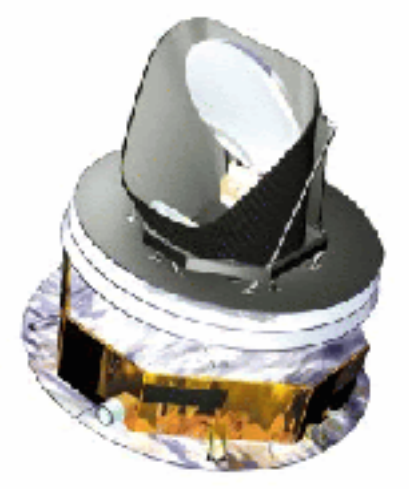
ESA's Planck

Credit: ESA



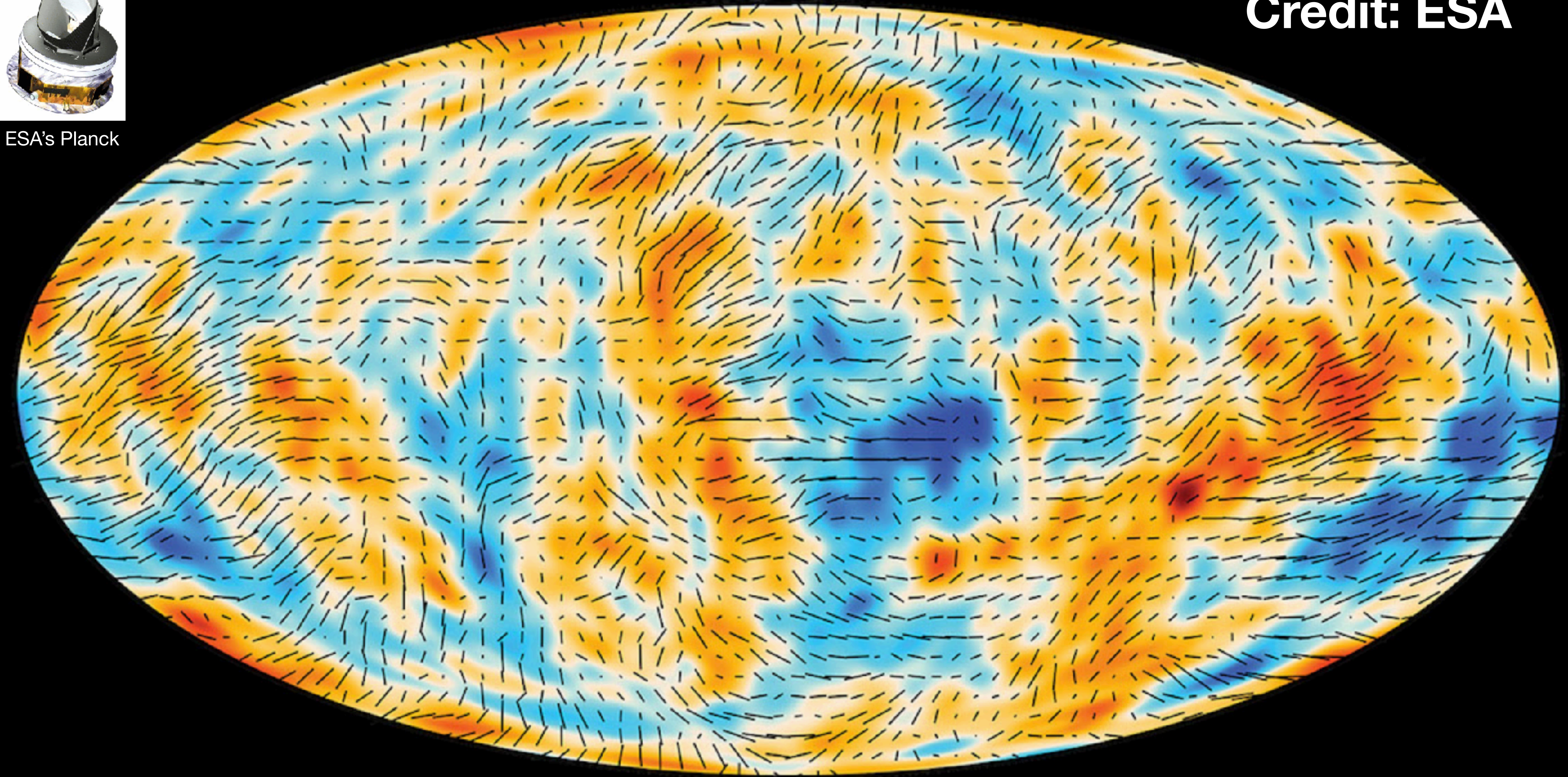
Foreground-cleaned Temperature (smoothed)

Emitted 13.8 billions years ago



ESA's Planck

Credit: ESA



Foreground-cleaned Temperature (smoothed) + Polarisation

Emitted 13.8 billions years ago

Credit: TALEX

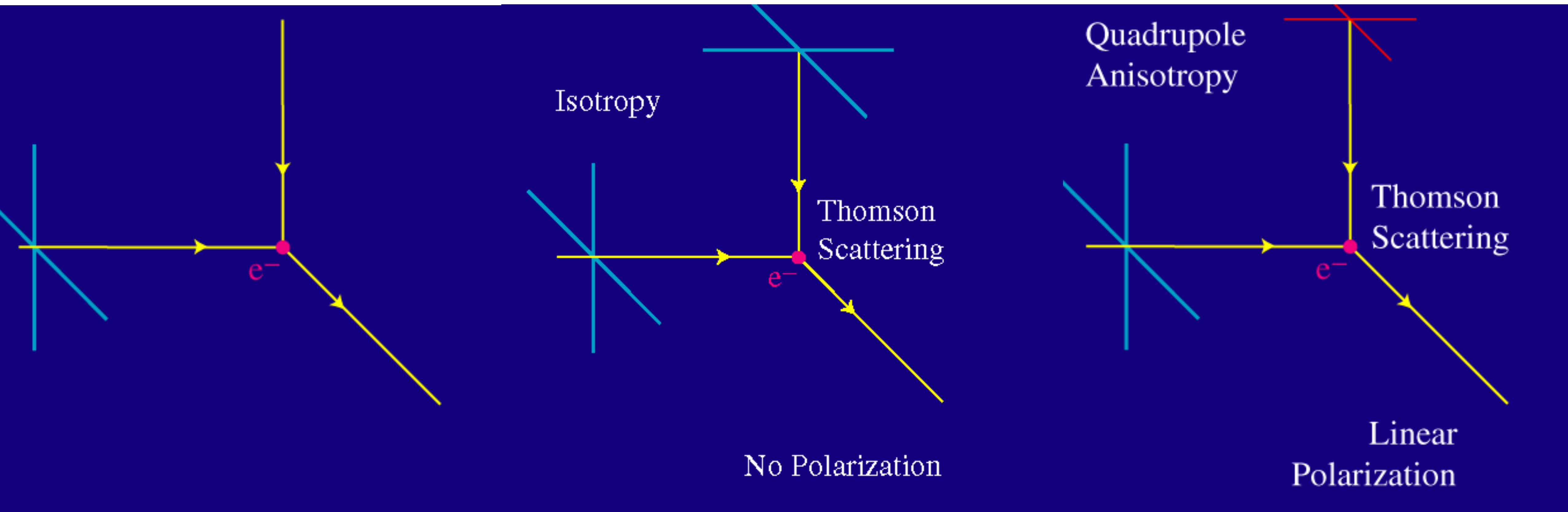


Credit: TALEX



# Physics of CMB Polarisation

Necessary and sufficient condition: Scattering and Quadrupole Anisotropy





# Standard Cosmological Model ( $\Lambda$ CDM) Requires New Physics

## Physics beyond Standard Model of elementary particles and fields

- **Dark Sector:** What is dark matter (*CDM*)? What is dark energy ( $\Lambda$ )?
  - **Cosmic birefringence** in CMB polarisation
- **Early Universe:** What powered the Big Bang? What is the fundamental physics behind cosmic inflation?
  - Imprint of **primordial gravitational waves** in CMB polarisation
- **Polarisation** of the CMB may hold the key to the answers.

[nature](#) > [nature reviews physics](#) > [review articles](#) > article

Available also at  
arXiv:2202.13919

Review Article | [Published: 18 May 2022](#)

## New physics from the polarized light of the cosmic microwave background

[Eiichiro Komatsu](#) 

[Nature Reviews Physics](#) (2022) | [Cite this article](#)

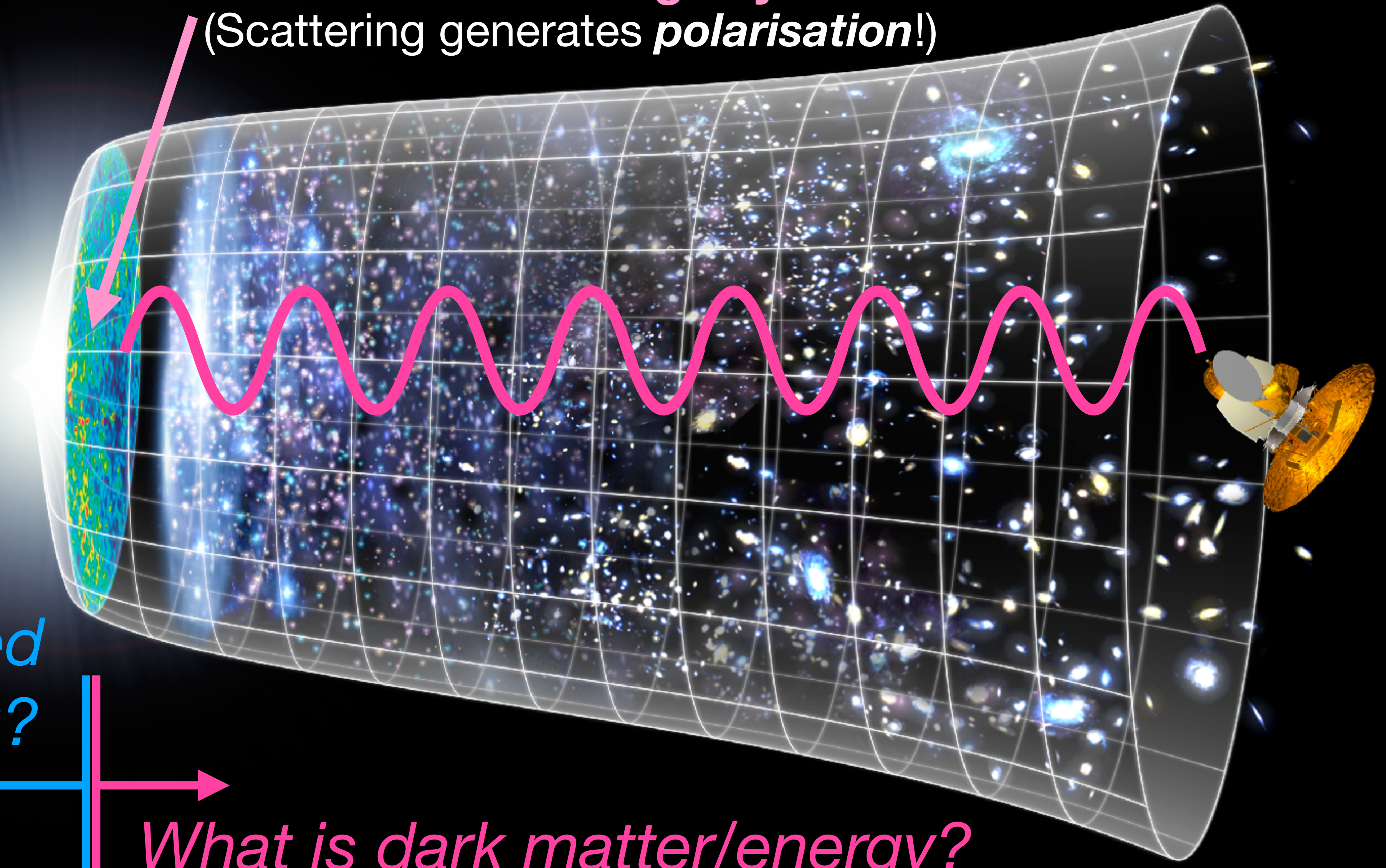
[Metrics](#)

### *Key Words:*

1. Cosmic Microwave Background (CMB)
2. Polarization
3. Parity Symmetry

The surface of "last scattering" by electrons

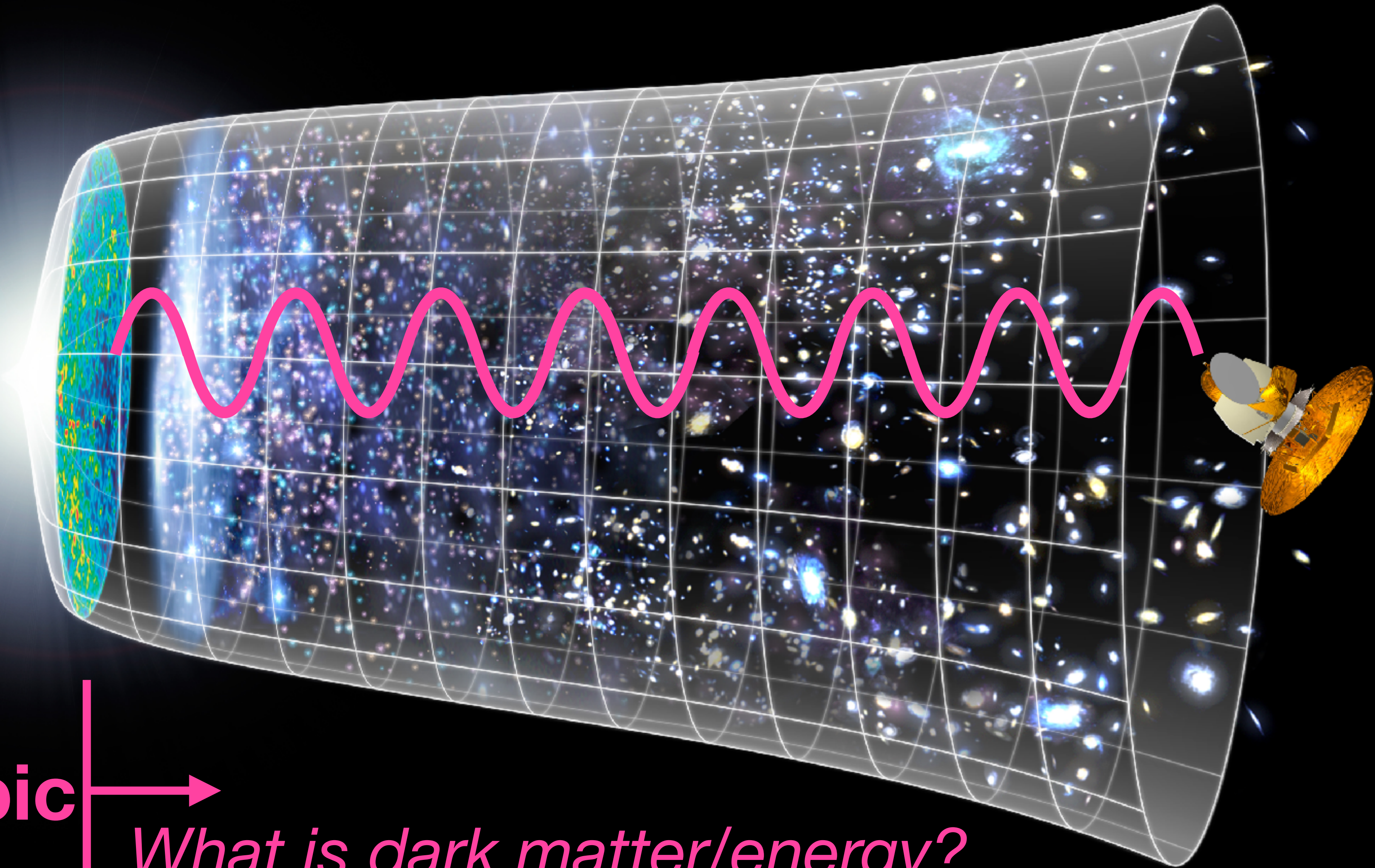
(Scattering generates *polarisation!*)



*What powered the Big Bang?*

*What is dark matter/energy?*

# How does the electromagnetic wave of the CMB propagate?

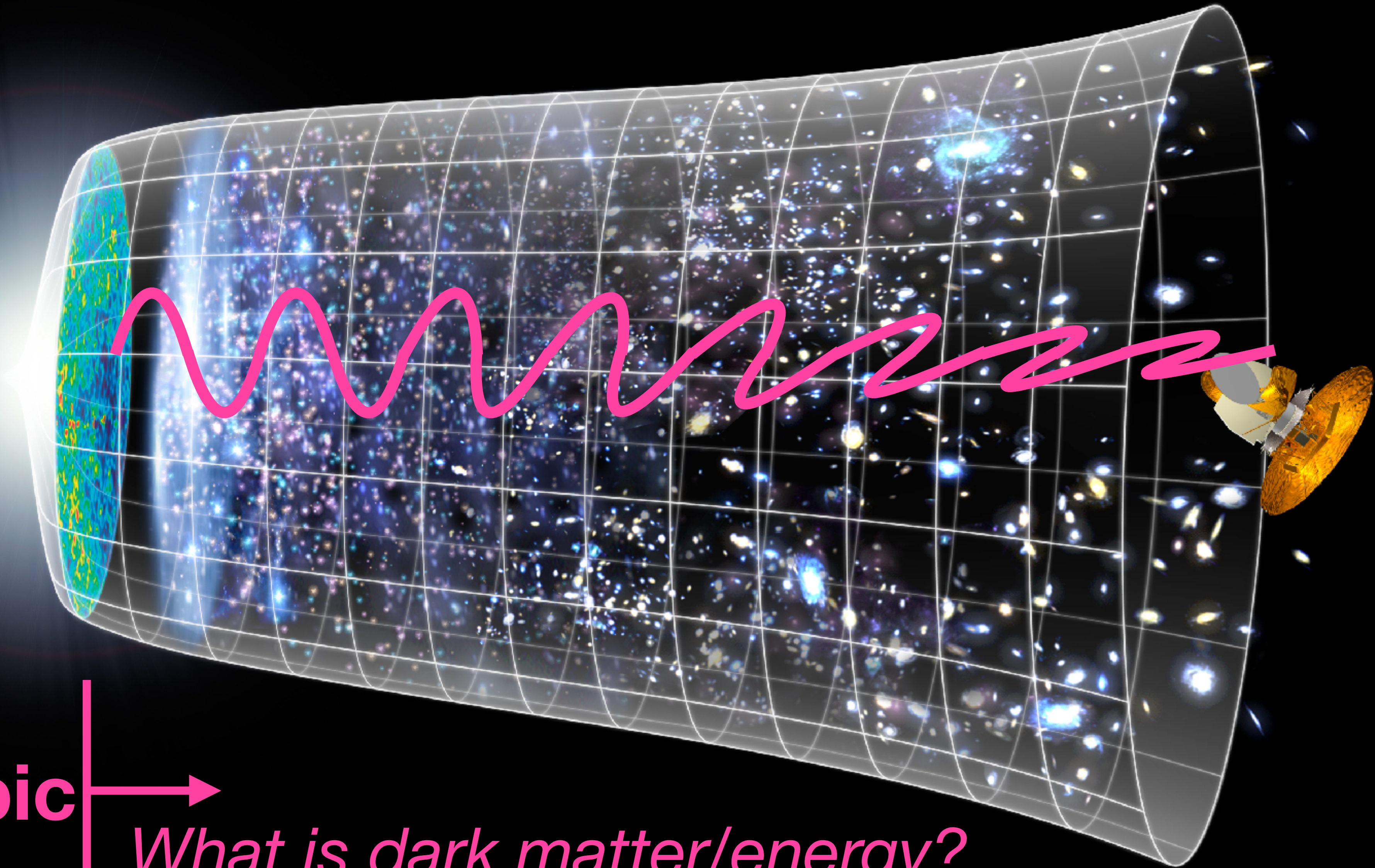


Today's topic



*What is dark matter/energy?*

# How does the electromagnetic wave of the CMB propagate?



Today's topic




*What is dark matter/energy?*

# Cosmic Birefringence

The Universe filled with a “birefringent material”

*This “axion” field can be dark matter or dark energy!*



- If the Universe is filled with a pseudoscalar field (e.g., an axion field) coupled to the electromagnetic tensor via a Chern-Simons coupling:

Ni (1977); Turner & Widrow (1988)

the effective Lagrangian for axion electrodynamics is

$$\mathcal{L} = -\frac{1}{2}\partial_\mu\theta\partial^\mu\theta - \frac{1}{4}F_{\mu\nu}F^{\mu\nu} + \underbrace{g_a\theta F_{\mu\nu}\tilde{F}^{\mu\nu}}_{\text{Chern-Simons term}}, \quad (3.7)$$

$$\tilde{F}^{\mu\nu} = \sum_{\alpha\beta} \frac{\epsilon^{\mu\nu\alpha\beta}}{2\sqrt{-g}} F_{\alpha\beta}$$

where  $g_a$  is a coupling constant of the order  $\alpha$ , and the vacuum angle  $\theta = \phi_a / f_a$  ( $\phi_a =$  axion field). The equations

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu \quad \sum_{\mu\nu} F_{\mu\nu}F^{\mu\nu} = 2(\mathbf{B} \cdot \mathbf{B} - \mathbf{E} \cdot \mathbf{E}) \quad \sum_{\mu\nu} F_{\mu\nu}\tilde{F}^{\mu\nu} = -4\mathbf{B} \cdot \mathbf{E}$$

Parity Even Parity Odd

# Cosmic Birefringence

The Universe filled with a “birefringent material”

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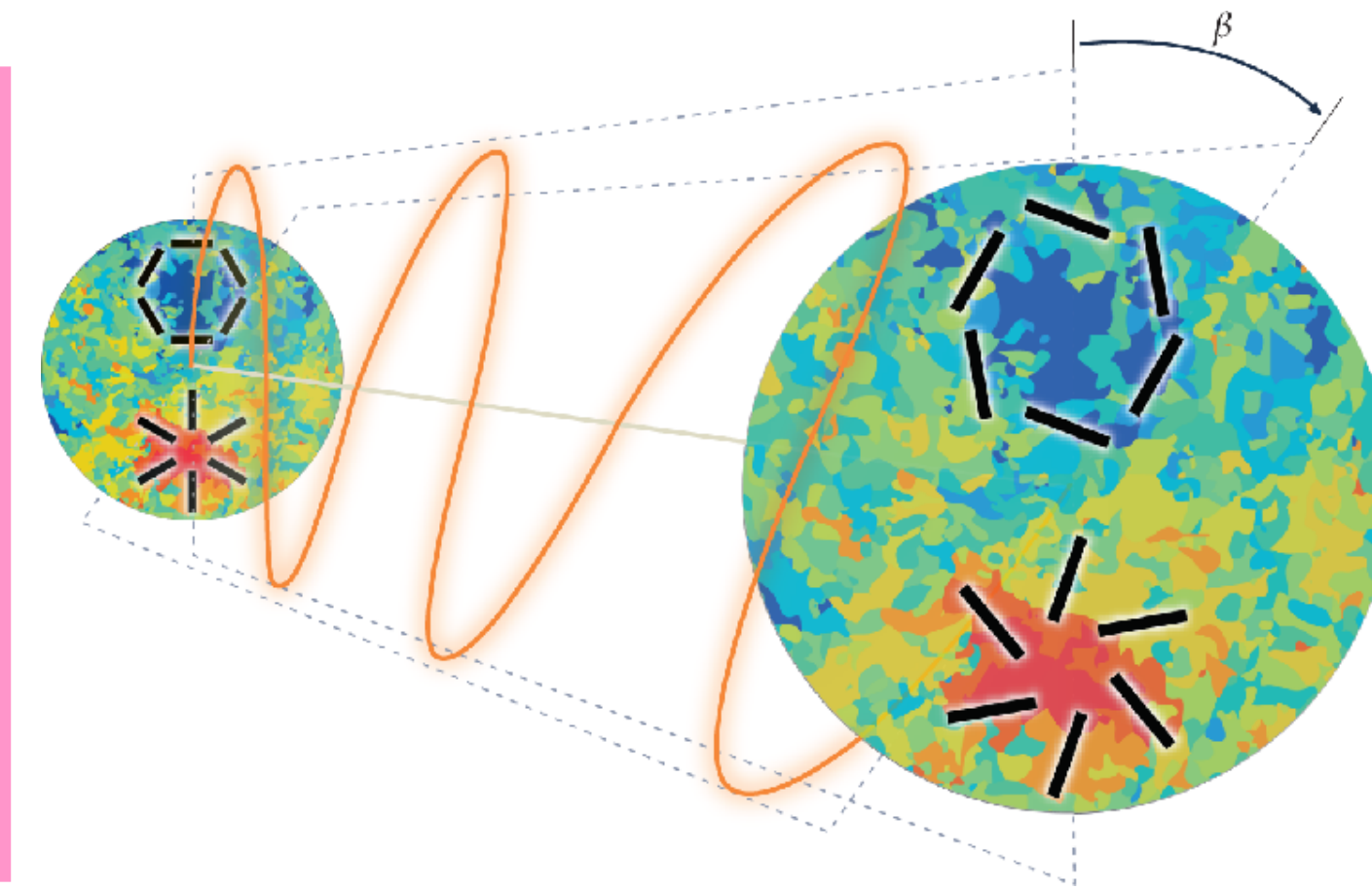
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“Cosmic Birefringence”



This term makes the phase velocities of right- and left-handed polarisation states of photons different, leading to **rotation of the linear polarisation direction.**

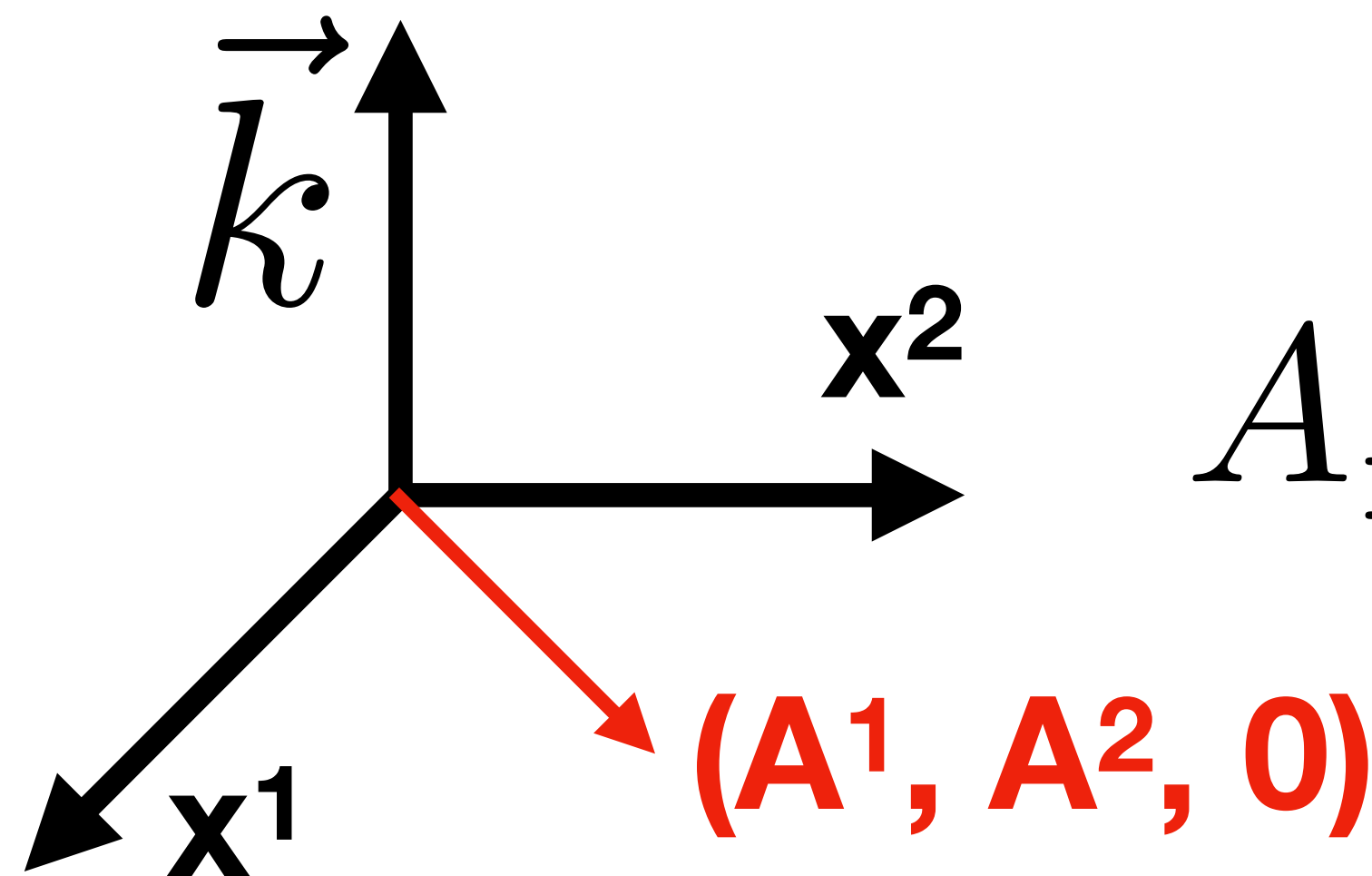
# Standard Maxwell Theory

## Warm up (1)

- To isolate a transverse wave, we require  $A_0=0$  and  $\text{div}(A_i)=0$ . Then, in vacuum,

$$\left( \frac{\partial^2}{\partial \eta^2} - \nabla^2 \right) A_i(\eta, \mathbf{x}) = 0 \quad ds^2 = a^2(-d\eta^2 + d\mathbf{x}^2)$$

- Go to Fourier space, choose the propagation direction of  $A_i$  to be in z-axis, and define right- and left-handed polarisation states as



$$A_{\pm} = \frac{A_1 \mp i A_2}{\sqrt{2}}$$

- $A_+$ : Right-handed state
- $A_-$ : Left-handed state



# Standard Maxwell Theory

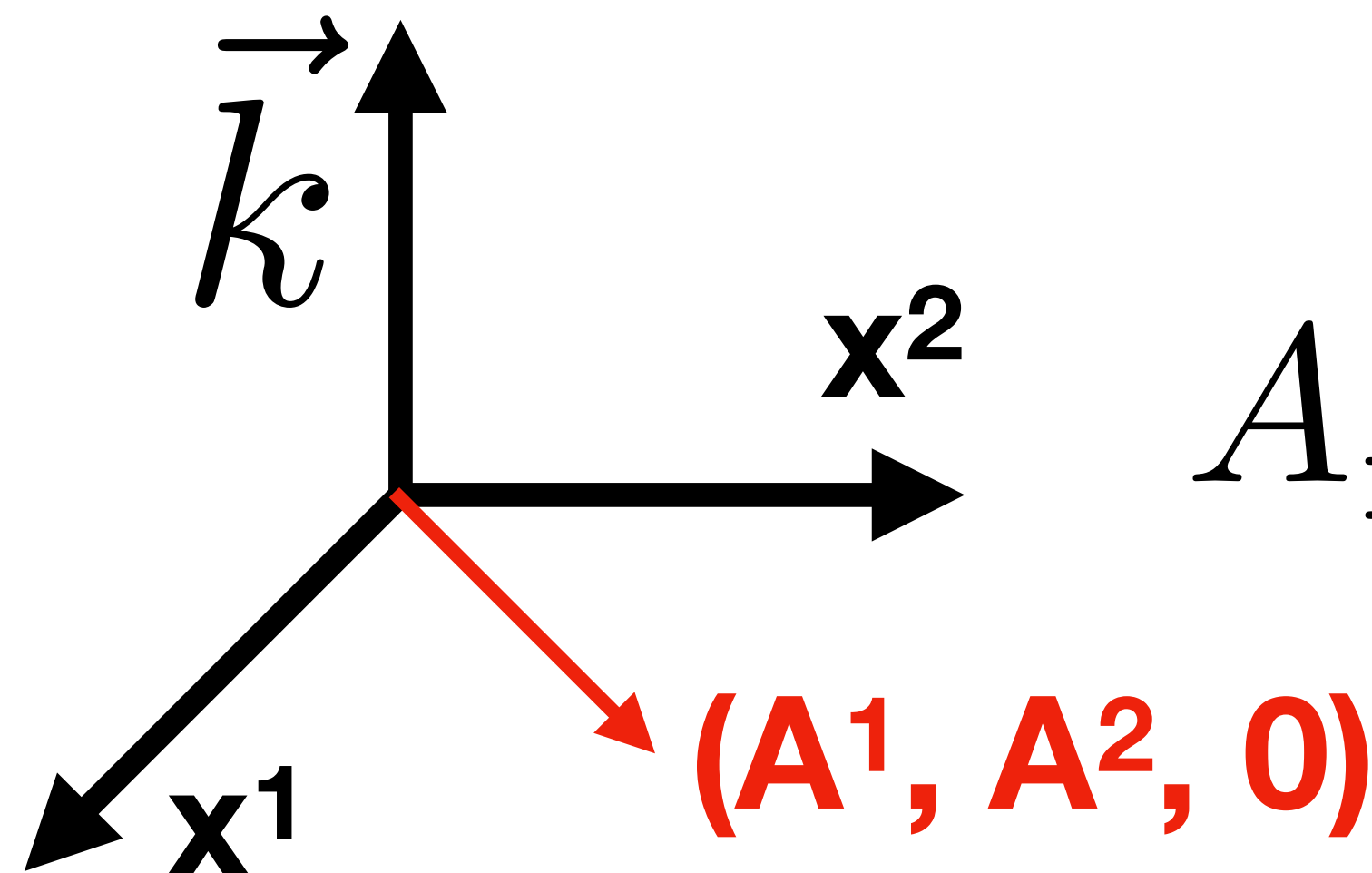
## Warm up (2)

- To isolate a transverse wave, we require  $A_0=0$  and  $\text{div}(A_i)=0$ . Then, in vacuum,

$$\left( \frac{\partial^2}{\partial \eta^2} - \nabla^2 \right) A_i(\eta, \mathbf{x}) = 0 \quad \rightarrow \quad \left( -\omega_{\pm}^2 + k^2 \right) A_{\pm}(\eta) = 0$$

Same dispersion relation for right- and left-handed states

- Go to Fourier space, choose the propagation direction of  $A_i$  to be in z-axis, and define right- and left-handed polarisation states as



$$A_{\pm} = \frac{A_1 \mp i A_2}{\sqrt{2}}$$

- $A_+$ : Right-handed state
- $A_-$ : Left-handed state

# Cosmic Birefringence

## Derivation (1)

- Now, include **the Chern-Simons term!**

the effective Lagrangian for axion electrodynamics is

$$\mathcal{L} = -\frac{1}{2}\partial_\mu\theta\partial^\mu\theta - \frac{1}{4}F_{\mu\nu}F^{\mu\nu} + \underbrace{g_a\theta F_{\mu\nu}\tilde{F}^{\mu\nu}}_{\text{Chern-Simons term}}, \quad (3.7)$$

$\tilde{F}^{\mu\nu} = \sum_{\alpha\beta} \frac{\epsilon^{\mu\nu\alpha\beta}}{2\sqrt{-g}} F_{\alpha\beta}$

where  $g_a$  is a coupling constant of the order  $\alpha$ , and the vacuum angle  $\theta = \phi_a / f_a$  ( $\phi_a =$  axion field). The equations

- The equation of motion is modified to

$$\left(-\omega_\pm^2 + k^2\right) A_\pm(\eta) = 0 \quad \longrightarrow \quad \left(-\omega_\pm^2 + k^2 \pm 4g_a k \theta'\right) A_\pm(\eta) = 0$$

$$\frac{\omega_\pm^2}{k^2} = 1 \pm \frac{4g_a \theta'}{k} \quad (\theta' = \partial\theta/\partial\eta)$$

# Cosmic Birefringence

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$$\frac{\omega_\pm^2}{k^2} = 1 \pm \frac{4g_a\theta'}{k} = \left(1 \pm \frac{2g_a\theta'}{k}\right)^2 - \frac{4g_a^2\theta'^2}{k^2}$$

# Cosmic Birefringence

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$$\frac{\omega_\pm}{k} \simeq 1 \pm \frac{2g_a\theta'}{k}$$

Phase velocities of right- and left-handed states are slightly different!

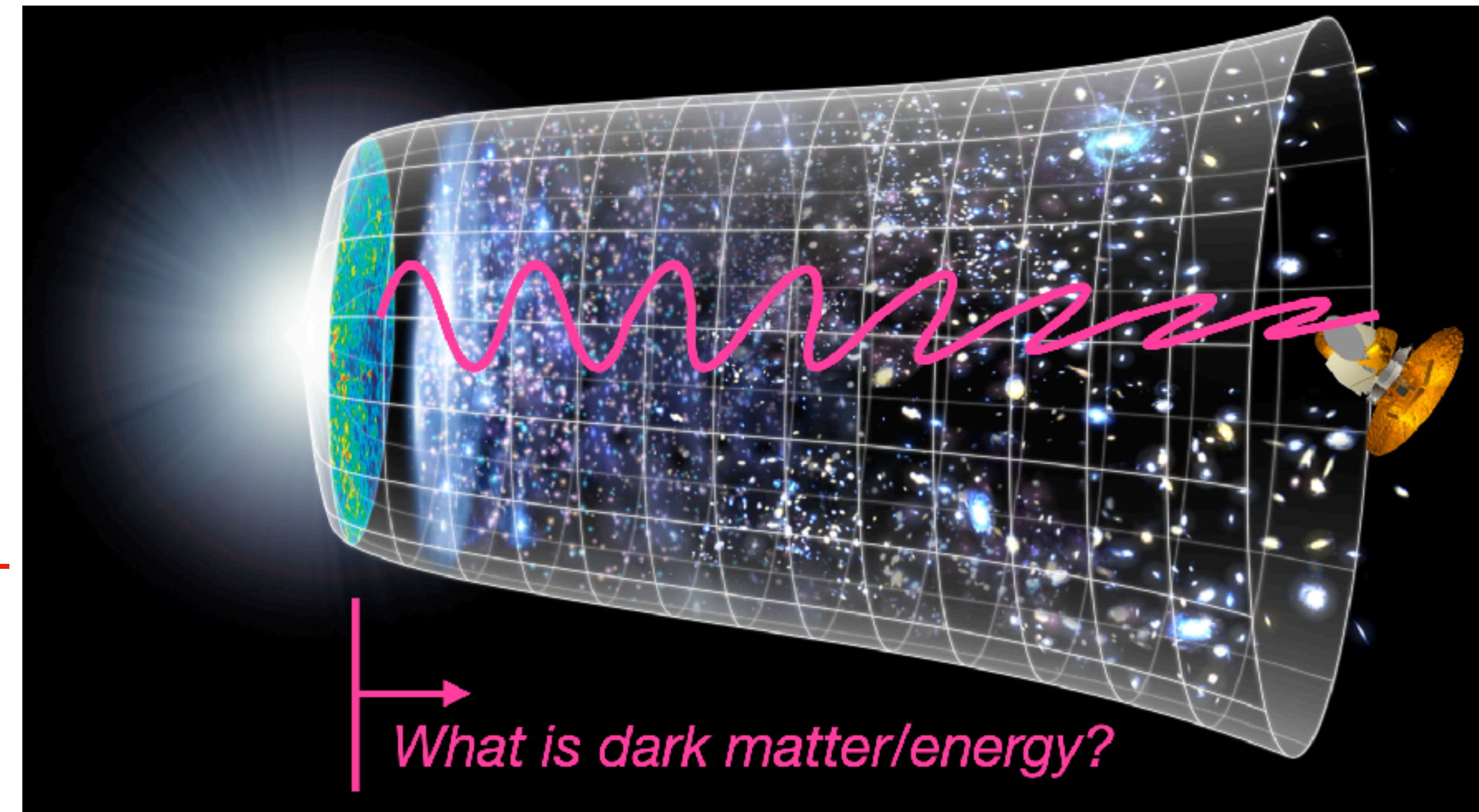
# Cosmic Birefringence

## Derivation (2)

- With

$$\frac{\omega_{\pm}}{k} \simeq 1 \pm \frac{2g_a \theta'}{k}$$

Phase velocities of right- and left-handed states are slightly different!



- The plane of linear polarisation rotates clockwise on the sky by an angle  $\beta$ :

$$-\beta = \int d\eta \frac{\omega_+ - \omega_-}{2} = 2g_a \int d\eta \theta' = 2g_a \int dt \dot{\theta}$$

**The effect accumulates over the distance!**

**=> CMB polarisation is sensitive to this effect**

# Cosmic Birefringence

## Recap

- If the Universe is filled with a pseudoscalar field (e.g., an axion field) coupled to the electromagnetic tensor via a Chern-Simons coupling:

*This “axion” field can be dark matter or dark energy!*

Ni (1977); Turner & Widrow (1988)

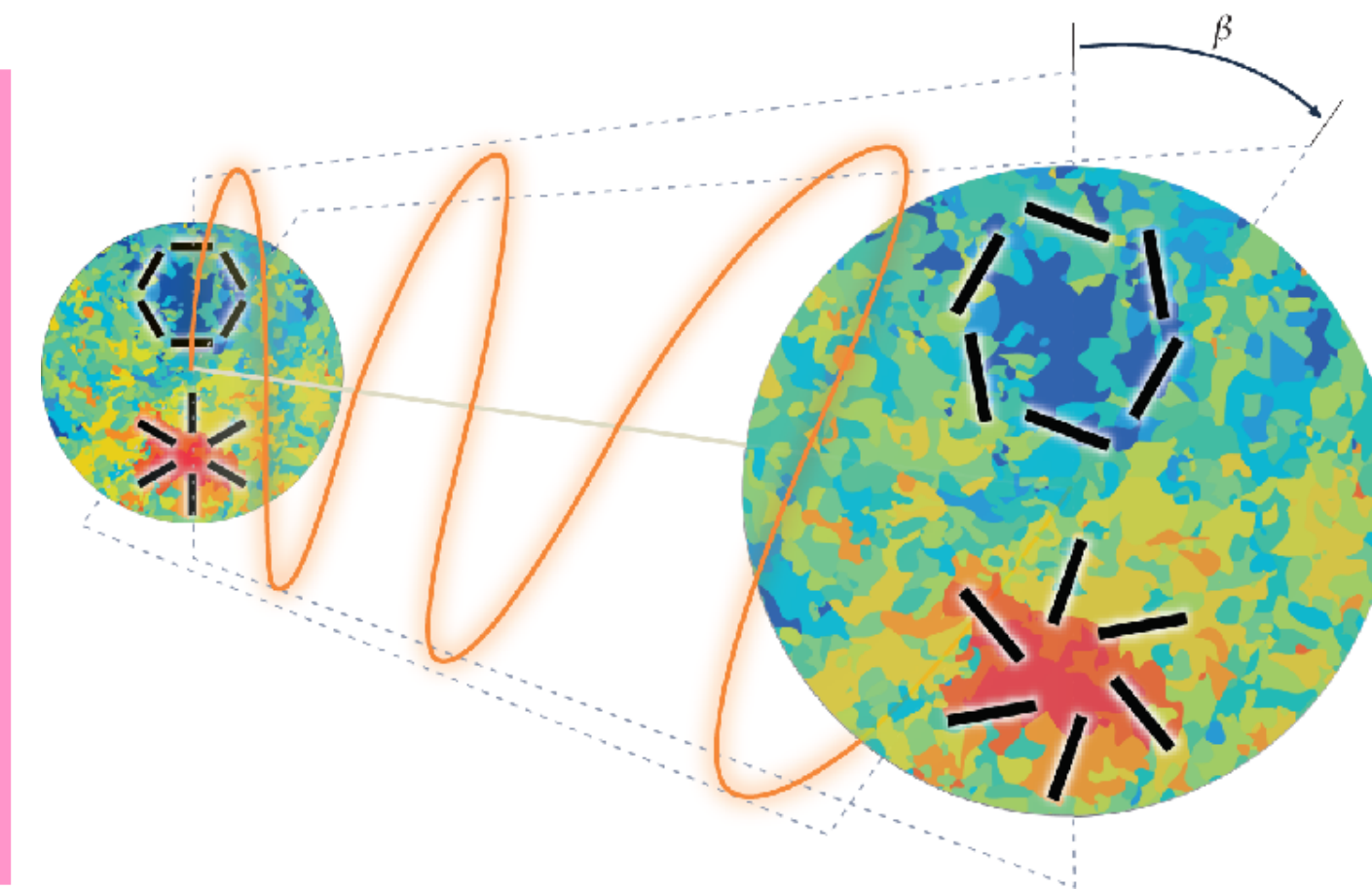
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$$\beta = -2g_a \int_{t_{\text{emitted}}}^{t_{\text{observed}}} dt \dot{\theta} = 2g_a [\theta(t_e) - \theta(t_o)]$$




The difference between the fields values at the end points gives  $\beta$ .

# Cosmic Birefringence

## Recap

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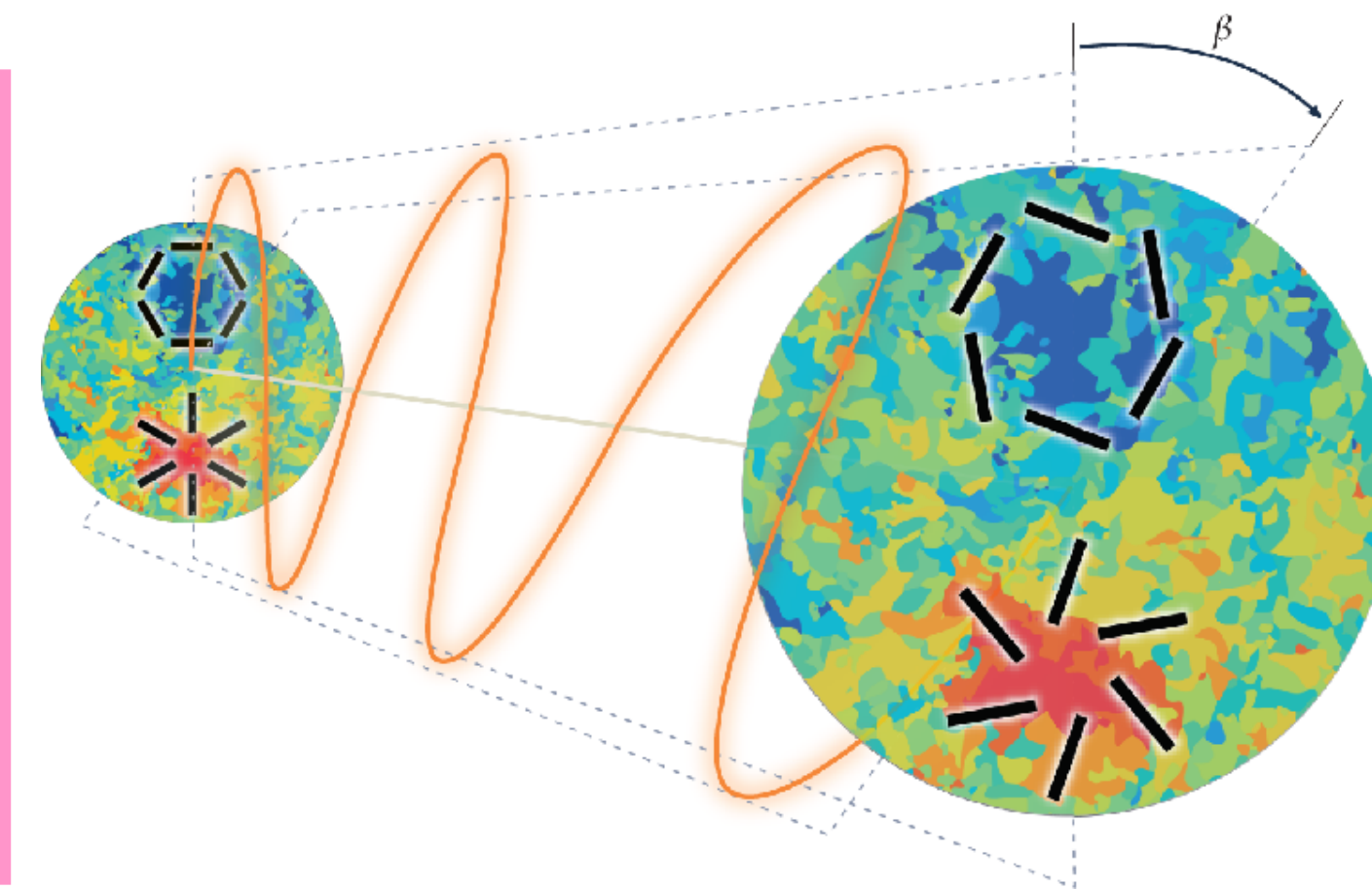
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where  $g_a$  is a coupling constant of the order  $\alpha$ , and the vacuum angle  $\theta = \phi_a / f_a$  ( $\phi_a =$  axion field). The equations



If  $\theta$  varies over space:

$$\beta(\hat{n}, \tau) = -2g_a \int_{t_{\text{emitted}}}^{t_{\text{observed}}} dt \frac{d\theta}{dt} = 2g_a [\theta(t_e, \hat{n}r_{oe}) - \theta(t_o, \tau)]$$

# Motivation

## Why study the cosmic birefringence?

- The Universe's energy budget is dominated by two dark components:
  - Dark Matter
  - Dark Energy
- Either or both of these can be an axion-like field!
  - See Marsh (2016) and Ferreira (2020) for reviews.
- Thus, detection of parity-violating physics in polarisation of the cosmic microwave background can transform our understanding of Dark Matter/Energy.



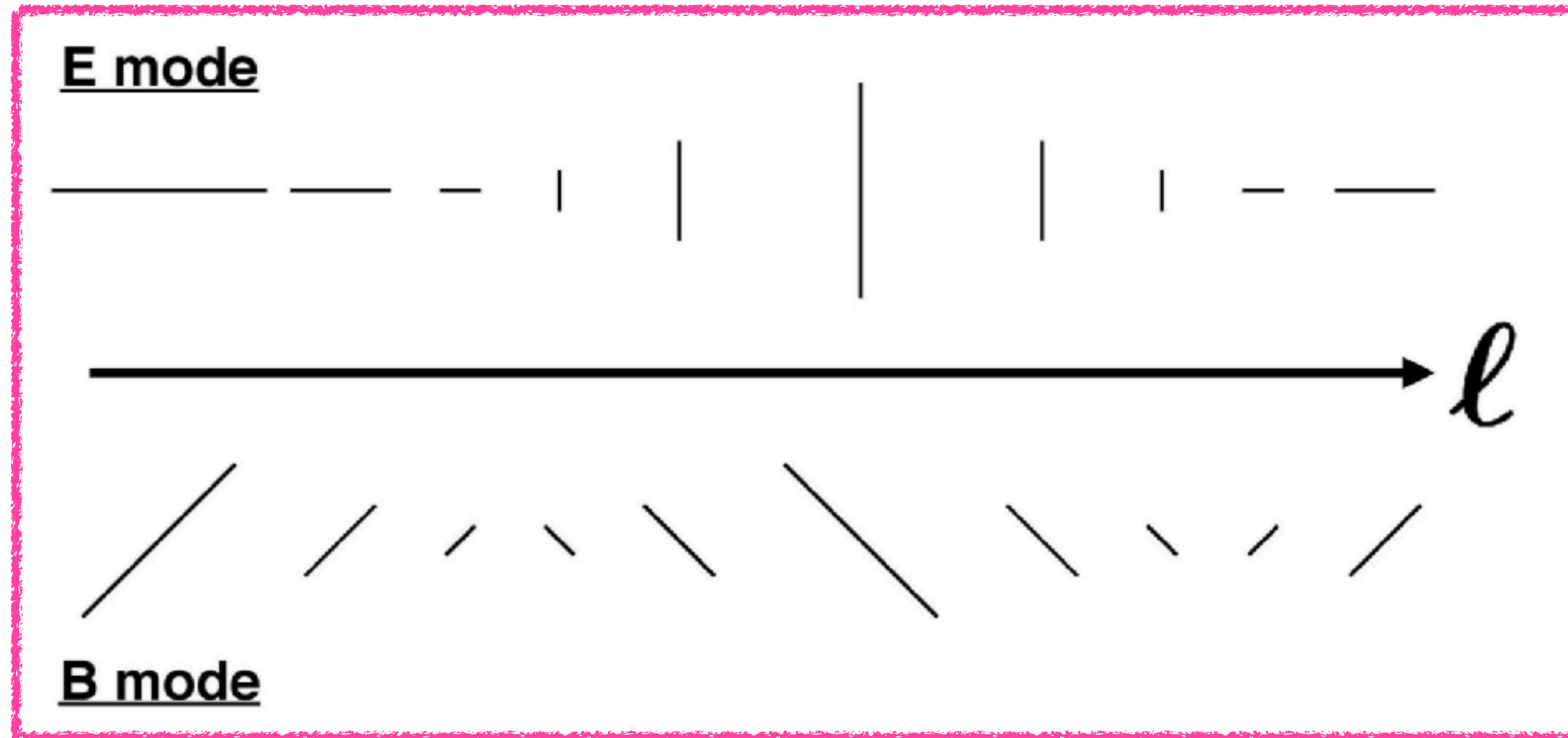
# **(Simpler) Motivation**

## **Why study the cosmic birefringence?**

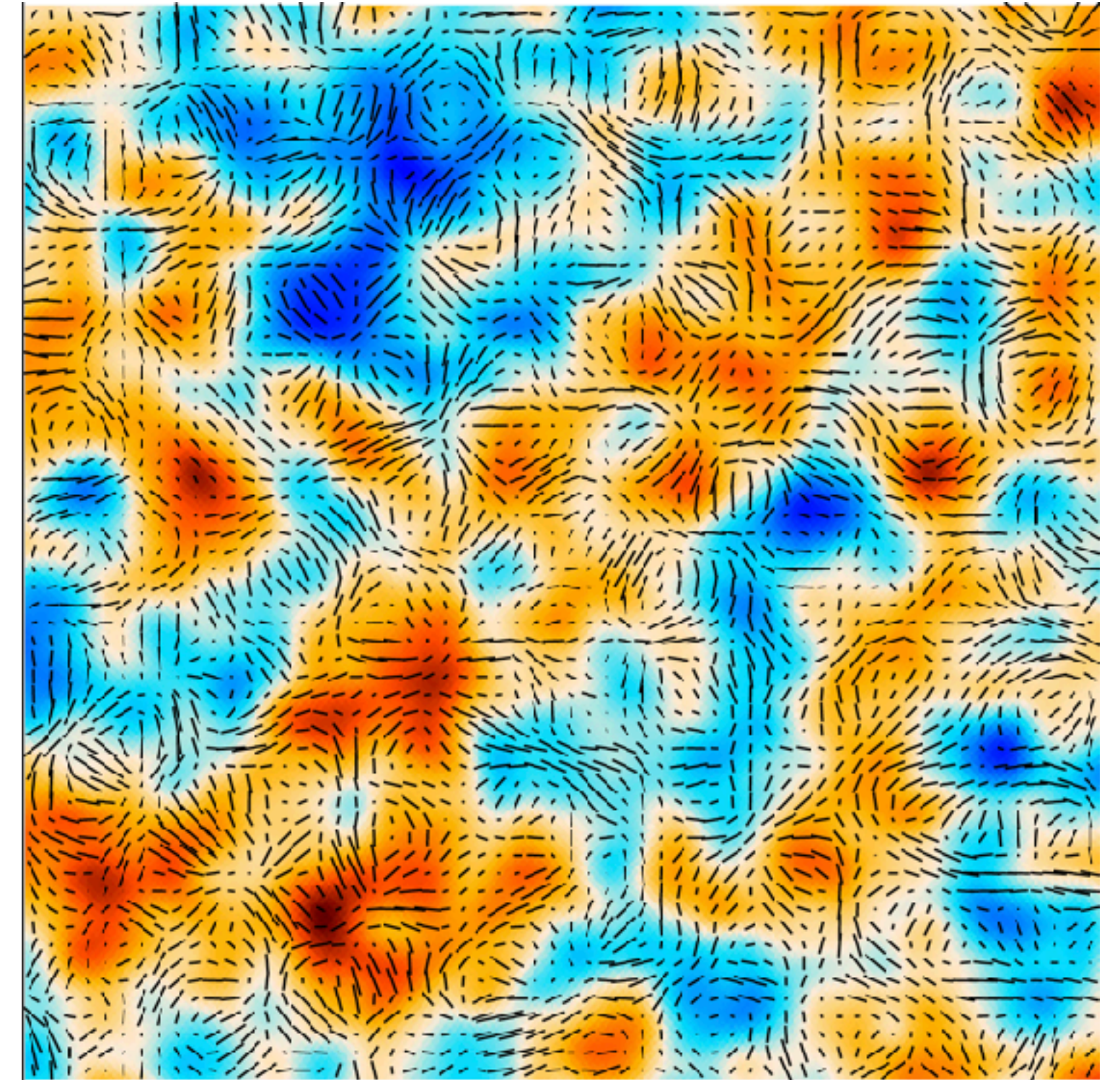
- We know that the weak interaction violates parity (Lee & Yang 1956; Wu et al. 1957).
  - Why should the laws of physics governing the Universe conserve parity?
- Let's look!

# Parity eigenstates: E and B modes

Concept defined in Fourier space



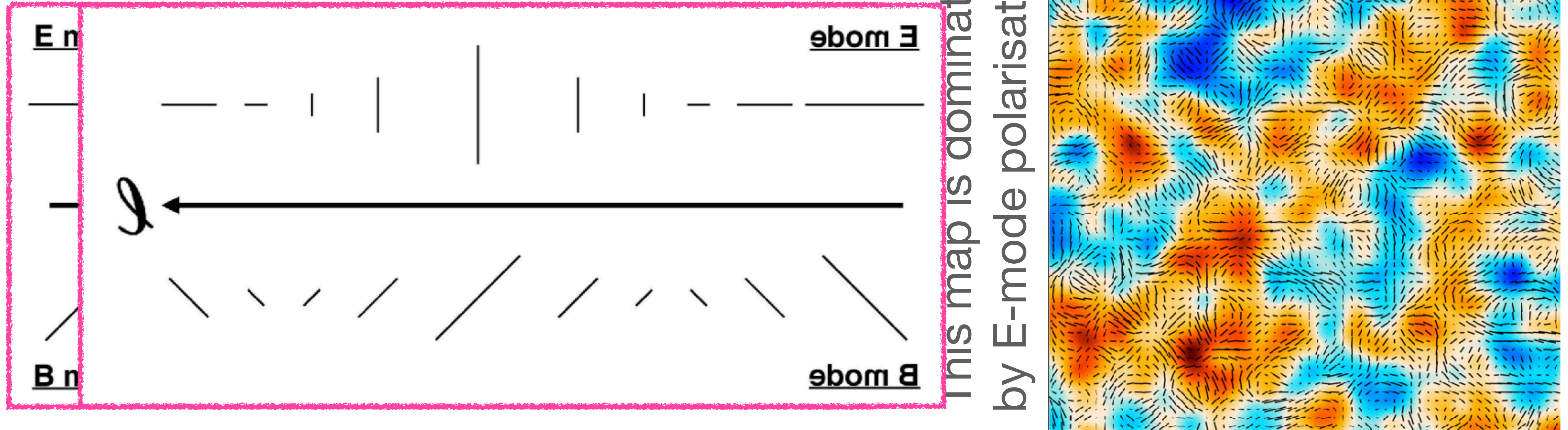
This map is dominated  
by E-mode polarisation



- **E-mode** : Polarisation directions are **parallel or perpendicular** to the wavenumber direction
- **B-mode** : Polarisation directions are **45 degrees tilted** w.r.t the wavenumber direction

# Parity eigenstates: E and B modes

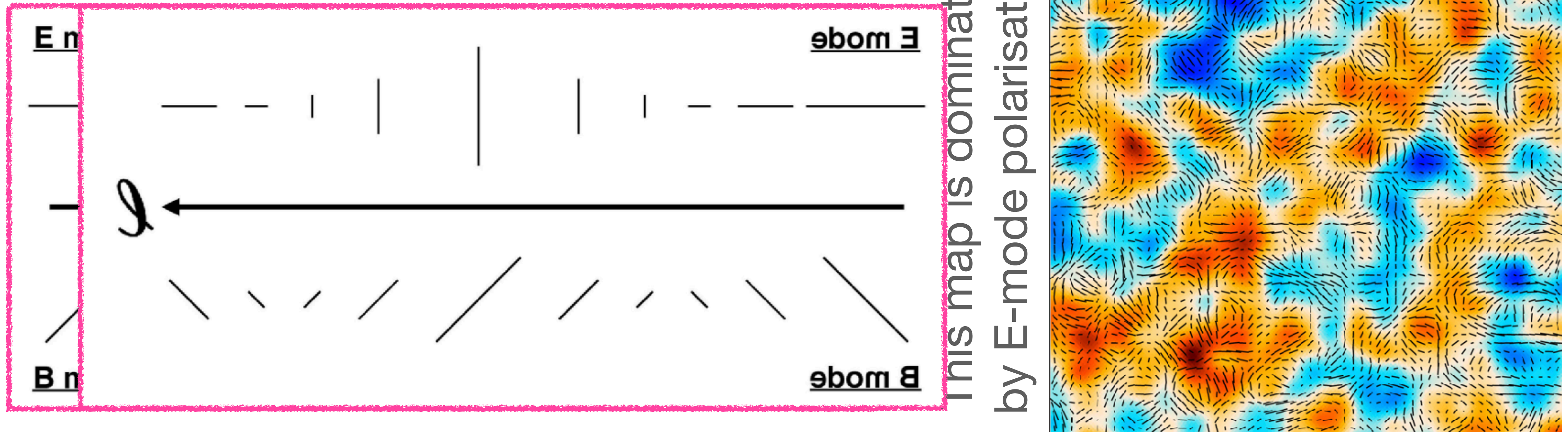
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# Parity eigenstates: E and B modes

Concept defined in Fourier space

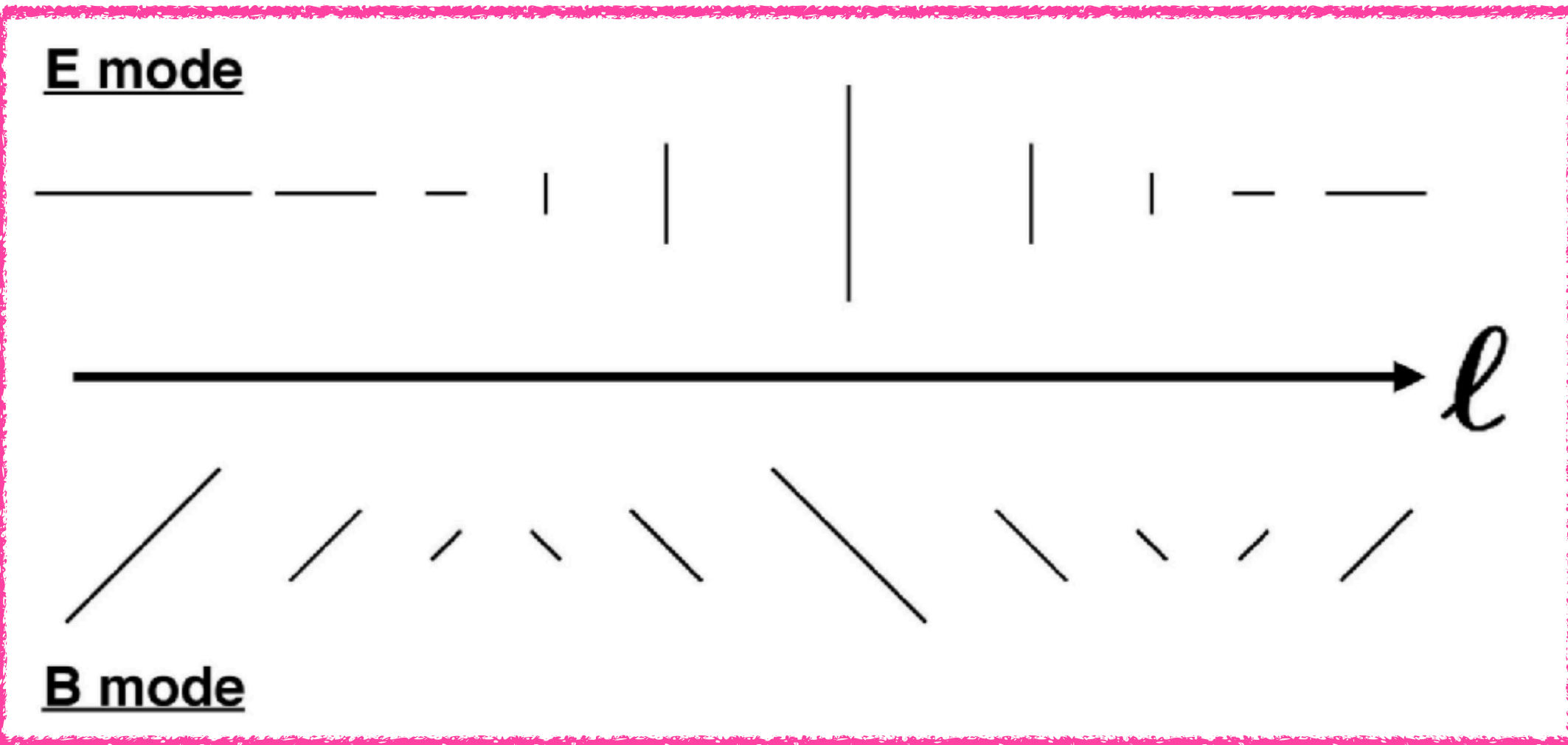


- **E-mode** : Polarisation directions are **parallel or perpendicular** to the wavenumber direction
- **B-mode** : Polarisation directions are **45 degrees tilted** w.r.t the wavenumber direction

**IMPORTANT**: These "E and B modes" are jargons in the CMB community, and completely unrelated to the electric and magnetic fields of the electromagnetism!!

# Parity Flip

**E-mode remains the same, whereas B-mode changes the sign**



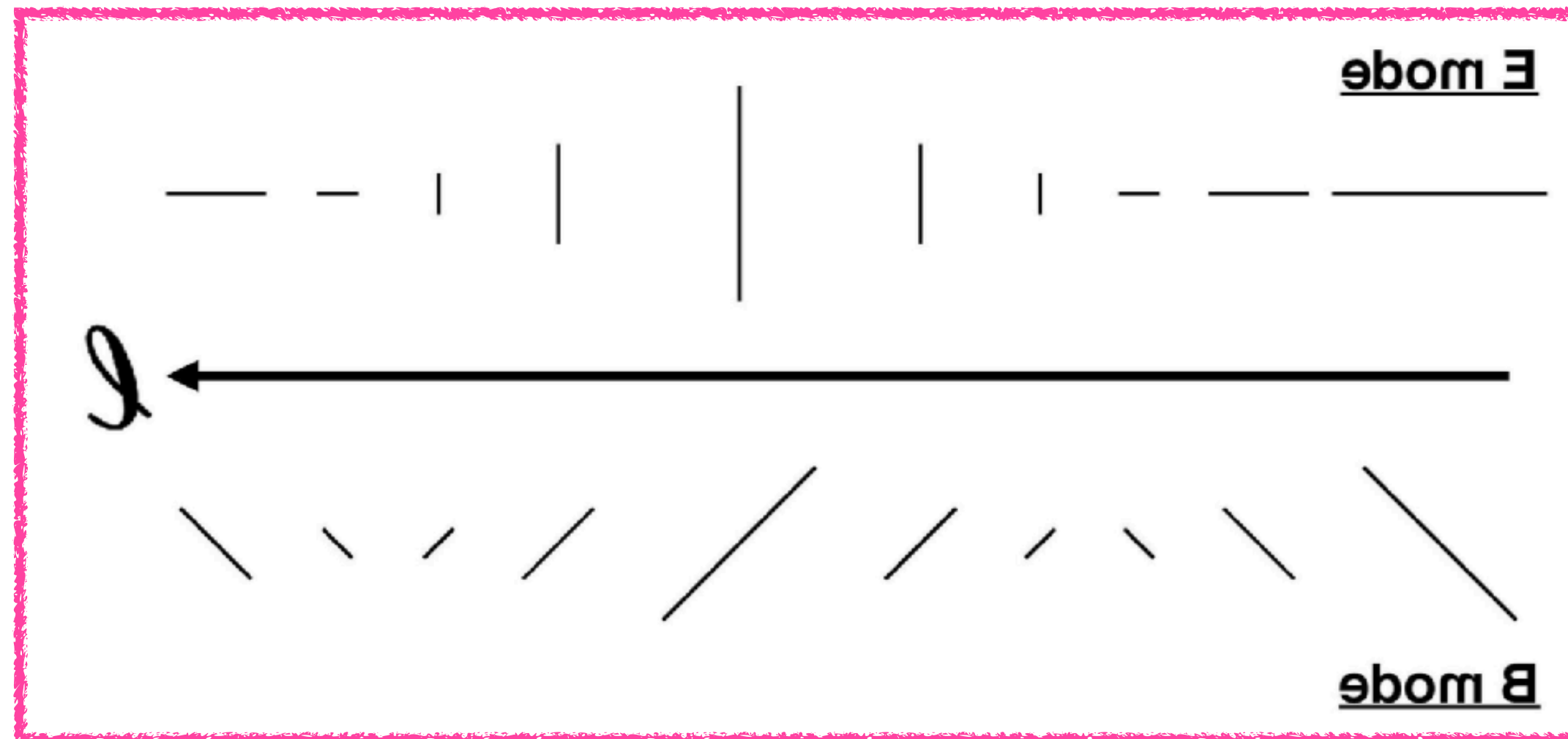
- Two-point correlation functions invariant under the parity flip are

$$\langle E_{\ell} E_{\ell'}^* \rangle = (2\pi)^2 \delta_D^{(2)}(\ell - \ell') C_{\ell}^{EE}$$

$$\langle B_{\ell} B_{\ell'}^* \rangle = (2\pi)^2 \delta_D^{(2)}(\ell - \ell') C_{\ell}^{BB}$$

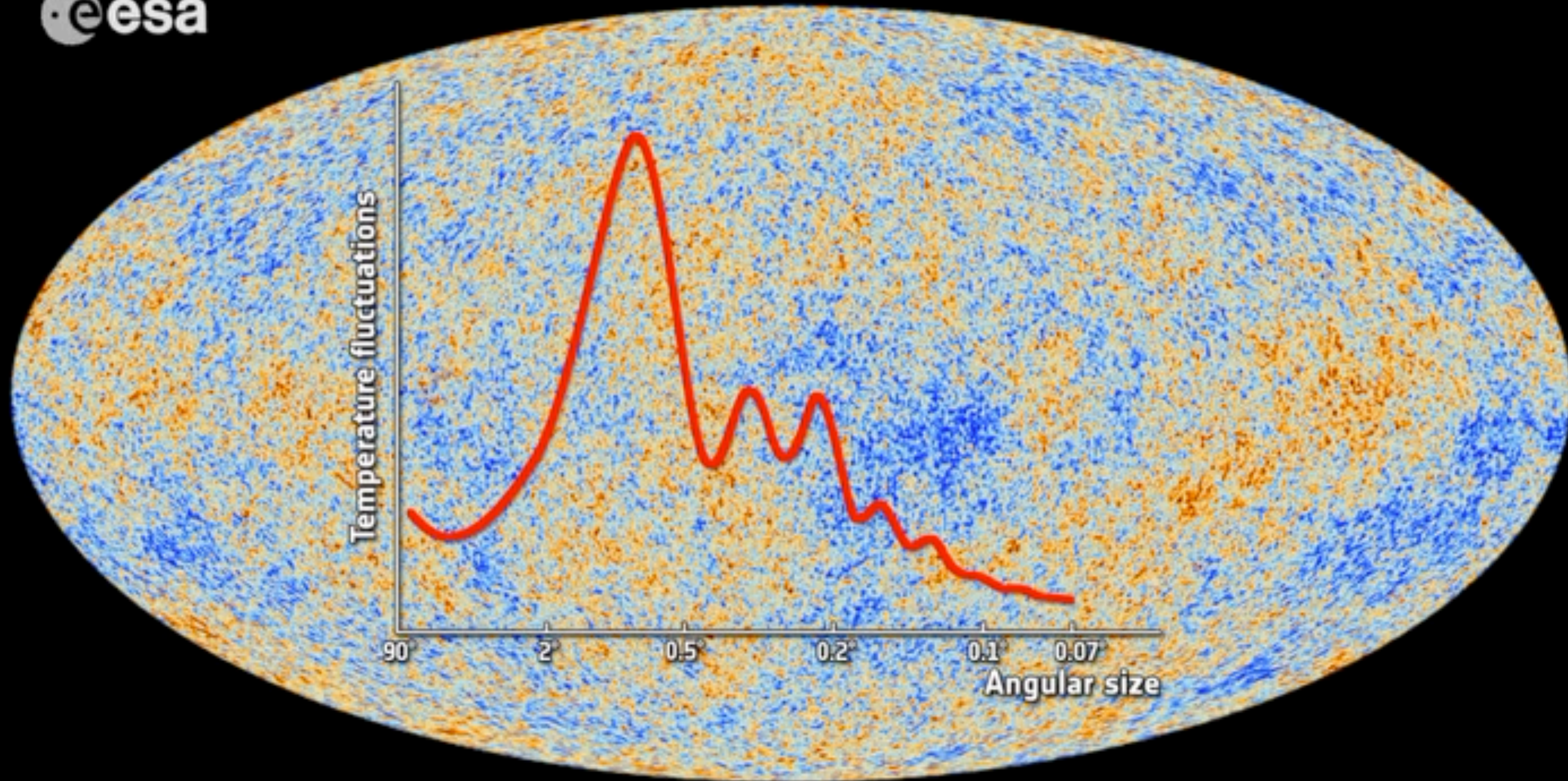
$$\langle T_{\ell} E_{\ell'}^* \rangle = \langle T_{\ell'}^* E_{\ell} \rangle = (2\pi)^2 \delta_D^{(2)}(\ell - \ell') C_{\ell}^{TE}$$

- The other combinations  $\langle TB \rangle$  and  $\langle EB \rangle$  are not invariant under the parity flip.



- **We can use these combinations to probe parity-violating physics (e.g., axions)**

# Power Spectrum, Explained



# Gravitational Field Equations (Einstein's Eq.)

$$\nabla^2 \Psi = 4\pi G a^2 \sum_{\alpha} \left[ \delta\rho_{\alpha} - \frac{3\dot{a}}{a} (\bar{\rho}_{\alpha} + \bar{P}_{\alpha}) \delta u_{\alpha} \right],$$

$$\partial_i \partial_j (\Phi - \Psi) = -8\pi G a^2 \partial_i \partial_j \sum_{\alpha} \pi_{\alpha},$$

## Energy Conservation

$$\frac{\partial}{\partial t} (\delta\rho_{\gamma} / \bar{\rho}_{\gamma}) - \frac{4q^2}{3a^2} \delta u_{\gamma} = 4\dot{\Psi},$$

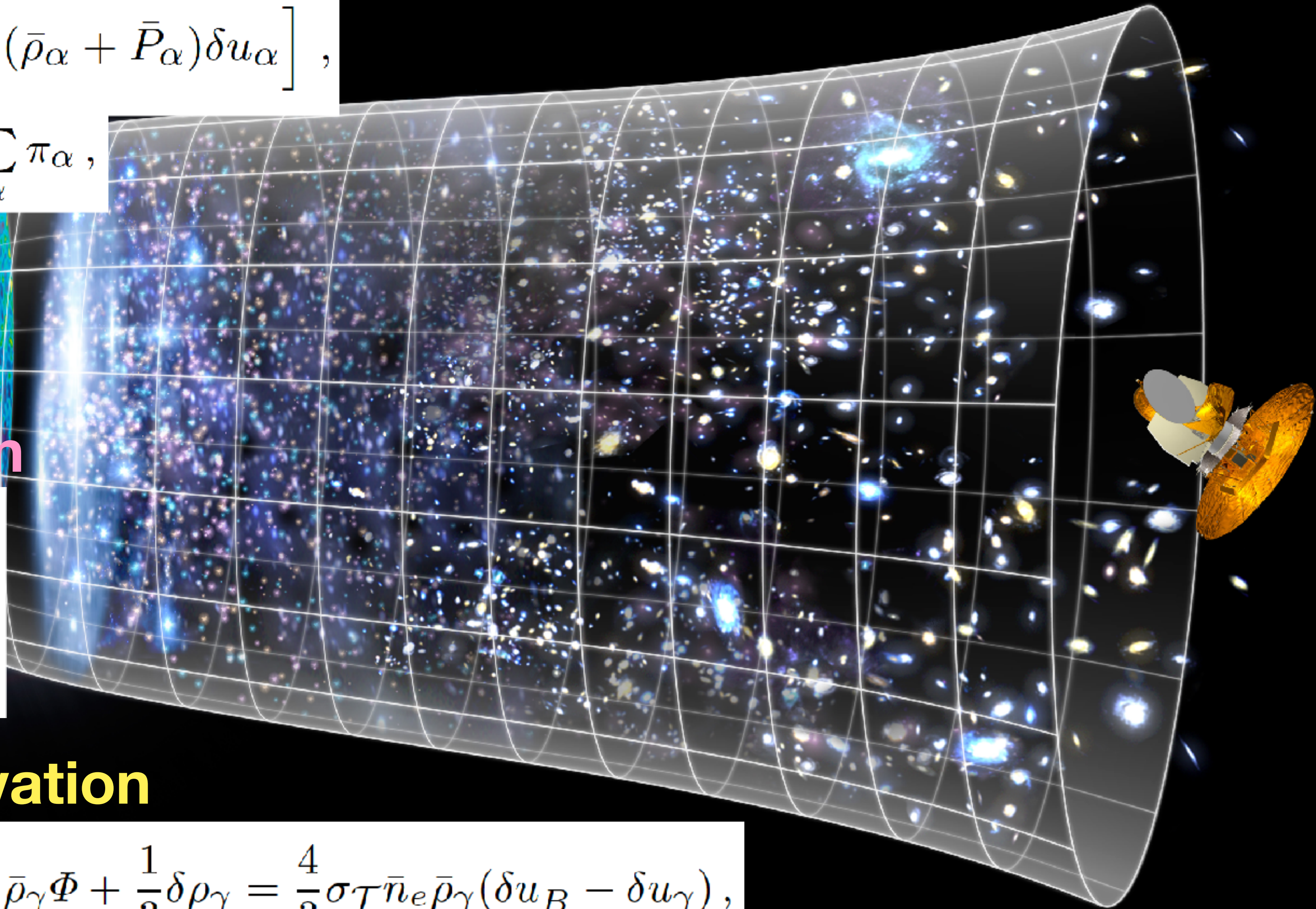
$$\frac{\partial}{\partial t} (\delta\rho_B / \bar{\rho}_B) - \frac{q^2}{a^2} \delta u_B = 3\dot{\Psi},$$

## Momentum Conservation

$$\frac{4}{3} \frac{\partial}{\partial t} (\bar{\rho}_{\gamma} \delta u_{\gamma}) + \frac{4\dot{a}}{a} \bar{\rho}_{\gamma} \delta u_{\gamma} + \frac{4}{3} \bar{\rho}_{\gamma} \Phi + \frac{1}{3} \delta\rho_{\gamma} = \frac{4}{3} \sigma_T \bar{n}_e \bar{\rho}_{\gamma} (\delta u_B - \delta u_{\gamma}),$$

$$\frac{\partial}{\partial t} (\bar{\rho}_B \delta u_B) + \frac{3\dot{a}}{a} \bar{\rho}_B \delta u_B + \bar{\rho}_B \Phi = -\frac{4}{3} \sigma_T \bar{n}_e \bar{\rho}_{\gamma} (\delta u_B - \delta u_{\gamma}),$$

*Laws of physics!*



Gravitational Field Equations

+

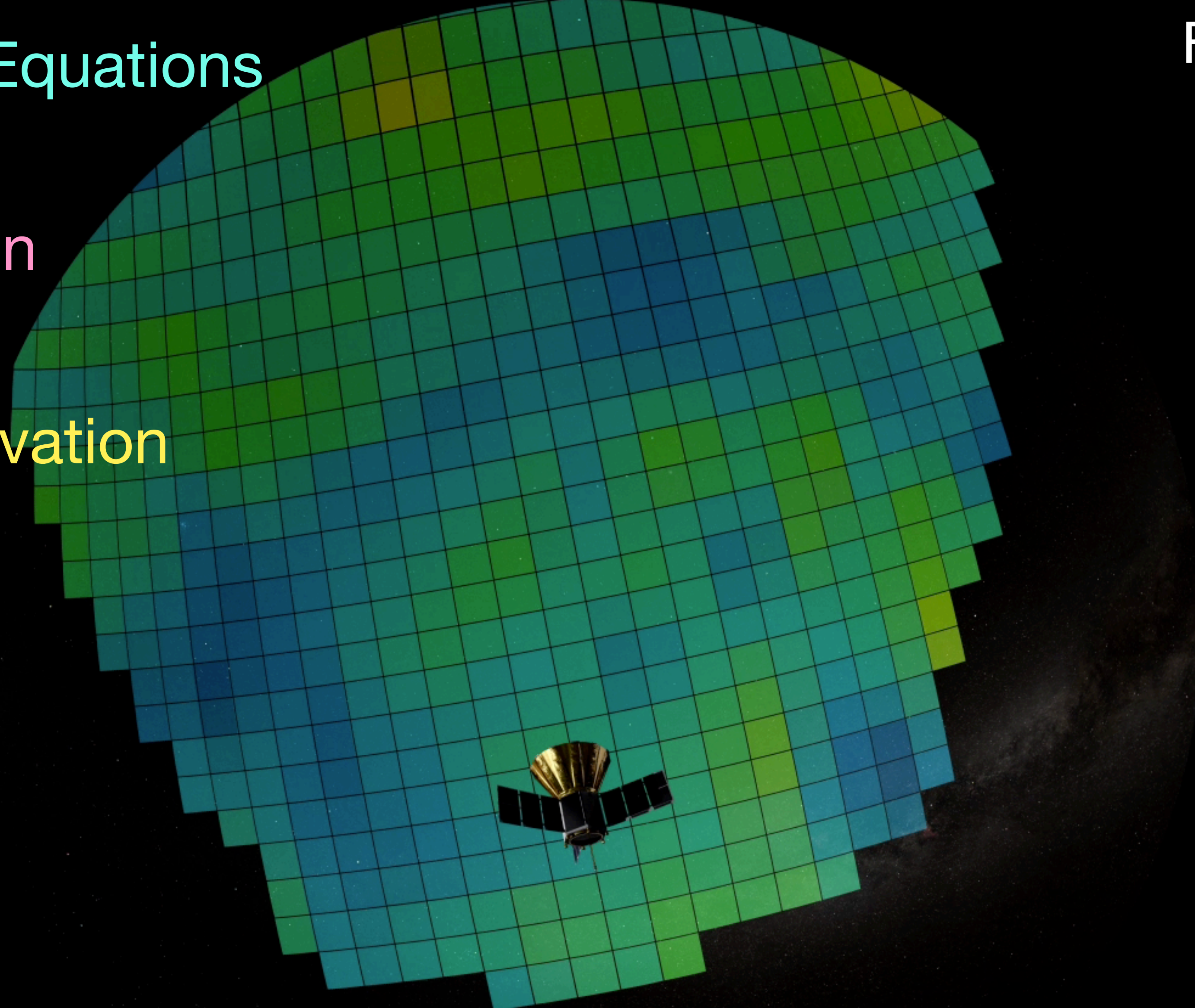
Energy Conservation

+

Momentum Conservation

||

**Sound Waves!**



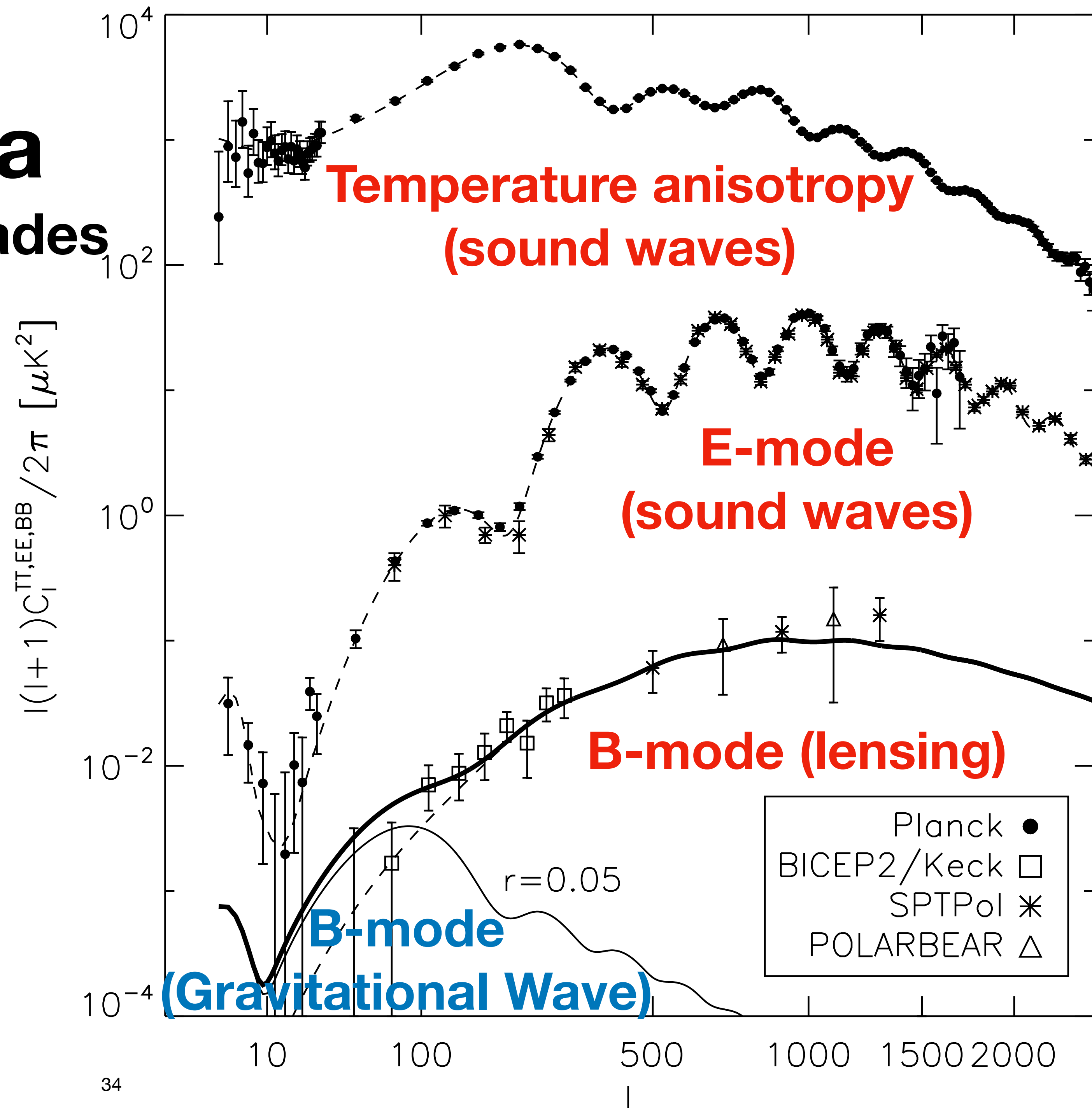




# CMB Power Spectra

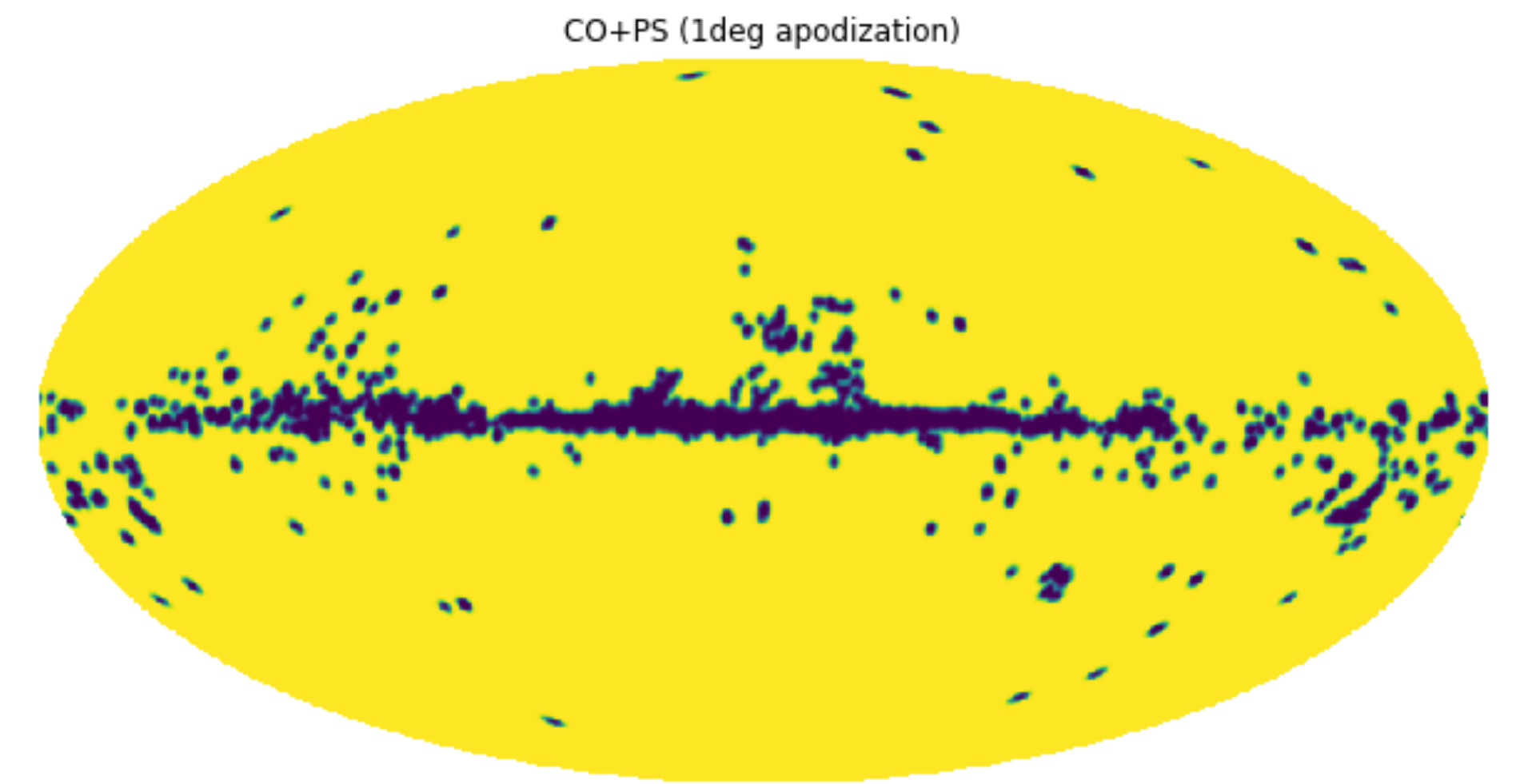
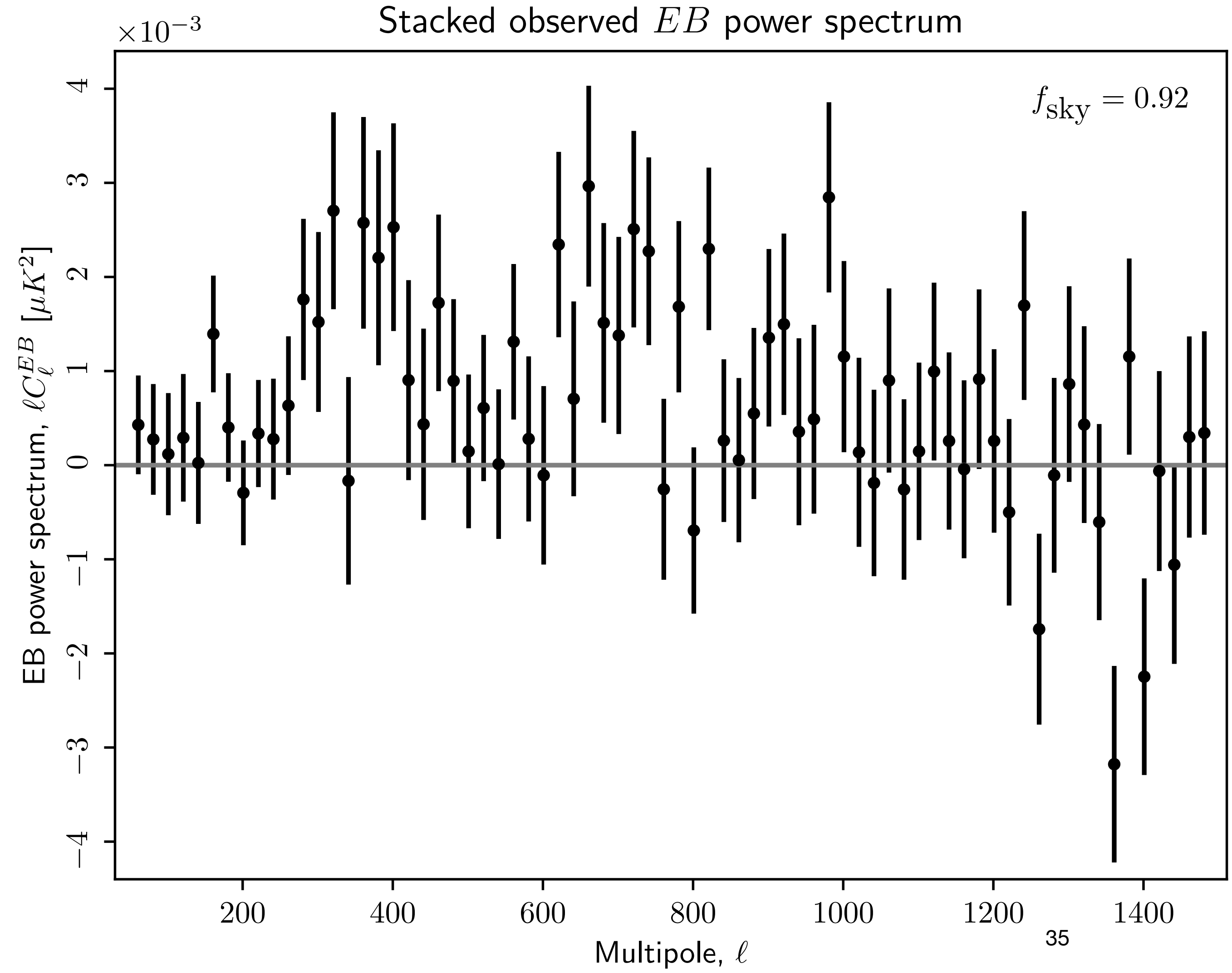
Progress over the last 3 decades

- This is the typical figure that you find in talks and lectures on CMB.
- The temperature power spectrum and the E- and B-mode polarisation power spectra have been measured well.
- **Our focus is the EB spectrum, which is not shown here.**



# This is the EB power spectrum (WMAP+Planck)

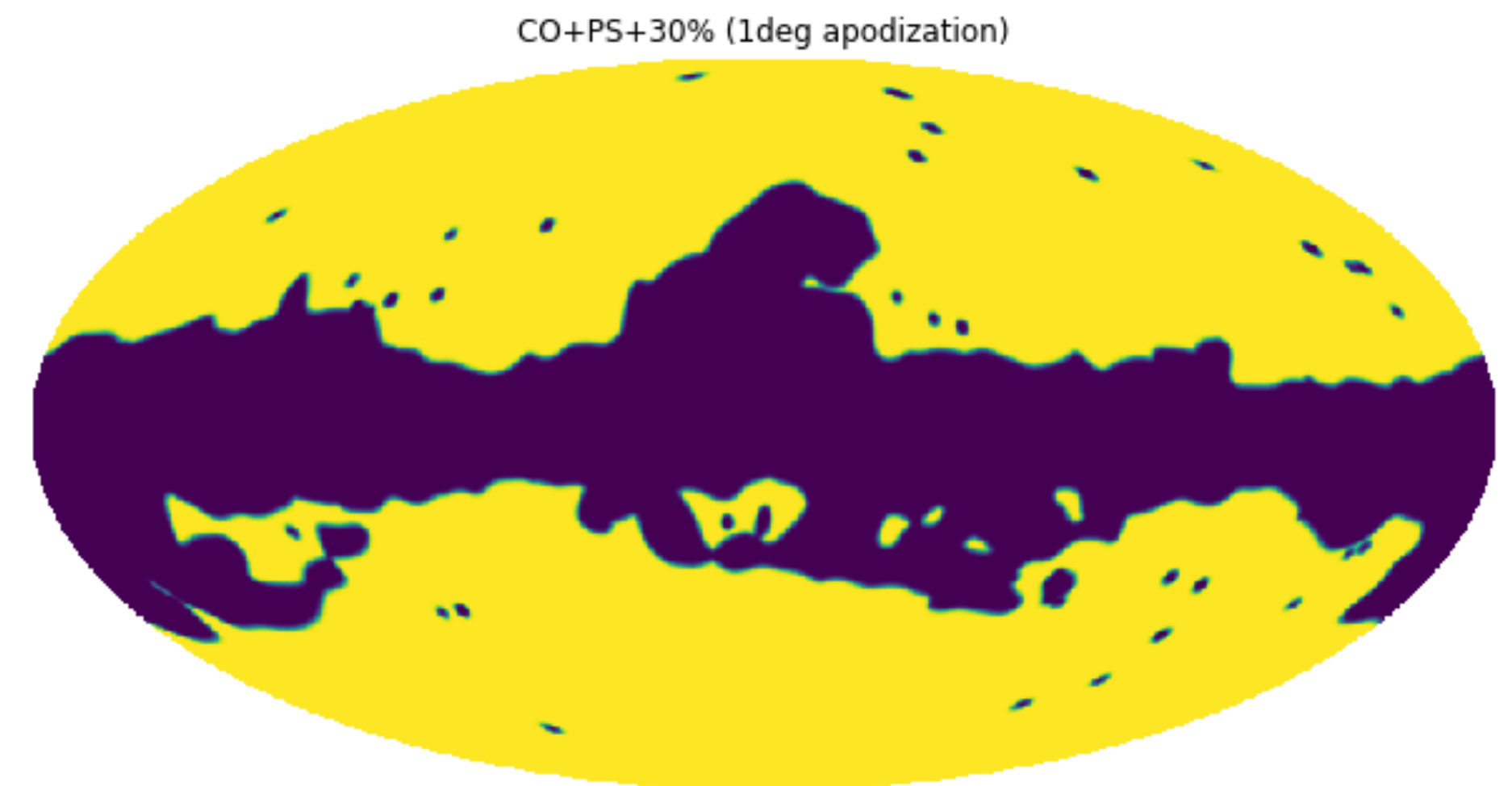
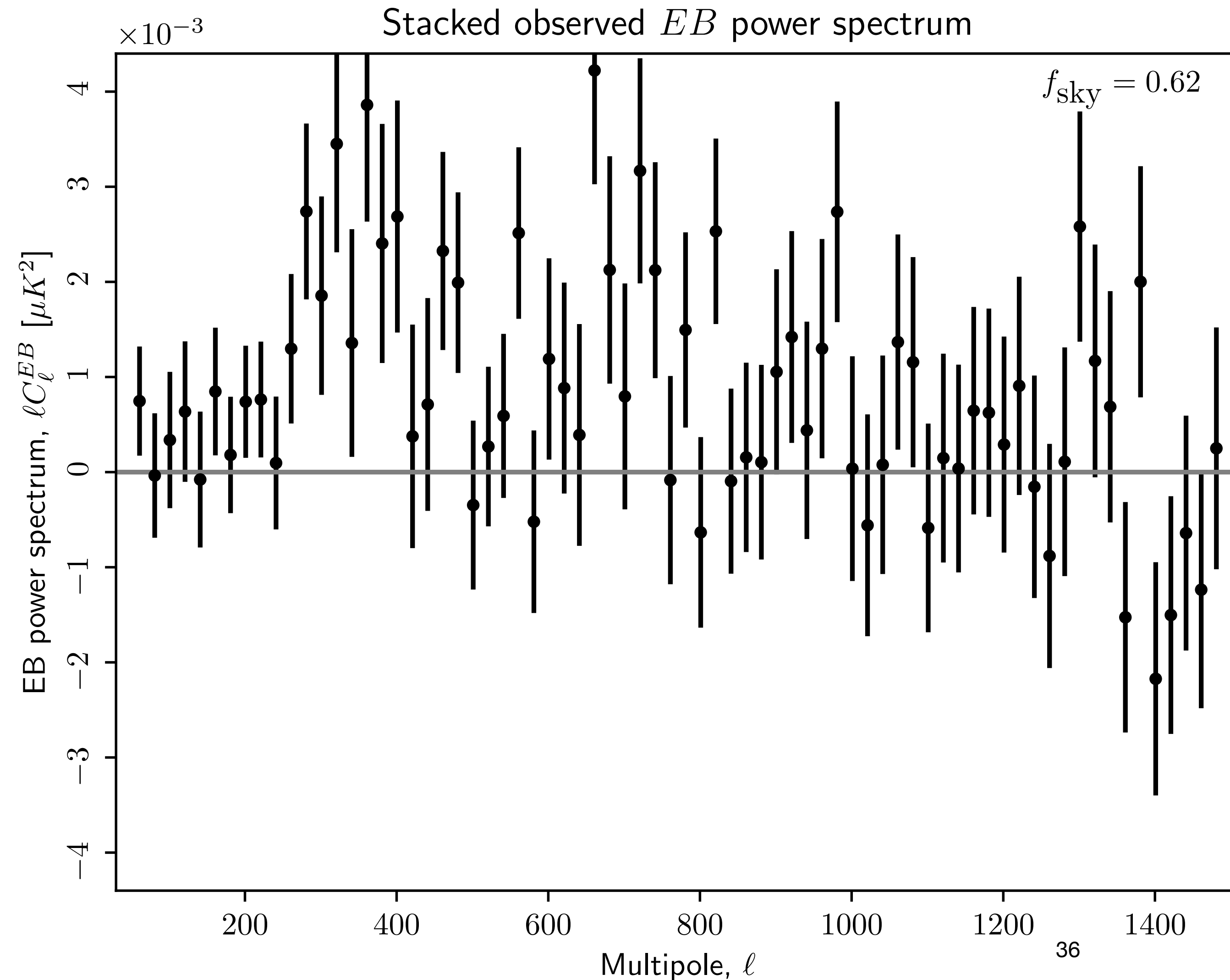
Nearly full-sky data (92% of the sky)



- $\chi^2 = 125.5$  for DOF=72
- Unambiguous signal of something!

# This is the EB power spectrum (WMAP+Planck)

Galactic plane removed (62% of the sky)



- $\chi^2 = 138.4$  for DOF=72
- The signal exists regardless of the Galactic mask. This rules out the Galactic foreground.

# The EB power spectrum from cosmic birefringence

# E-B mixing by rotation of the plane of linear polarisation

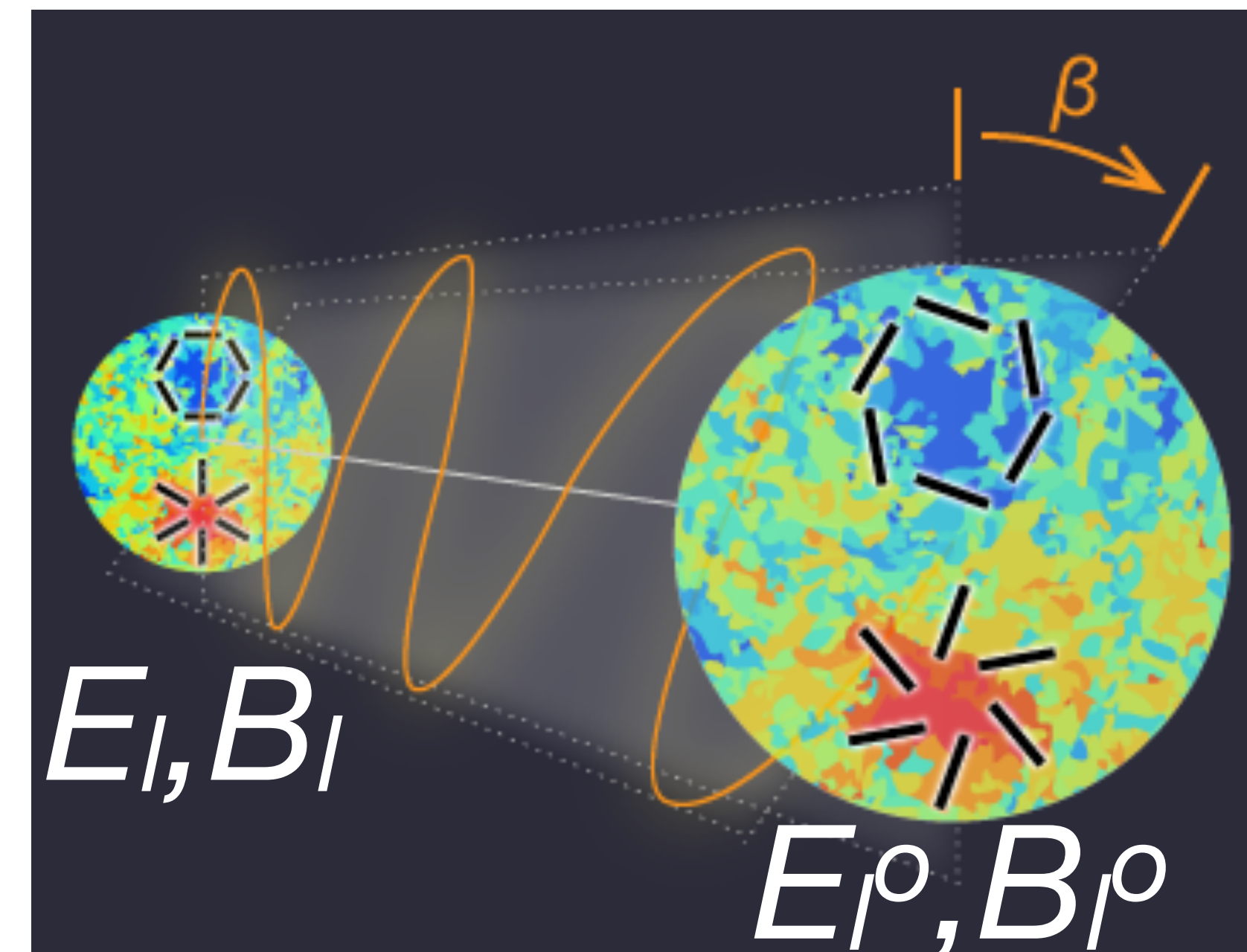
- Observed E- and B-mode polarisation,  $E_l^\circ$  and  $B_l^\circ$ , are related to those before rotation as

$$E_l^\circ \pm iB_l^\circ = (E_l \pm iB_l)e^{\pm 2i\beta}$$

- which gives

$$E_l^\circ = E_l \cos(2\beta) - B_l \sin(2\beta)$$

$$B_l^\circ = E_l \sin(2\beta) + B_l \cos(2\beta)$$



# Searching for cosmic birefringence

- Computing observed difference between EE and BB spectra,

$$C_{\ell}^{EE, \text{obs}} = C_{\ell}^{EE} \cos^2(2\beta) + C_{\ell}^{BB} \sin^2(2\beta) - C_{\ell}^{EB} \sin(4\beta)$$

$$C_{\ell}^{BB, \text{obs}} = C_{\ell}^{EE} \sin^2(2\beta) + C_{\ell}^{BB} \cos^2(2\beta) + C_{\ell}^{EB} \sin(4\beta)$$

$$C_{\ell}^{EE, \text{obs}} - C_{\ell}^{BB, \text{obs}} = (C_{\ell}^{EE} - C_{\ell}^{BB}) \cos(4\beta) - 2C_{\ell}^{EB} \sin(4\beta)$$

- We find

$$\begin{aligned} C_{\ell}^{EB, \text{obs}} &= \frac{1}{2} (C_{\ell}^{EE} - C_{\ell}^{BB}) \sin(4\beta) + C_{\ell}^{EB} \cos(4\beta) \\ &= \frac{1}{2} \underline{(C_{\ell}^{EE, \text{obs}} - C_{\ell}^{BB, \text{obs}})} \tan(4\beta) + \frac{C_{\ell}^{EB}}{\cos(4\beta)} \end{aligned}$$

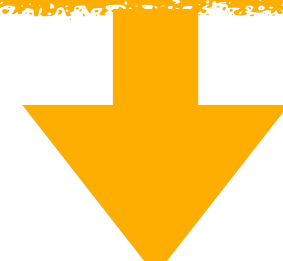
EB is generated by the *difference* between EE and BB spectra.

# CMB Power Spectra

**EE >> BB!**

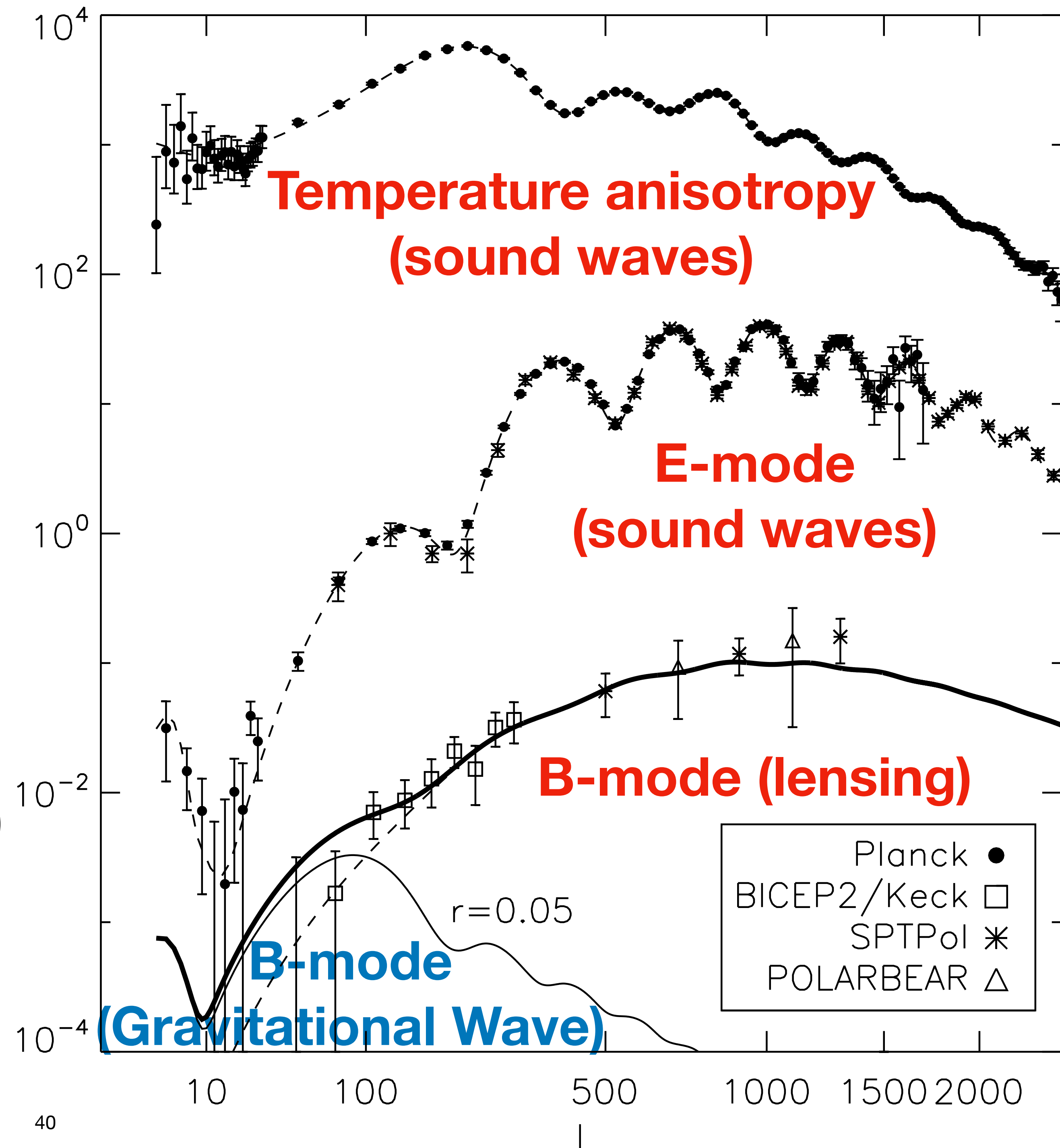
- In our Universe, CMB EE is much greater than BB. This makes CMB sensitive to birefringence.

$$C_{\ell}^{EB,obs} = \frac{1}{2} (C_{\ell}^{EE,obs} - C_{\ell}^{BB,obs}) \tan(4\beta)$$



**The expectation: EB should look like EE. Let's look at the data!**

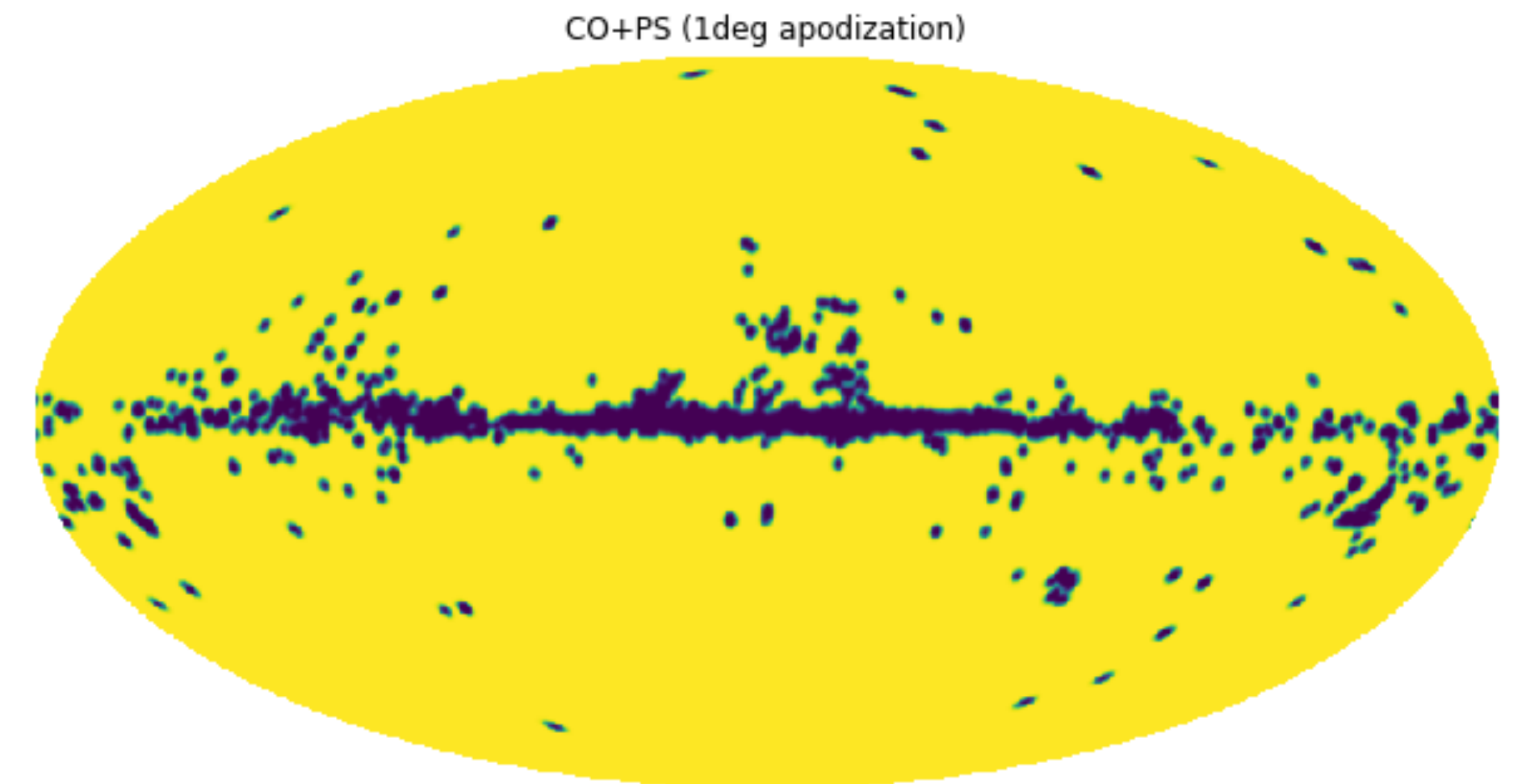
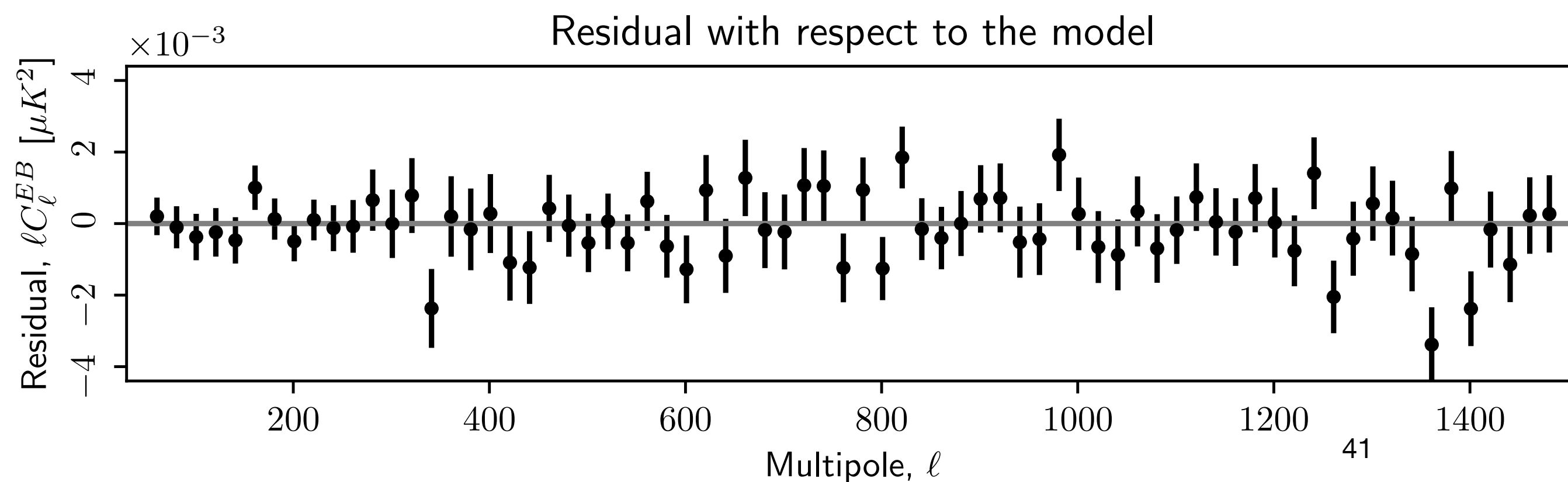
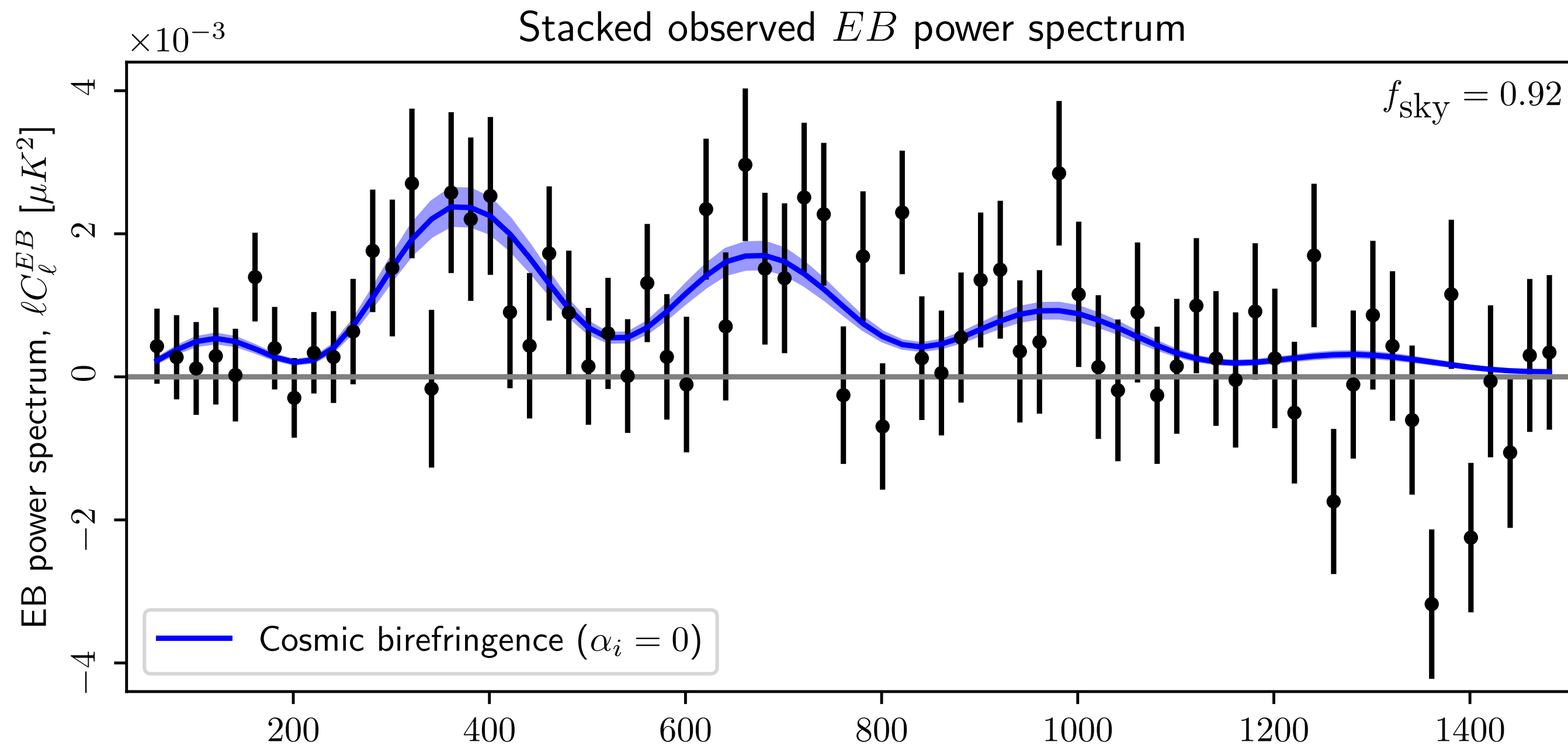
$l(l+1)C_l^{TT,EE,BB} / 2\pi \text{ [}\mu\text{K}^2\text{]}$





# Cosmic Birefringence fits well(?)

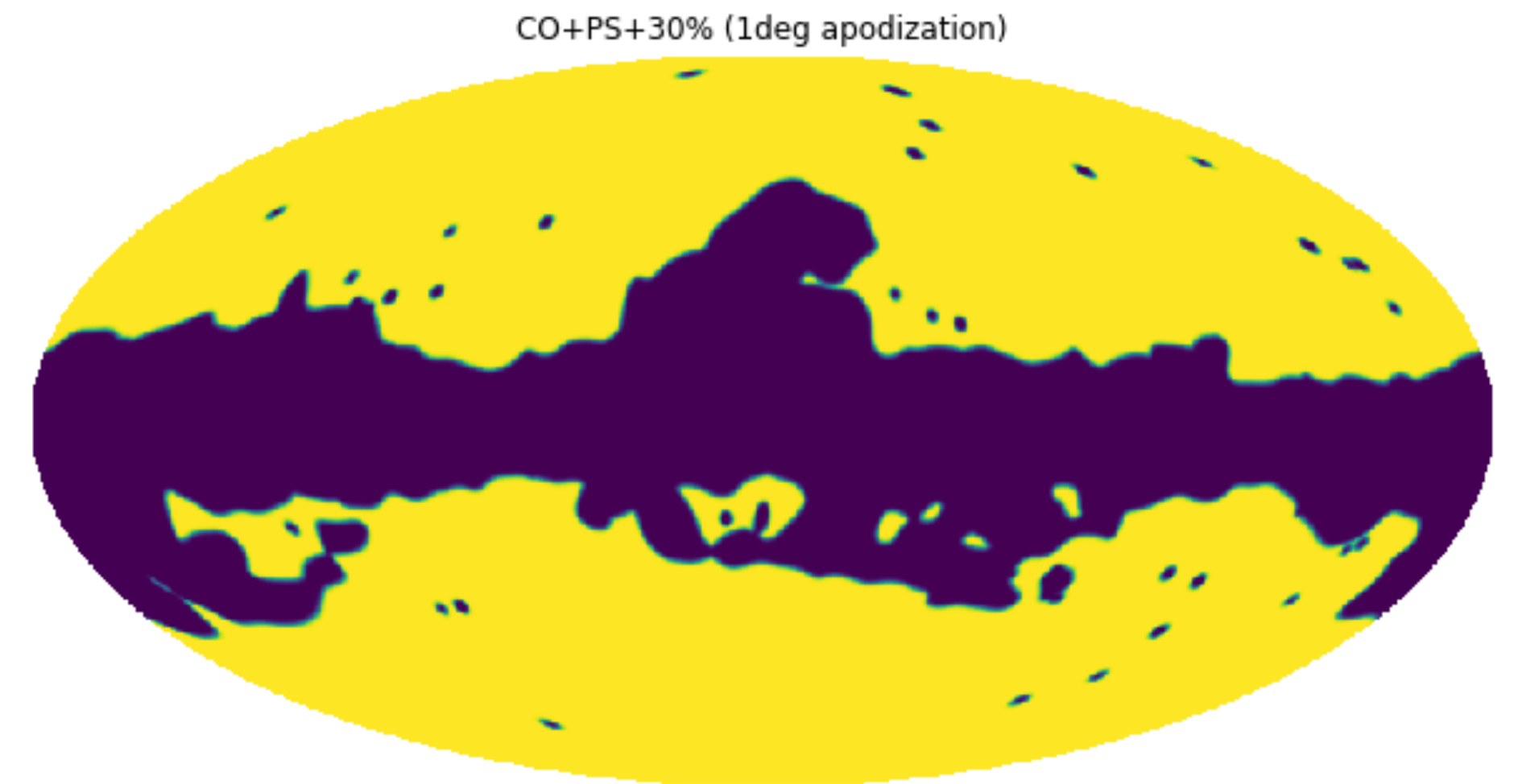
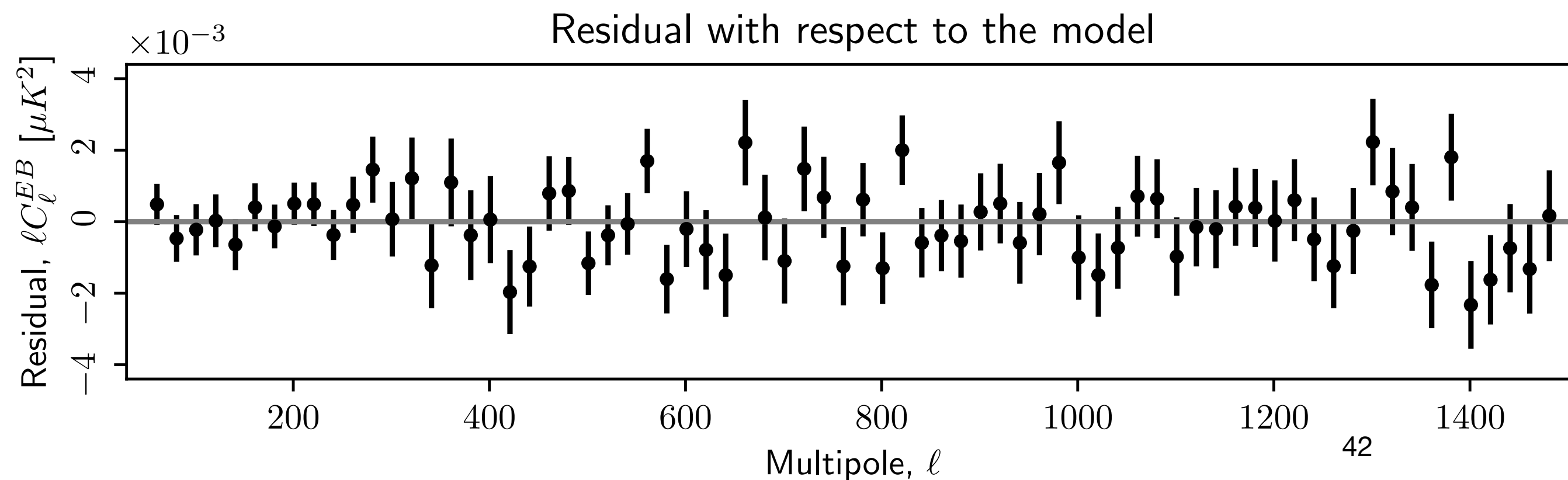
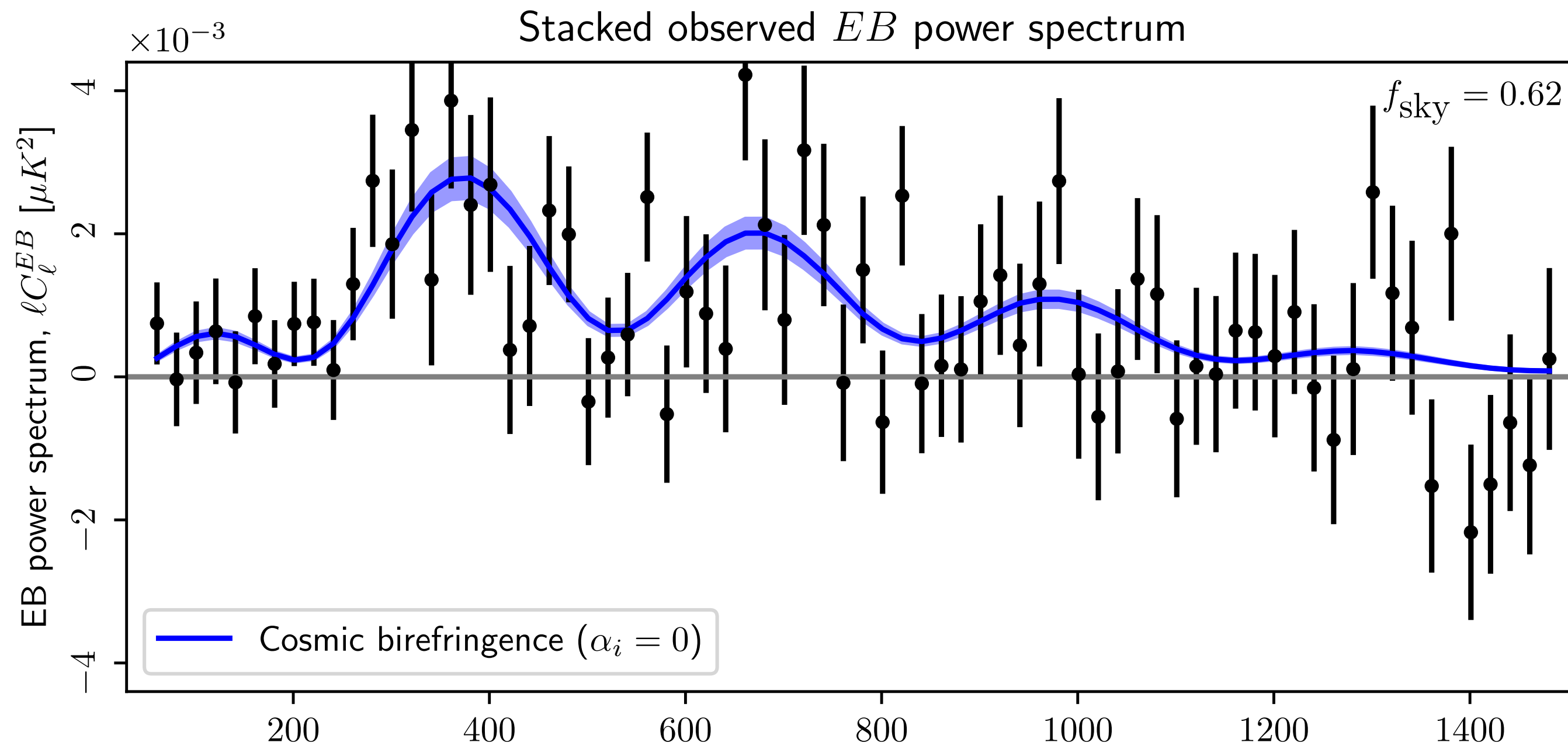
Nearly full-sky data (92% of the sky)



- $\beta = 0.288 \pm 0.032$  deg
- $\chi^2 = 66.1$
- Good fit!  $9\sigma$  detection?

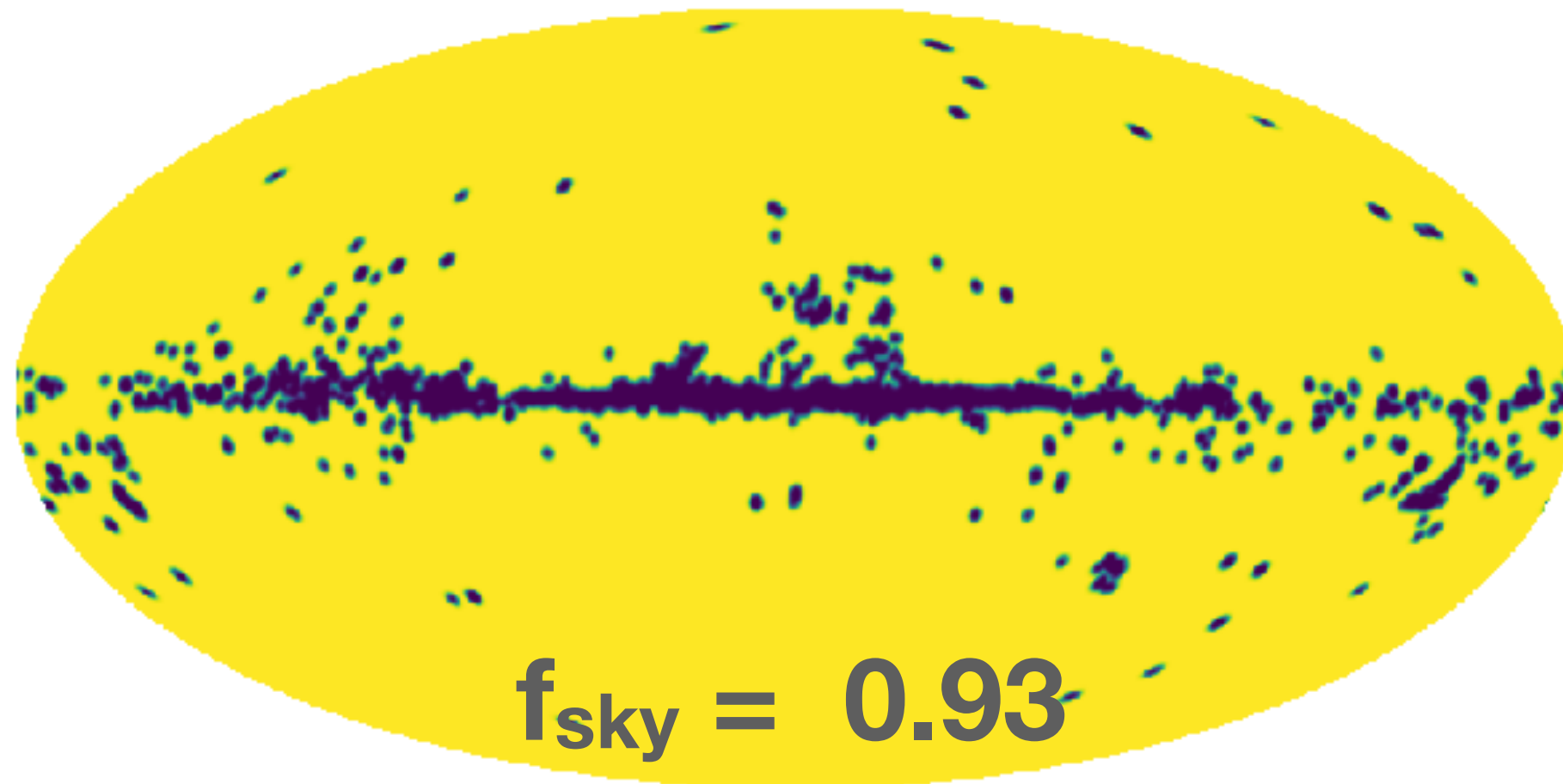
# Cosmic Birefringence fits well(?)

## Galactic plane removed (62% of the sky)



- $\beta = 0.330 \pm 0.035$  deg
- $\chi^2 = 64.5$
- Signal is robust with respect to the Galactic mask.

CO+PS (1deg apodization)

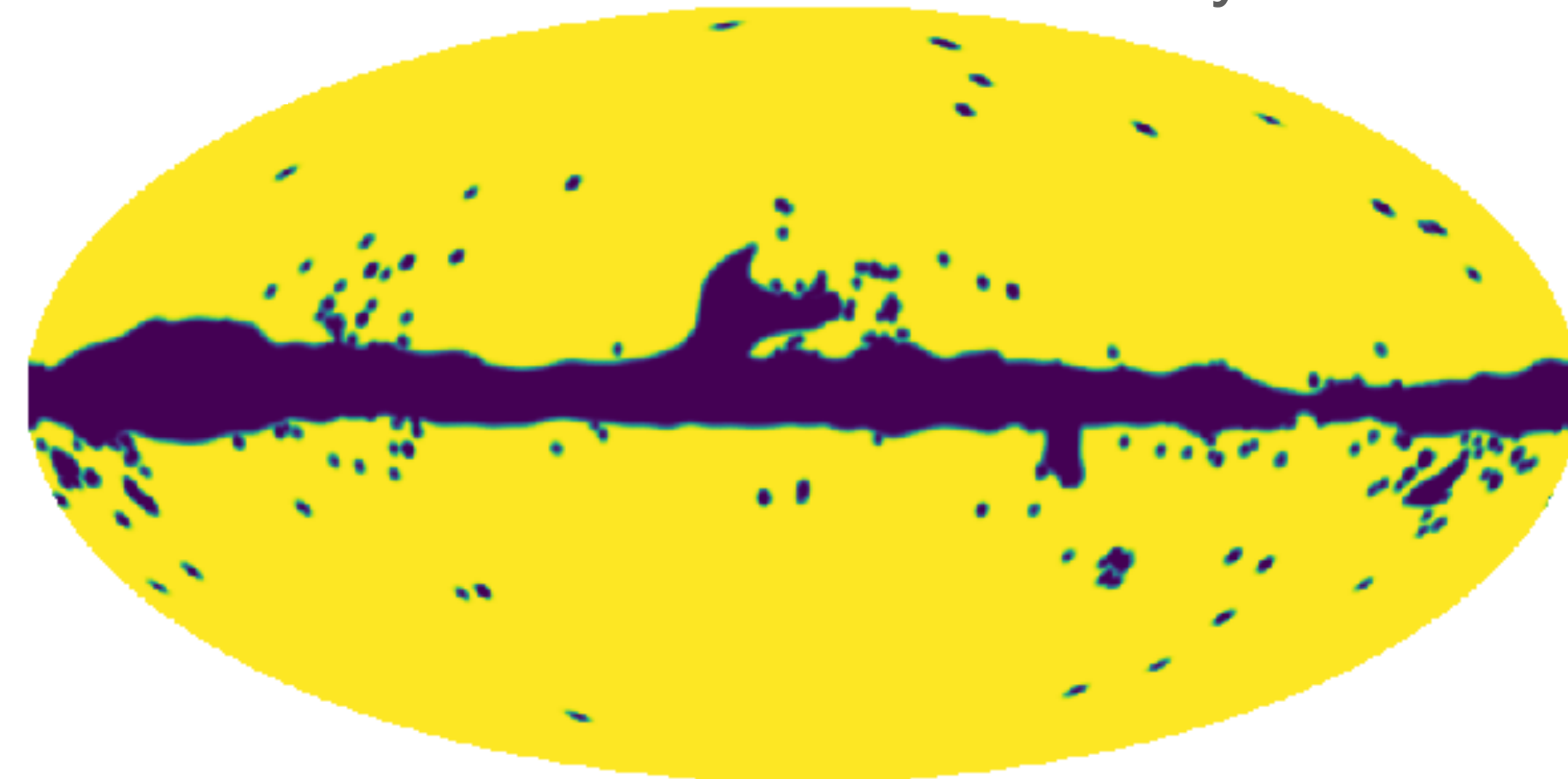


$f_{\text{sky}} = 0.93$

= nearly full sky

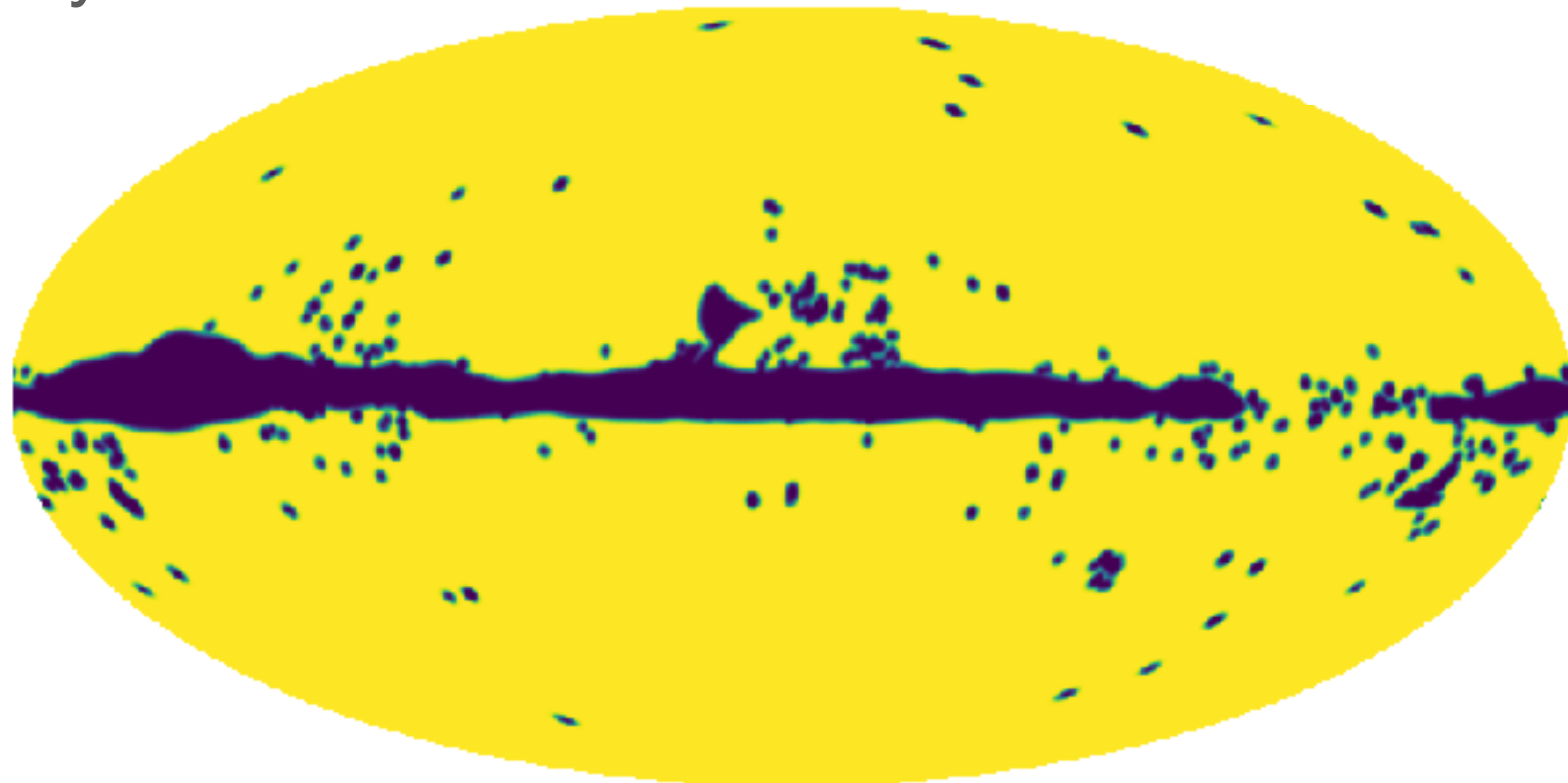
CO+PS+5% (1deg apodization)

$f_{\text{sky}} = 0.85$



$f_{\text{sky}} = 0.90$

CO+PS+5% (1deg apodization)



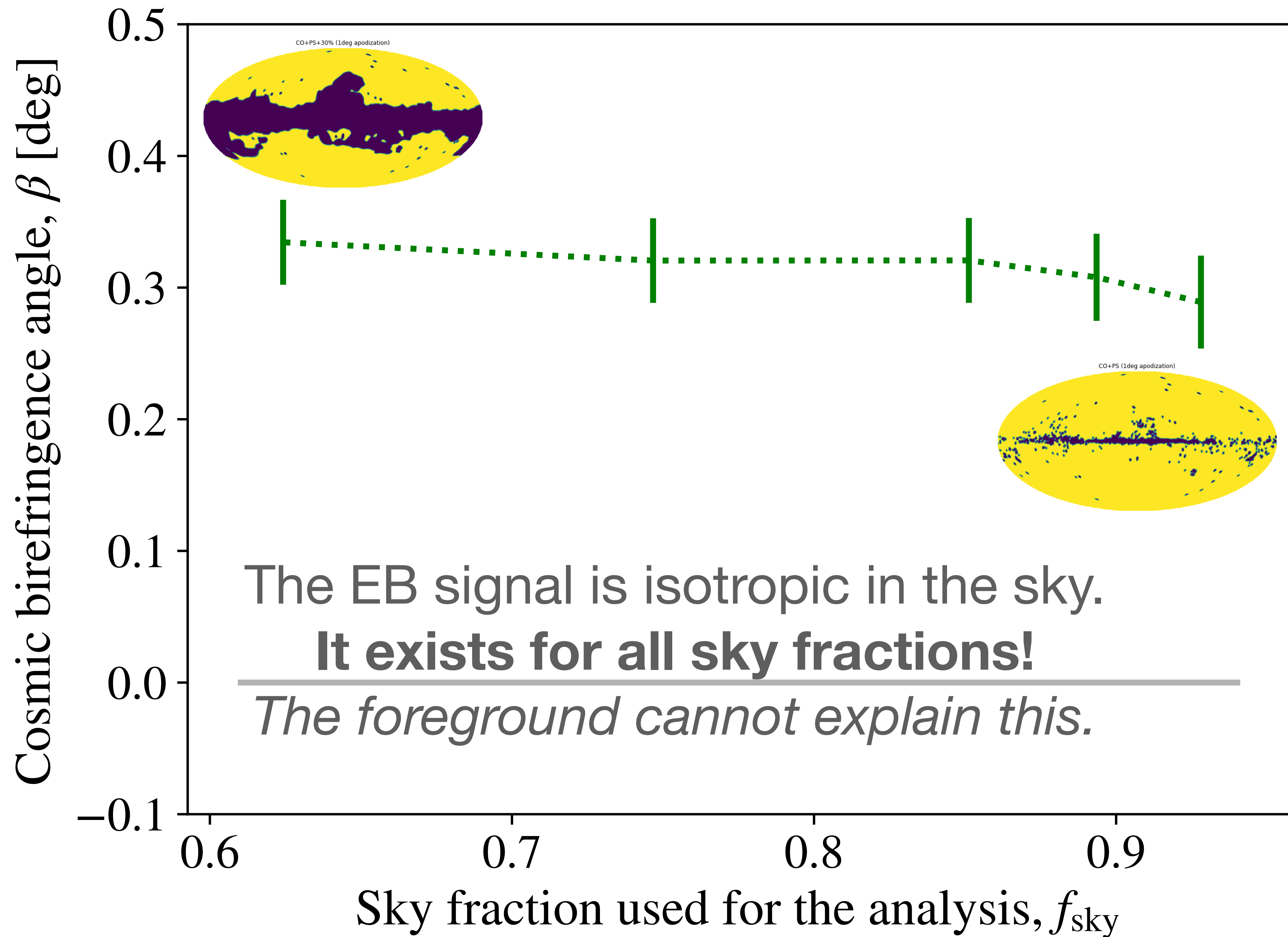
CO+PS+20% (1deg apodization)

CO+PS+30% (1deg apodization)



$f_{\text{sky}} = 0.75$

$f_{\text{sky}} = 0.63$



# **The Biggest Problem: Miscalibration of detectors**

# Impact of miscalibration of polarisation angles

## Cosmic or Instrumental?



- Is the plane of linear polarisation rotated by the genuine cosmic birefringence effect, or simply because the polarisation-sensitive directions of detectors are rotated with respect to the sky coordinates (and we did not know it)?

- If the detectors are rotated by  $\alpha$ , it seems that we can measure only the **sum  $\alpha + \beta$** .

# The past measurements

The quoted uncertainties are all statistical only (68%CL)

- $\alpha + \beta = -6.0 \pm 4.0$  deg (Feng et al. 2006) **first measurement**
- $\alpha + \beta = -1.1 \pm 1.4$  deg (WMAP Collaboration, Komatsu et al. 2009; 2011)
- $\alpha + \beta = 0.55 \pm 0.82$  deg (QUaD Collaboration, Wu et al. 2009)
- ...
- $\alpha + \beta = 0.31 \pm 0.05$  deg (Planck Collaboration 2016)
- $\alpha + \beta = -0.61 \pm 0.22$  deg (POLARBEAR Collaboration 2020)
- $\alpha + \beta = 0.63 \pm 0.04$  deg (SPT Collaboration, Bianchini et al. 2020)
- $\alpha + \beta = 0.12 \pm 0.06$  deg (ACT Collaboration, Namikawa et al. 2020)
- $\alpha + \beta = 0.07 \pm 0.09$  deg (ACT Collaboration, Choi et al. 2020)

**Why not yet discovered?**

# The past measurements

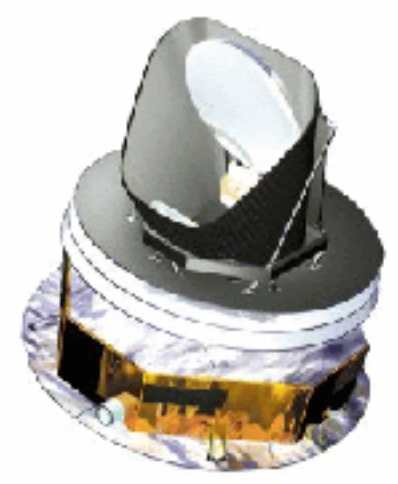
Now including the estimated systematic errors on  $\alpha$

- $\beta = -6.0 \pm 4.0 \pm ??$  deg (Feng et al. 2006)
- $\beta = -1.1 \pm 1.4 \pm 1.5$  deg (WMAP Collaboration, Komatsu et al. 2009; 2011)
- $\beta = 0.55 \pm 0.82 \pm 0.5$  deg (QUaD Collaboration, Wu et al. 2009)
- ...
- $\beta = 0.31 \pm 0.05 \pm 0.28$  deg (Planck Collaboration 2016)
- $\beta = -0.61 \pm 0.22 \pm ??$  deg (POLARBEAR Collaboration 2020)
- $\beta = 0.63 \pm 0.04 \pm ??$  deg (SPT Collaboration, Bianchini et al. 2020)
- $\beta = 0.12 \pm 0.06 \pm ??$  deg (ACT Collaboration, Namikawa et al. 2020)
- $\beta = 0.07 \pm 0.09 \pm ??$  deg (ACT Collaboration, Choi et al. 2020)

**Uncertainty in the calibration of  $\alpha$  has been the major limitation**



**The Key Idea: The polarised Galactic foreground emission as a calibrator**

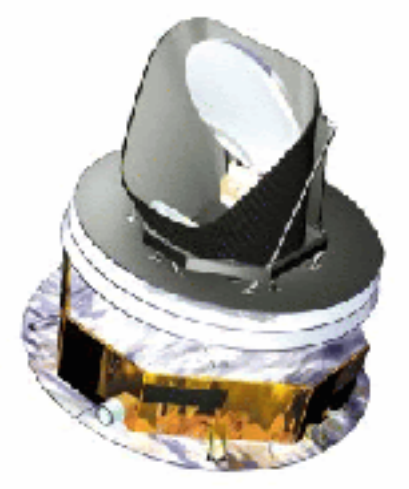


ESA's Planck

# Polarised dust emission within our Milky Way!

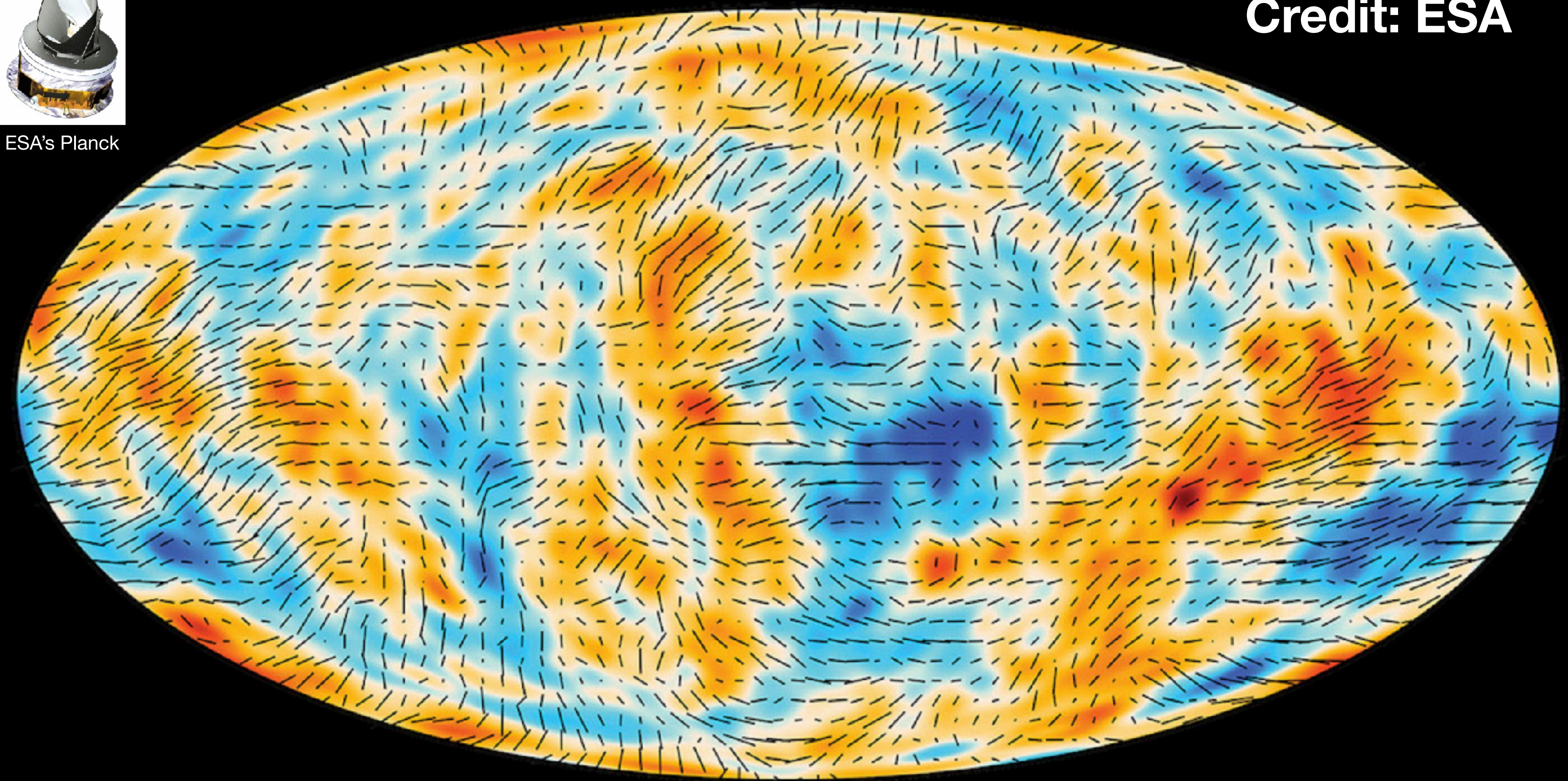
Emitted “right there” - it would not be affected by the cosmic birefringence.

Directions of the magnetic field inferred from polarisation of the thermal dust emission in the Milky Way



ESA's Planck

Credit: ESA

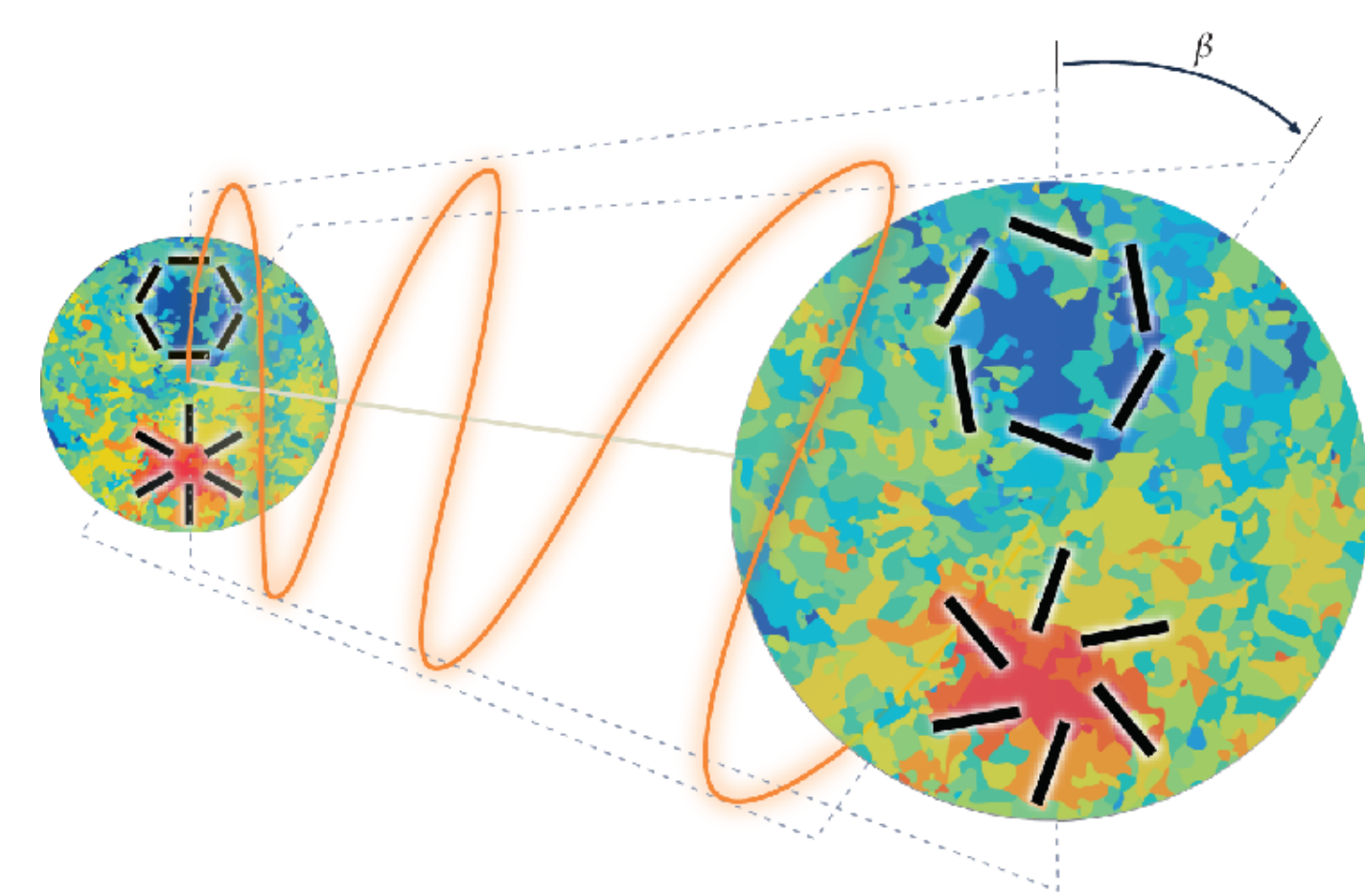


Foreground-cleaned Temperature (smoothed) + Polarisation

Emitted 13.8 billions years ago

# Searching for the birefringence

## Including the miscalibration angle



- **Idea:** Miscalibration of the polarization angle  $\alpha$  rotates both the foreground and CMB, but  $\beta$  affects only the CMB.

$$E_{\ell,m}^o = E_{\ell,m}^{\text{fg}} \cos(2\alpha) - B_{\ell,m}^{\text{fg}} \sin(2\alpha) + E_{\ell,m}^{\text{CMB}} \cos(2\alpha + 2\beta) - B_{\ell,m}^{\text{CMB}} \sin(2\alpha + 2\beta) + E_{\ell,m}^{\text{N}}$$

$$B_{\ell,m}^o = E_{\ell,m}^{\text{fg}} \sin(2\alpha) + B_{\ell,m}^{\text{fg}} \cos(2\alpha) + E_{\ell,m}^{\text{CMB}} \sin(2\alpha + 2\beta) + B_{\ell,m}^{\text{CMB}} \cos(2\alpha + 2\beta) + B_{\ell,m}^{\text{N}}$$

noise

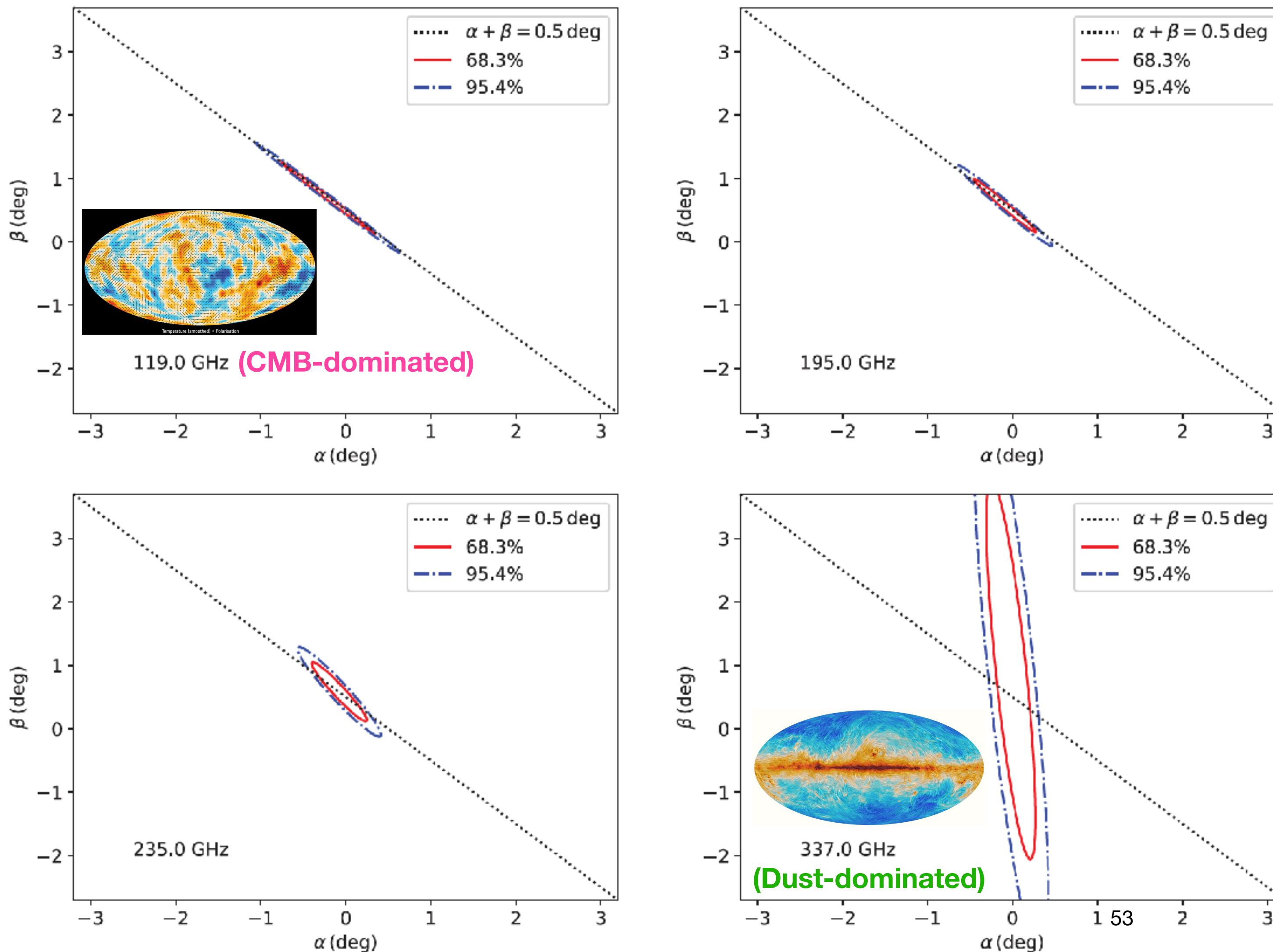
- Thus,

$$\langle C_{\ell}^{EB,o} \rangle = \frac{\tan(4\alpha)}{2} \left( \underbrace{\langle C_{\ell}^{EE,o} \rangle - \langle C_{\ell}^{BB,o} \rangle}_{\text{measured}} \right) + \frac{\sin(4\beta)}{2 \cos(4\alpha)} \left( \underbrace{\langle C_{\ell}^{EE,\text{CMB}} \rangle - \langle C_{\ell}^{BB,\text{CMB}} \rangle}_{\text{known accurately}} \right) + \frac{1}{\cos(4\alpha)} \langle C_{\ell}^{EB,\text{fg}} \rangle + \frac{\cos(4\beta)}{\cos(4\alpha)} \langle C_{\ell}^{EB,\text{CMB}} \rangle.$$

Key: No explicit modelling of the foreground EE and BB is necessary

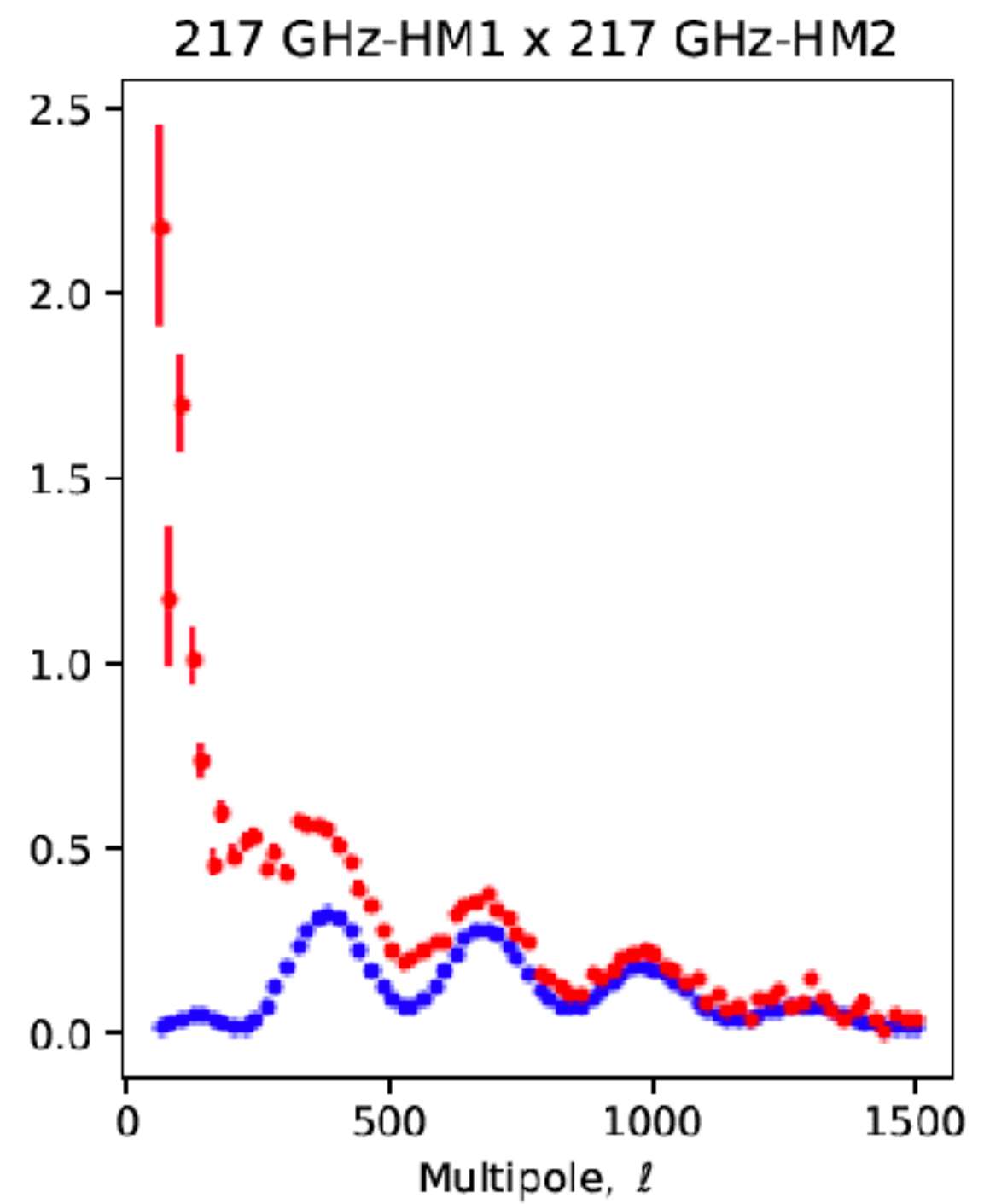
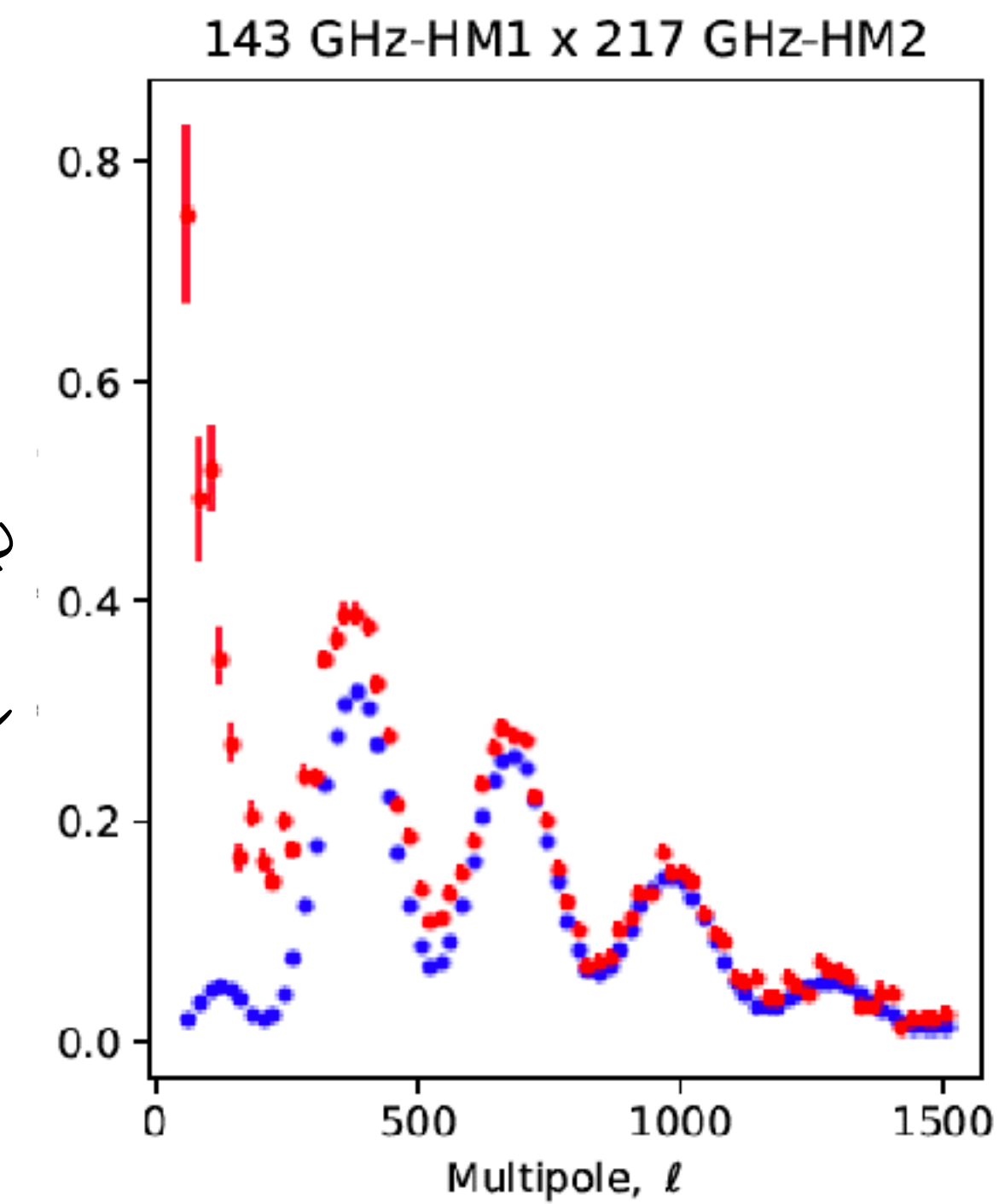
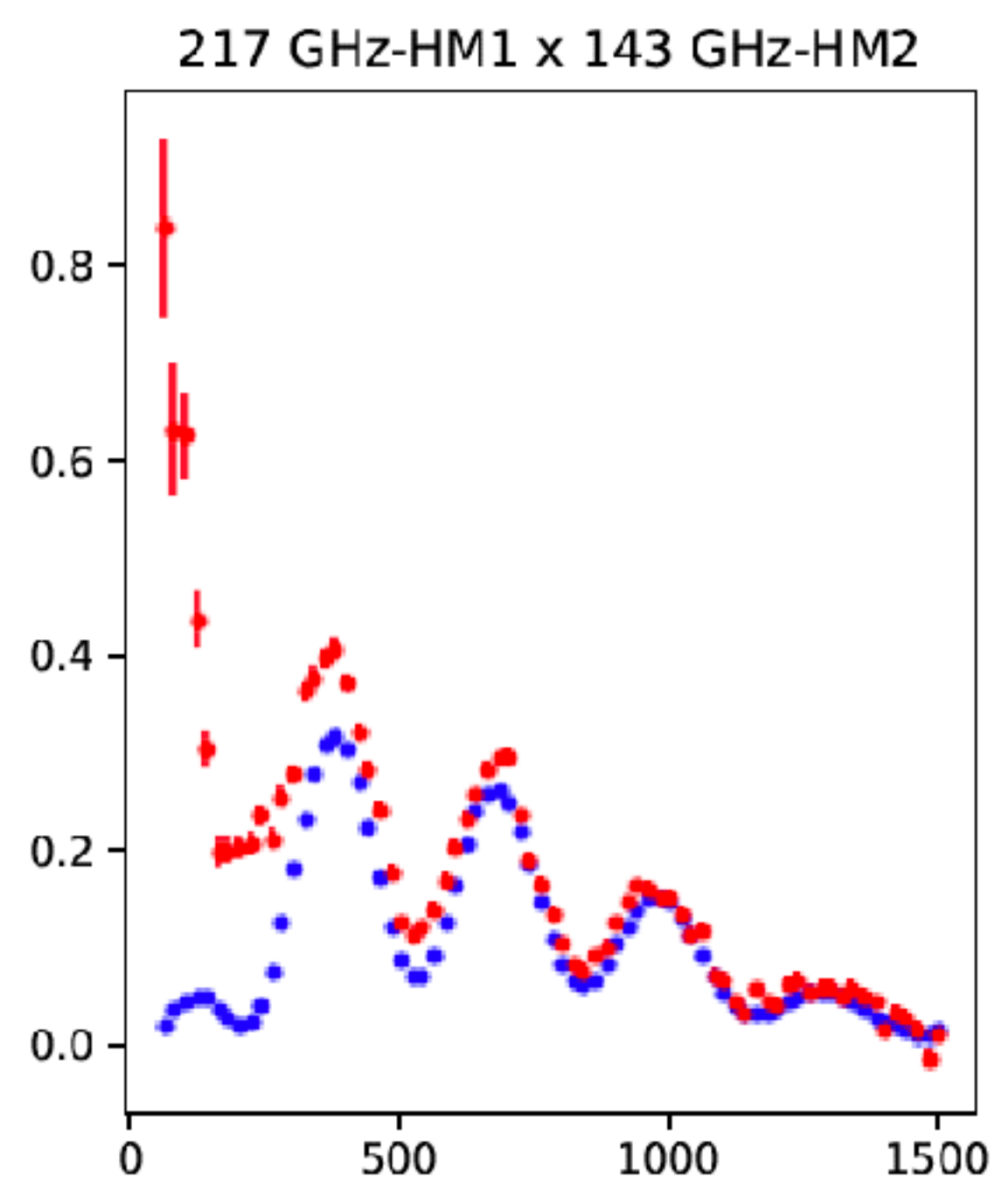
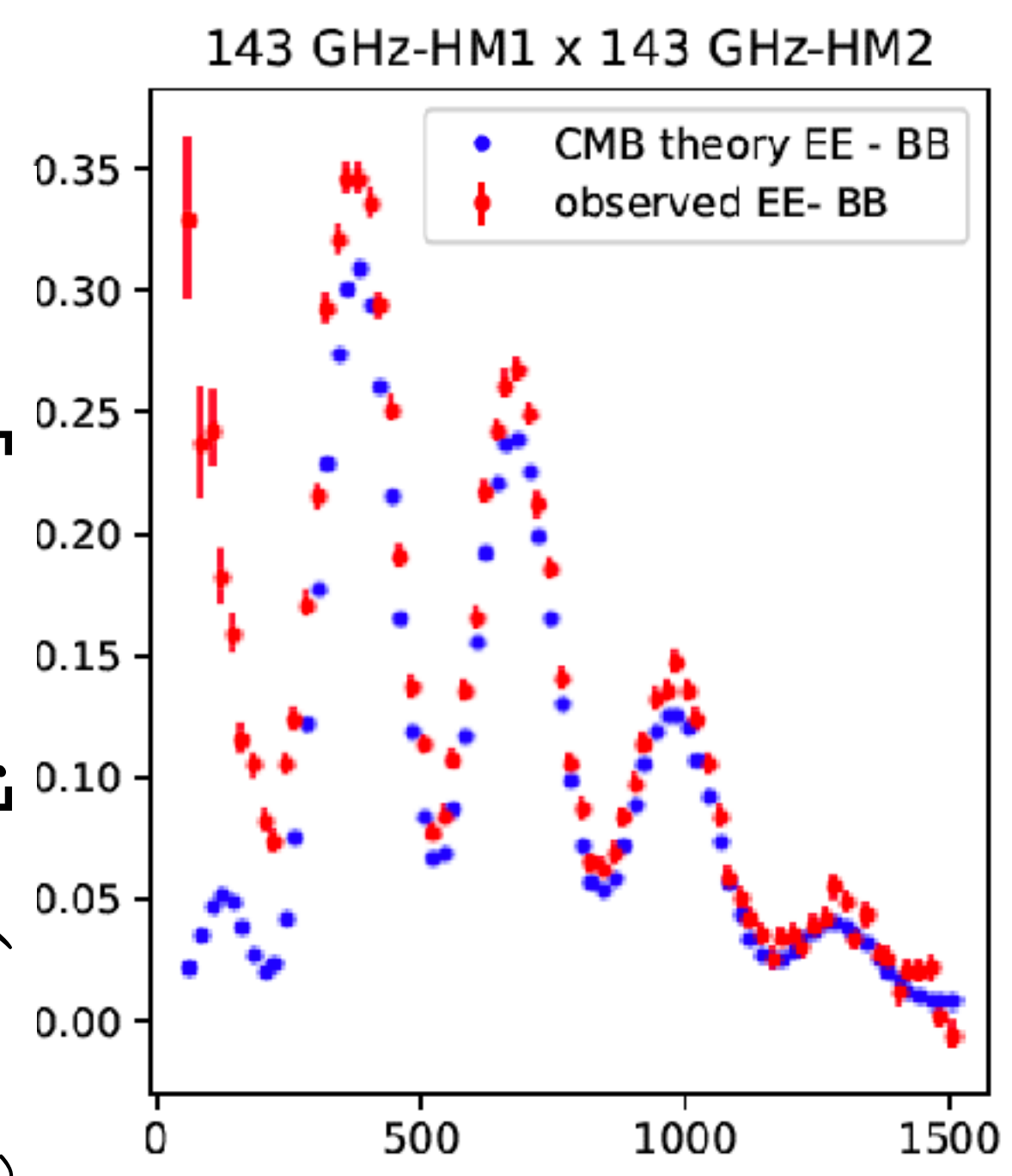
# How does it work?

## Simulation of future CMB data (LiteBIRD)



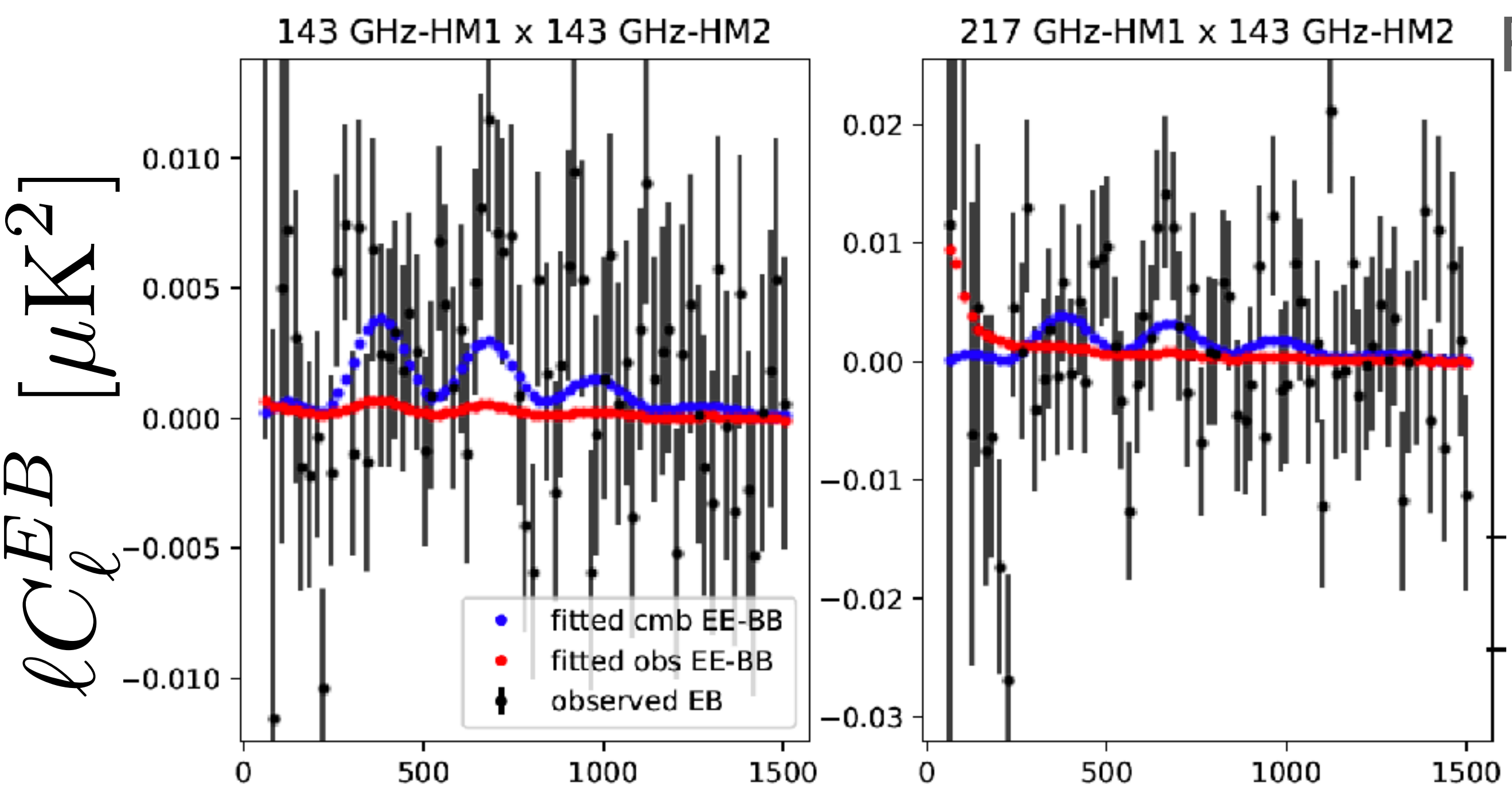
- When the data are dominated by CMB, the sum of two angles,  $\alpha + \beta$ , is determined precisely.
  - This is the diagonal line.
- The foreground determines  $\alpha$  with some uncertainty, breaking the degeneracy. Then  $\sigma(\beta) \sim \sigma(\alpha)$  because  $\sigma(\alpha + \beta) \ll \sigma(\alpha)$ .
- When the data are dominated by the foreground, it can determine  $\alpha$  but not  $\beta$  due to the lack of sensitivity to the CMB.

$\ell(C_\ell^{EE} - C_\ell^{BB}) [\mu\text{K}^2]$



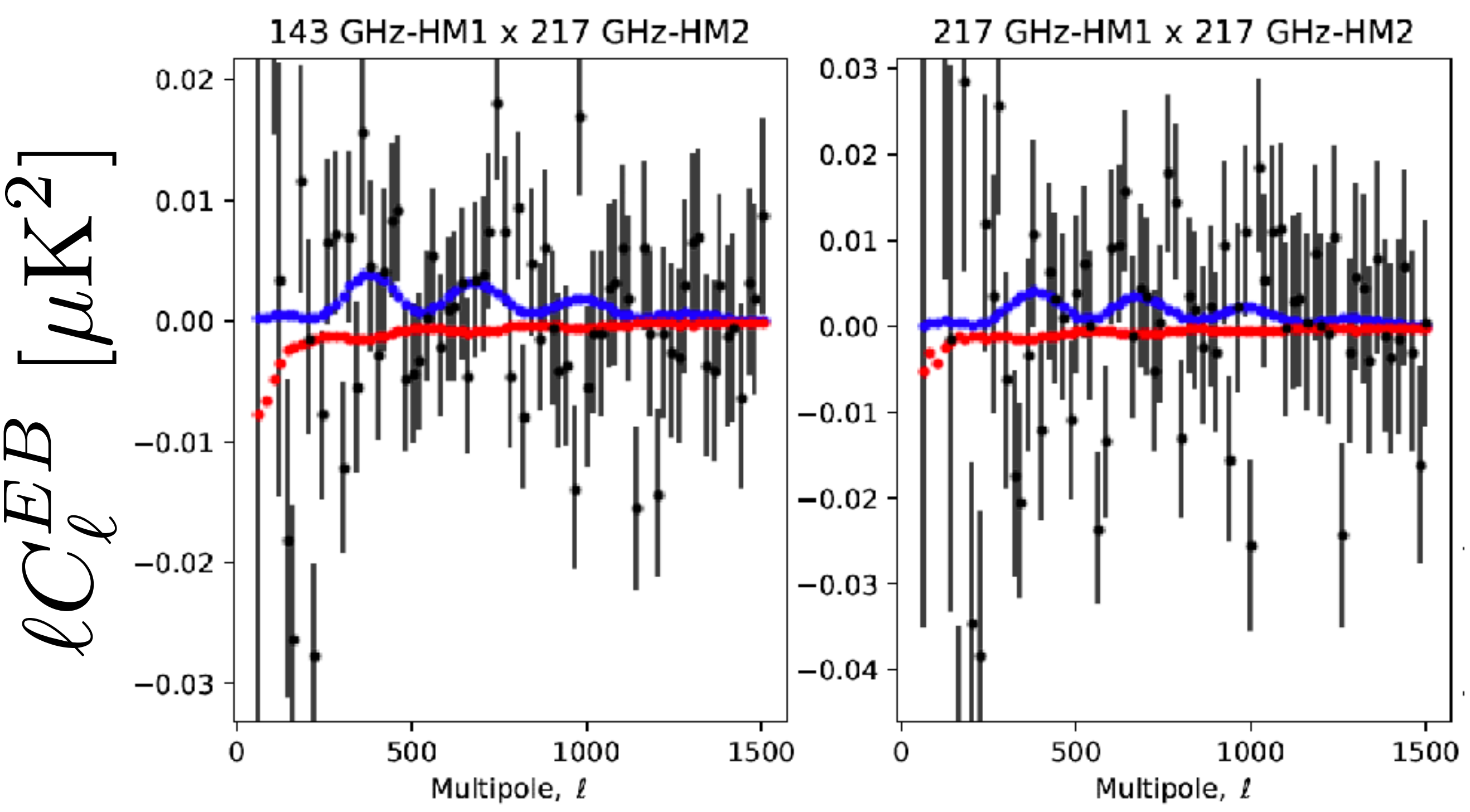
$$\langle C_\ell^{EB,o} \rangle = \frac{\tan(4\alpha)}{2} \left( \langle C_\ell^{EE,o} \rangle - \langle C_\ell^{BB,o} \rangle \right) + \frac{\sin(4\beta)}{2 \cos(4\alpha)} \left( \langle C_\ell^{EE,CMB} \rangle - \langle C_\ell^{BB,CMB} \rangle \right)$$

- Can we see  $\beta$  by eyes?
- First, take a look at the observed EE–BB spectra.
- **Red: Total**
- **Blue: The best-fitting CMB model**
- *The difference is due to the FG (and maybe unknown systematics)*



$$\langle C_\ell^{EB,o} \rangle = \frac{\tan(4\alpha)}{2} (\langle C_\ell^{EE,o} \rangle - \langle C_\ell^{BB,o} \rangle) + \frac{\sin(4\beta)}{2 \cos(4\alpha)} (\langle C_\ell^{EE,CMB} \rangle - \langle C_\ell^{BB,CMB} \rangle)$$

- Can we see  $\beta$  by eyes?
- Red: The signal attributed to the miscalibration angle,  $\alpha_v$
- Blue: The signal attributed to the cosmic birefringence,  $\beta$
- Red + Blue is the best-fitting model for explaining the data points



Angles	Results (deg)
$\beta$	$0.35 \pm 0.14$
$\alpha_{100}$	$-0.28 \pm 0.13$
$\alpha_{143}$	$0.07 \pm 0.12$
$\alpha_{217}$	$-0.07 \pm 0.11$
$\alpha_{353}$	$-0.09 \pm 0.11$

# Assumption for the baseline result

What about the intrinsic EB correlation of the foreground emission?

$$\langle C_\ell^{EB,o} \rangle = \frac{\tan(4\alpha)}{2} \left( \langle C_\ell^{EE,o} \rangle - \langle C_\ell^{BB,o} \rangle \right) + \frac{\sin(4\beta)}{2 \cos(4\alpha)} \left( \langle C_\ell^{EE,CMB} \rangle - \langle C_\ell^{BB,CMB} \rangle \right) + \frac{1}{\cos(4\alpha)} \langle C_\ell^{EB,fg} \rangle + \frac{\cos(4\beta)}{\cos(4\alpha)} \langle C_\ell^{EB,CMB} \rangle.$$

- For the baseline result, we ignore the intrinsic EB correlation of the CMB,  $\langle C_\ell^{EB,CMB} \rangle$  but we take into account the foreground (dust) EB,  $\langle C_\ell^{EB,fg} \rangle$
- We account for the dust EB by assuming that EB/EE is proportional to TB/TE **measured from the data**. Not really a modelling.



# Relating EB to TB

- A generic approach:

$$\frac{C_{\ell}^{EB, \text{dust}}}{C_{\ell}^{EE, \text{dust}}} \propto \frac{C_{\ell}^{TB, \text{dust}}}{C_{\ell}^{TE, \text{dust}}}$$

This is unknown

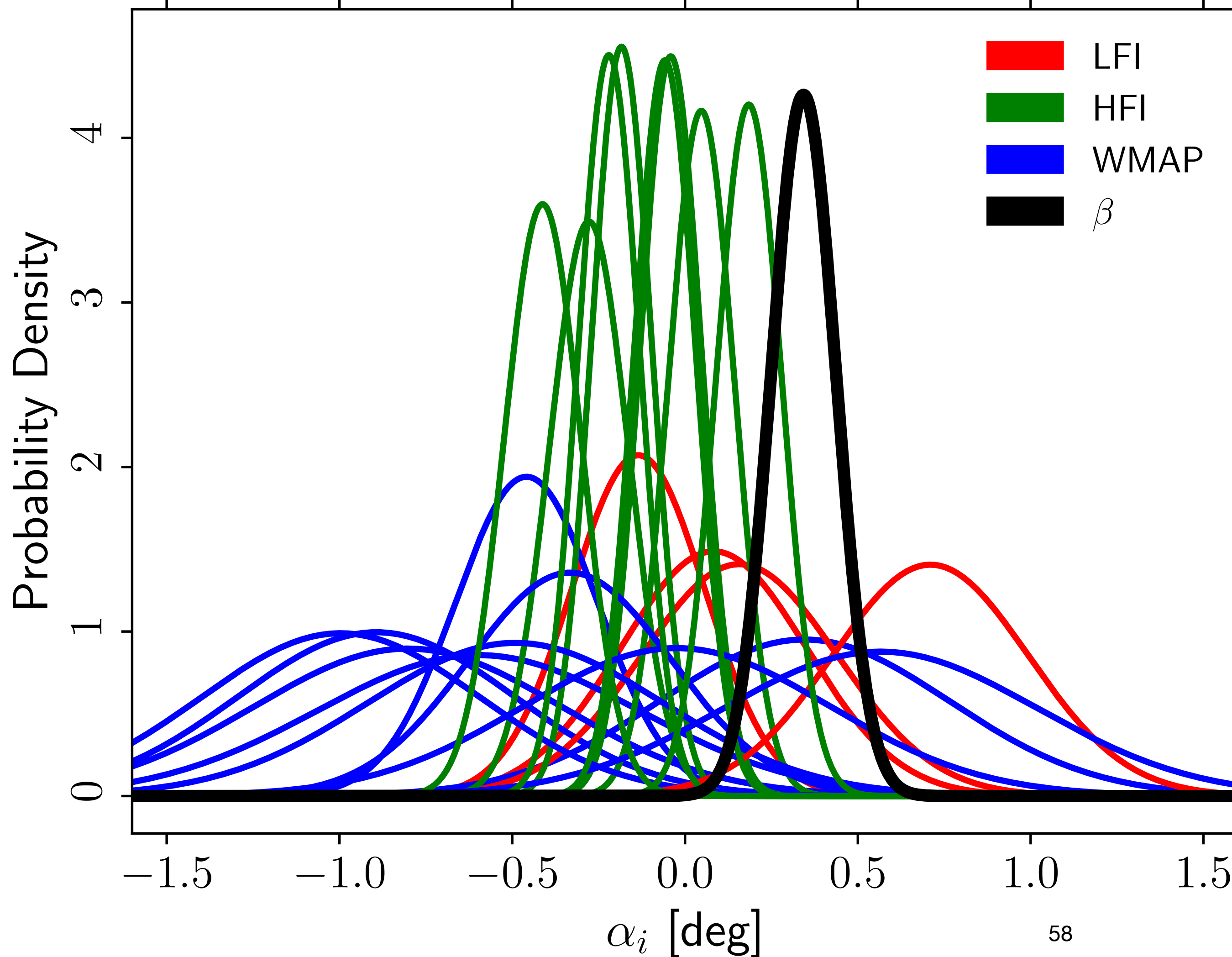
Measured well!

Measured well!

Measured well!

# Miscalibration angles (WMAP and Planck)

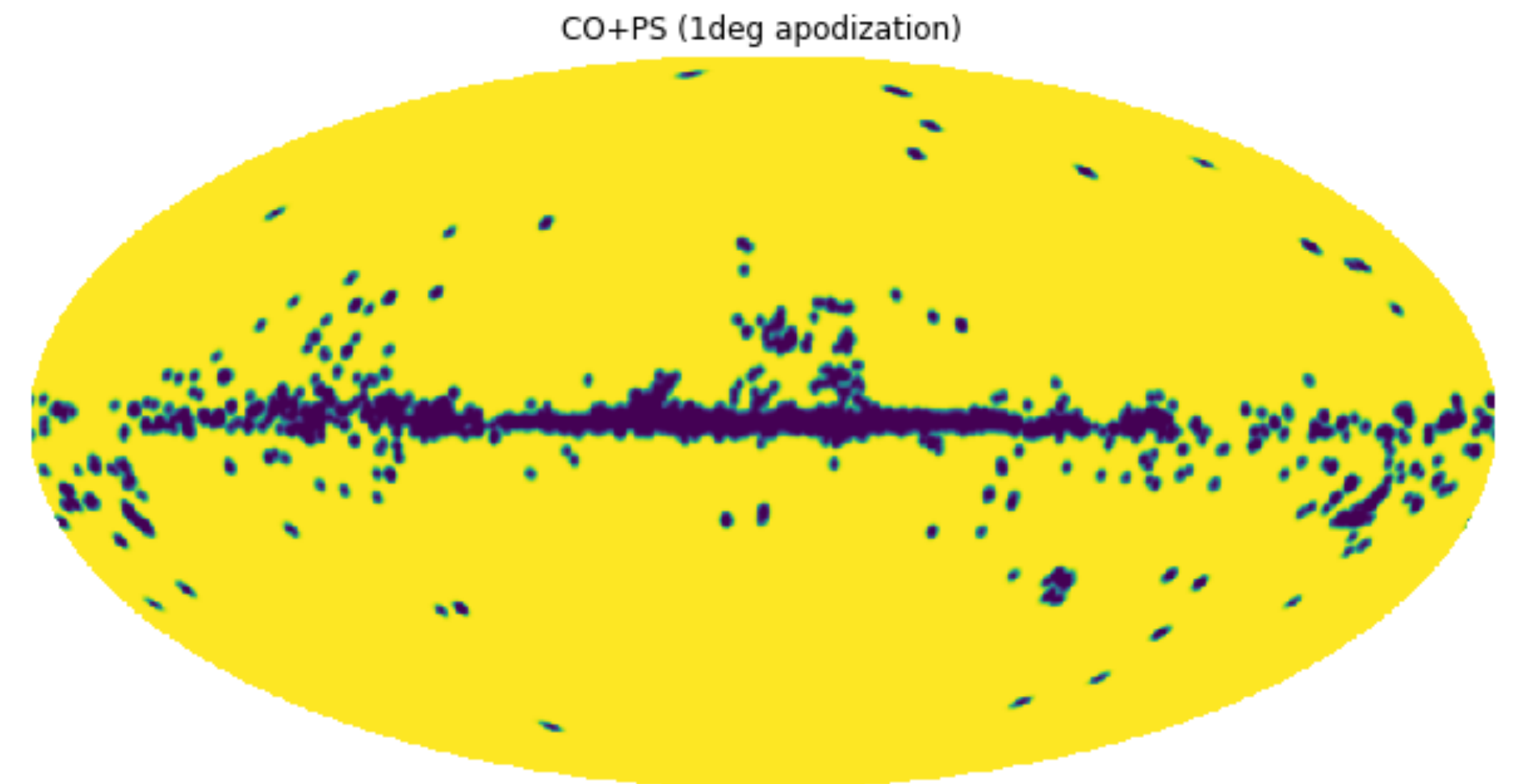
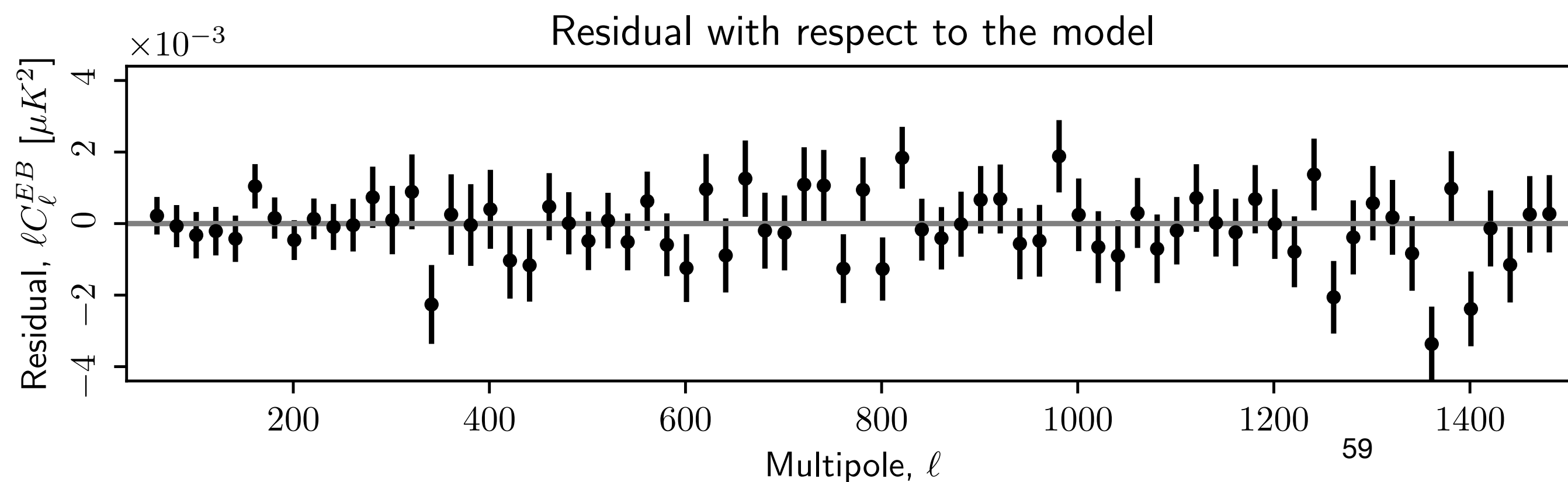
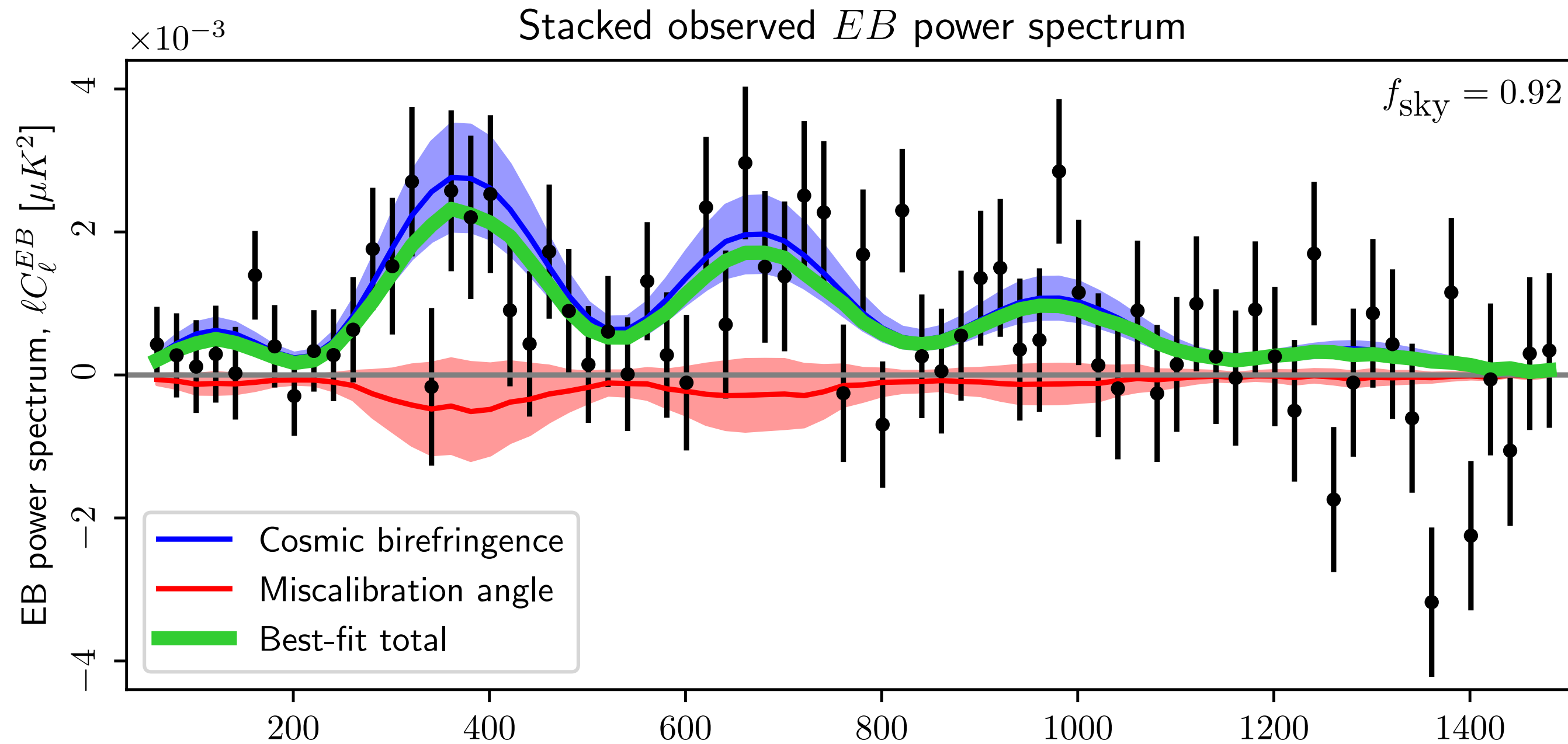
Nearly full-sky data (92% of the sky)



- The angles are all over the place, and are well within the quoted calibration uncertainty of instruments.
  - 1.5 deg for WMAP
  - 1 deg for Planck
- They cancel!
  - The power of adding independent datasets.

# Cosmic Birefringence fits well (WMAP+Planck)

## Nearly full-sky data (92% of the sky)



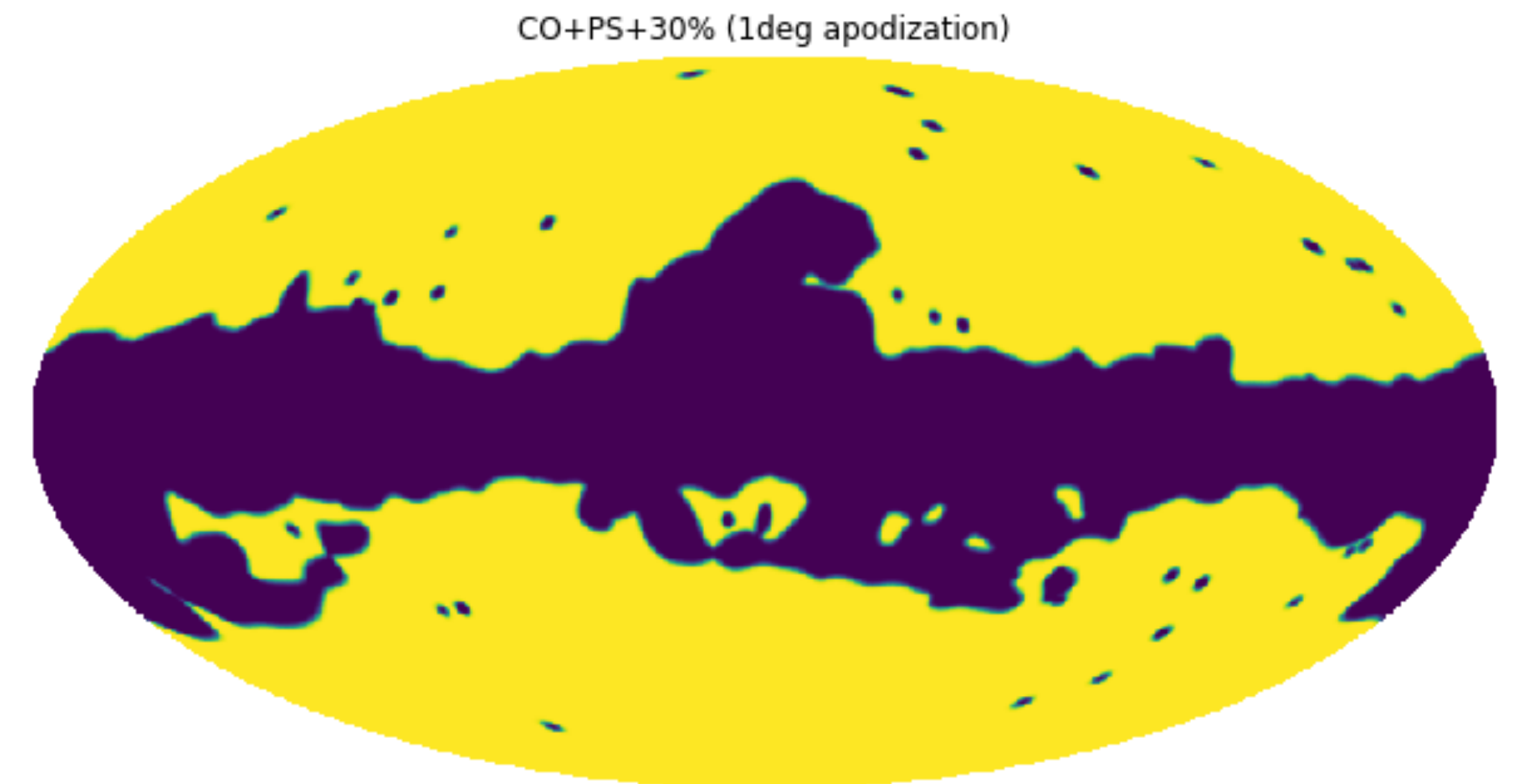
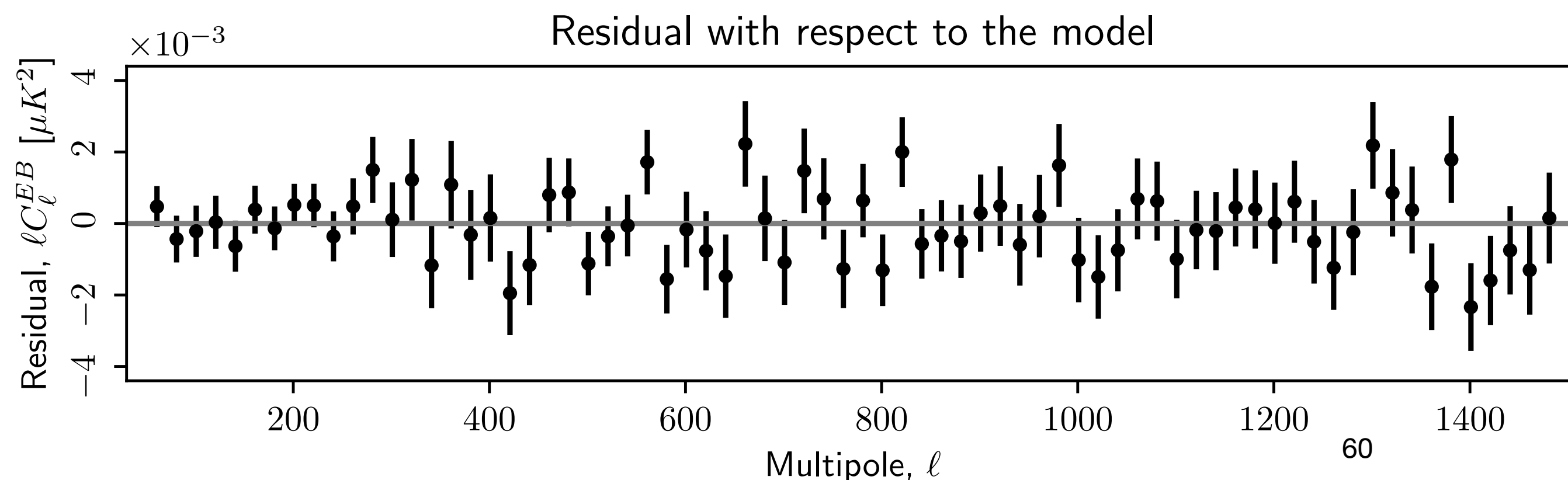
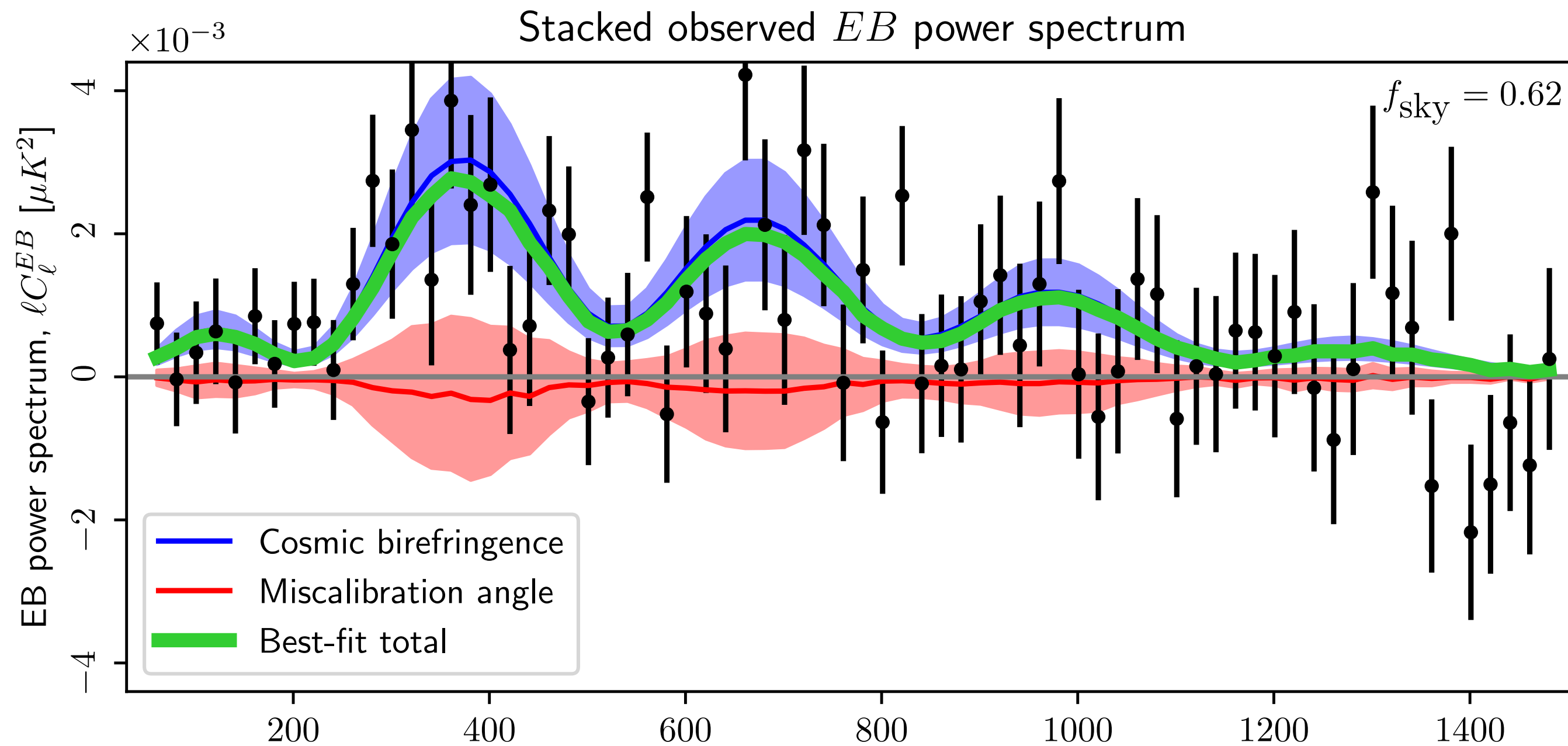
- Miscalibration angles** make only small contributions thanks to the cancellation.

- $\beta = 0.34 \pm 0.09$  deg

- $\chi^2 = 65.3$  for DOF=72

# Cosmic Birefringence fits well (WMAP+Planck)

## Robust against the Galactic mask (62% of the sky)



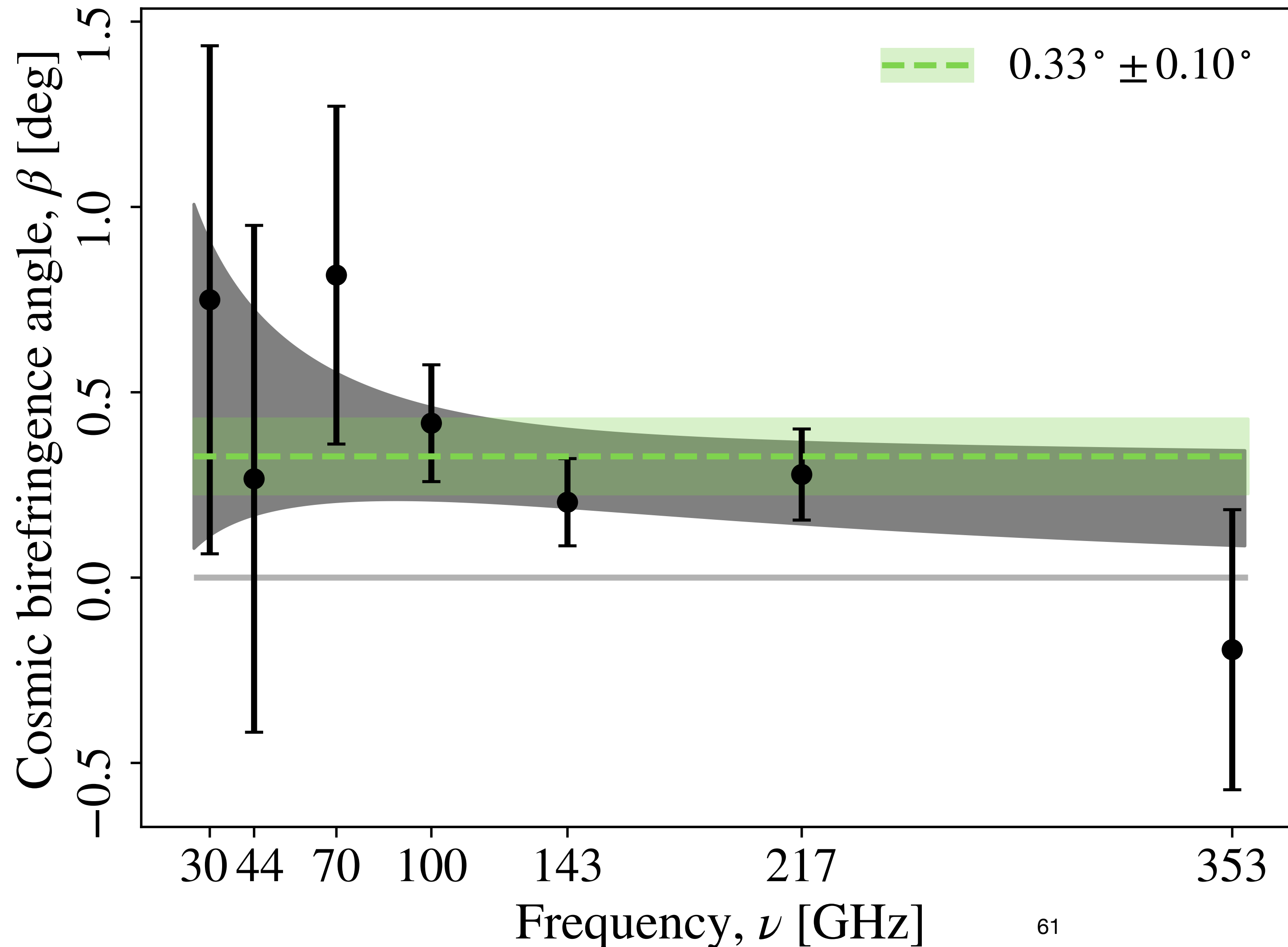
- **Miscalibration angles** make only small contributions thanks to the cancellation.

- $\beta = 0.37 \pm 0.14$  deg

- $\chi^2 = 65.8$  for DOF=72

# No frequency dependence is found

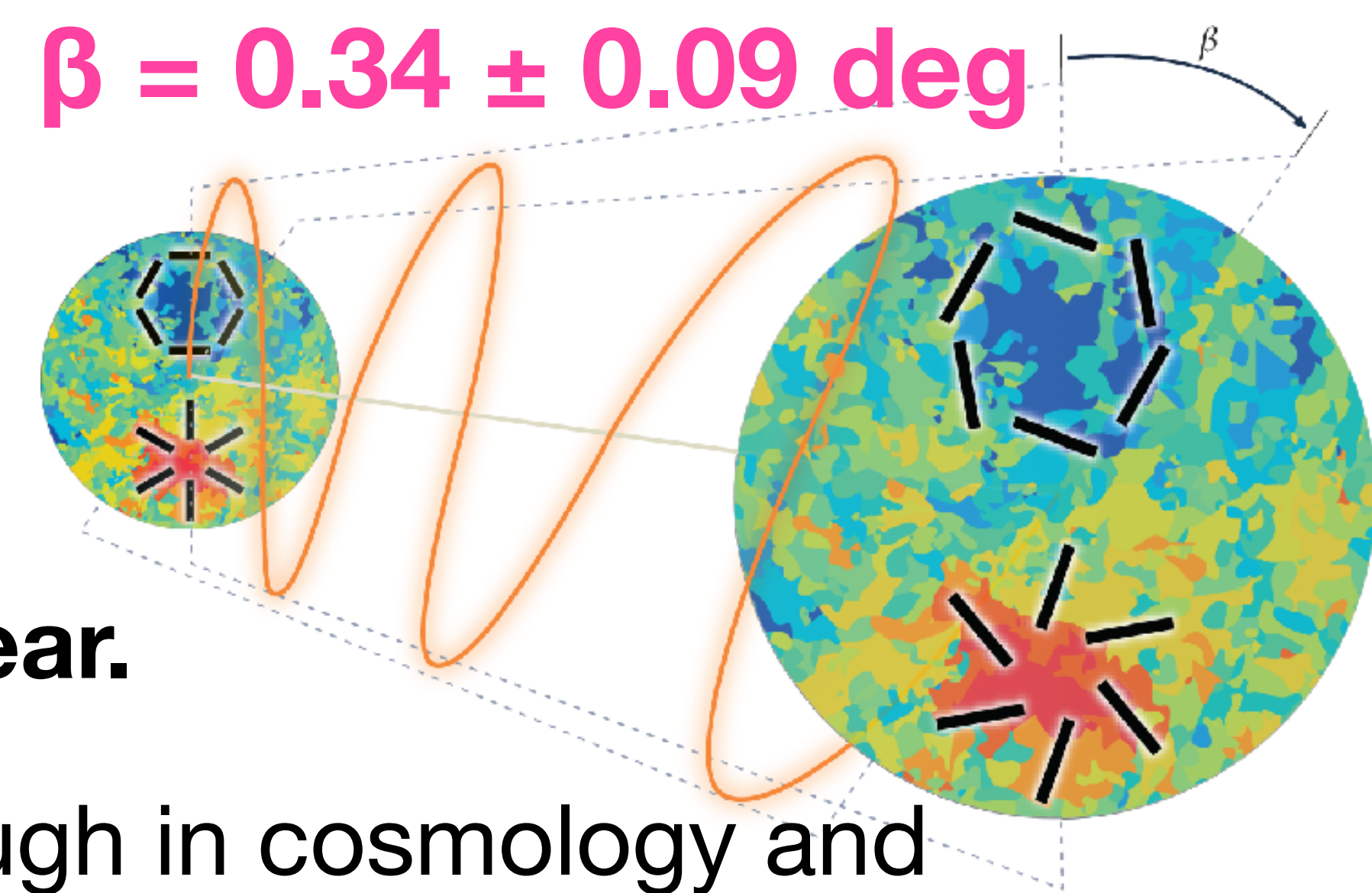
## Consistent with the expectation from cosmic birefringence



- No evidence for frequency dependence:
- For  $\beta \sim (\nu/150\text{GHz})^n$ ,  
 $n = -0.20^{+0.41}_{-0.39}$  (68% CL)
- Faraday rotation ( $n=-2$ ) is disfavoured.

# Conclusion

$\beta = 0.34 \pm 0.09$  deg (68%CL; nearly full sky)



- I am old enough to know that  **$3.6\sigma$  can still disappear.**
  - If confirmed in the future, it would be a breakthrough in cosmology and fundamental physics.
- The signal is robust against the sky fraction used for the analysis and has no frequency dependence.
- Good news: **The impact of the known instrumental systematics of Planck is negligible** (*Diego-Palazuelos et al., arXiv:2210.07655*).
- It is fair to say that **there is something in the Planck data. No evidence for significant impacts of the Galactic foreground or the known systematics.**
  - But we keep investigating!