

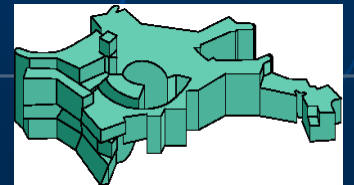
# Supernova Theory

*(and Cosmological Distances)*

*Wolfgang Hillebrandt  
MPI für Astrophysik  
Garching*



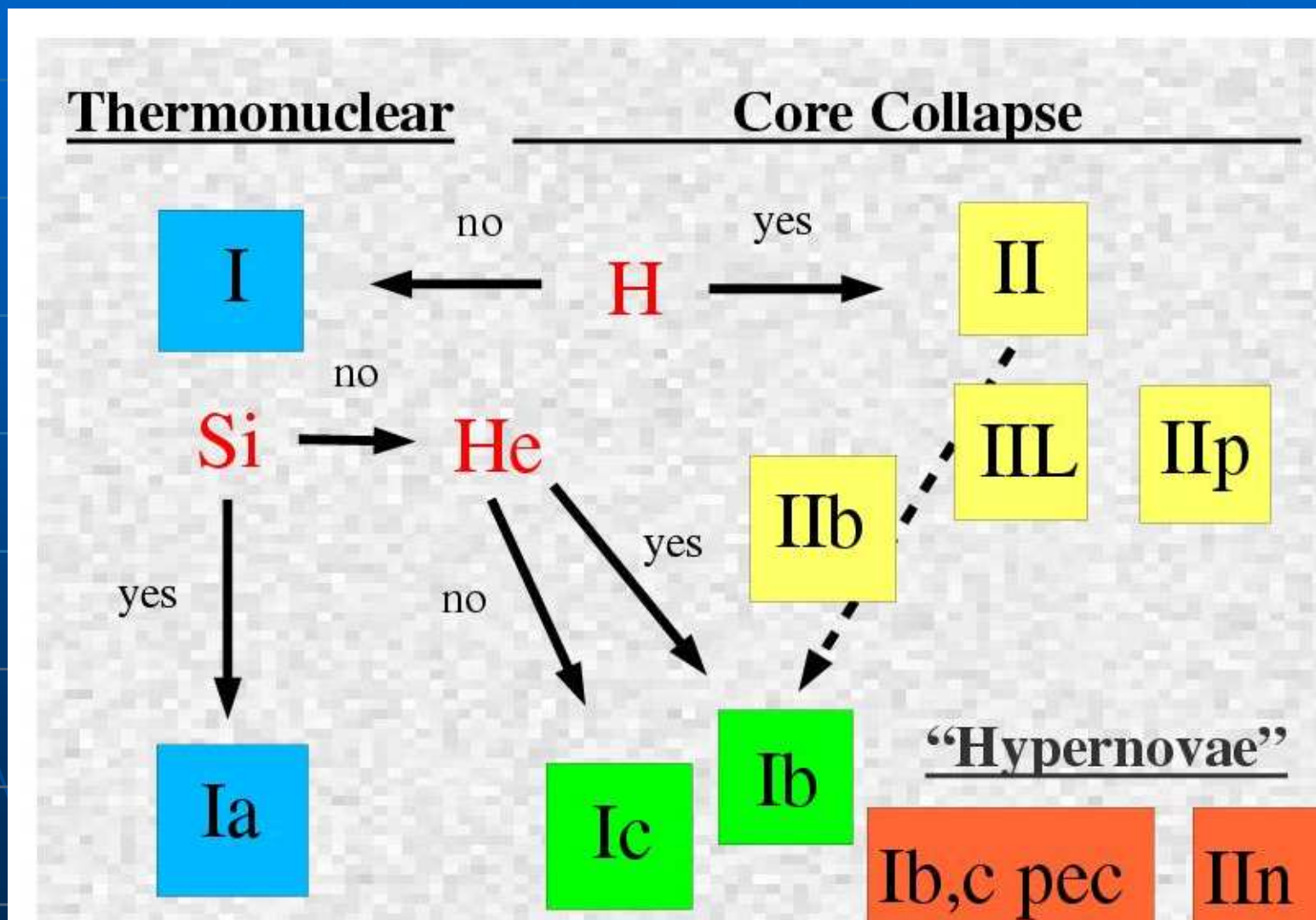
Scuola Nazionale di Astrofisica,  
Sant'Agata, May 8 – 13, 2005



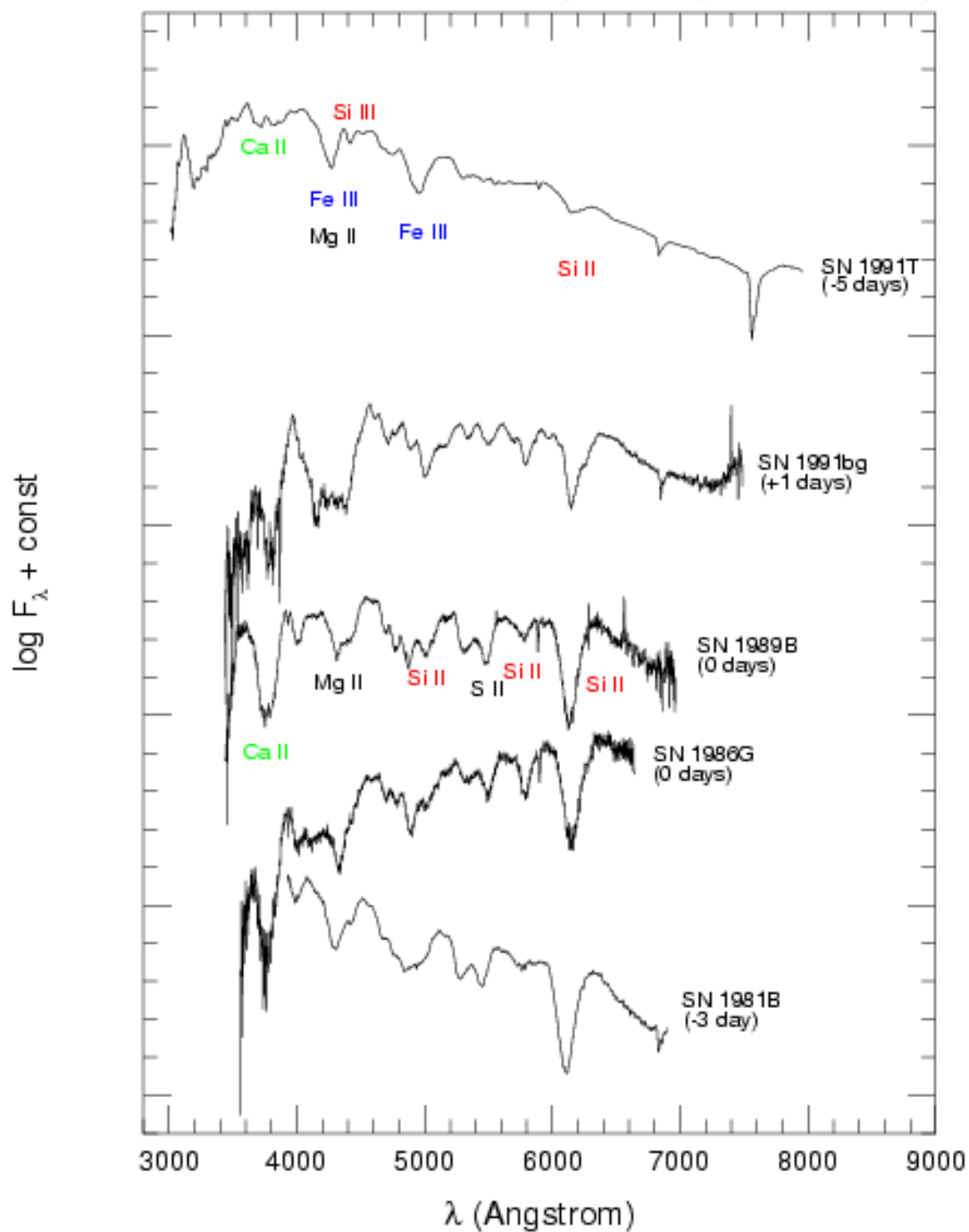
# Outline of the lectures

- n Supernova types and phenomenology
- n Models of core-collapse supernovae (Type II; Type Ib,c; GRB's)
- n Models of thermonuclear supernovae (Type Ia)
- n Luminosity distances and supernova cosmology

# Supernova classification



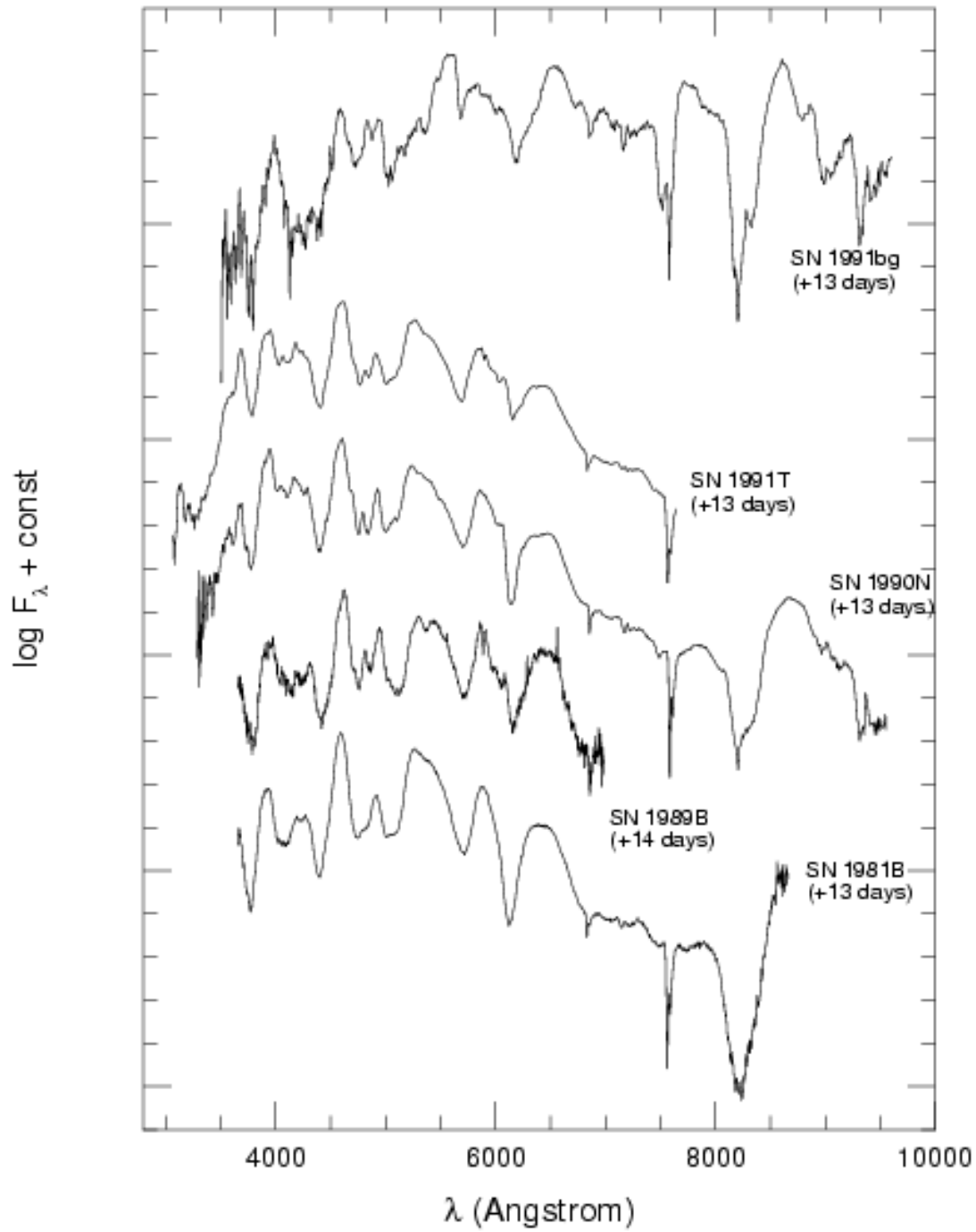
(Leibundgut et al. 1993)



# Supernova Spectroscopy

Type Ia

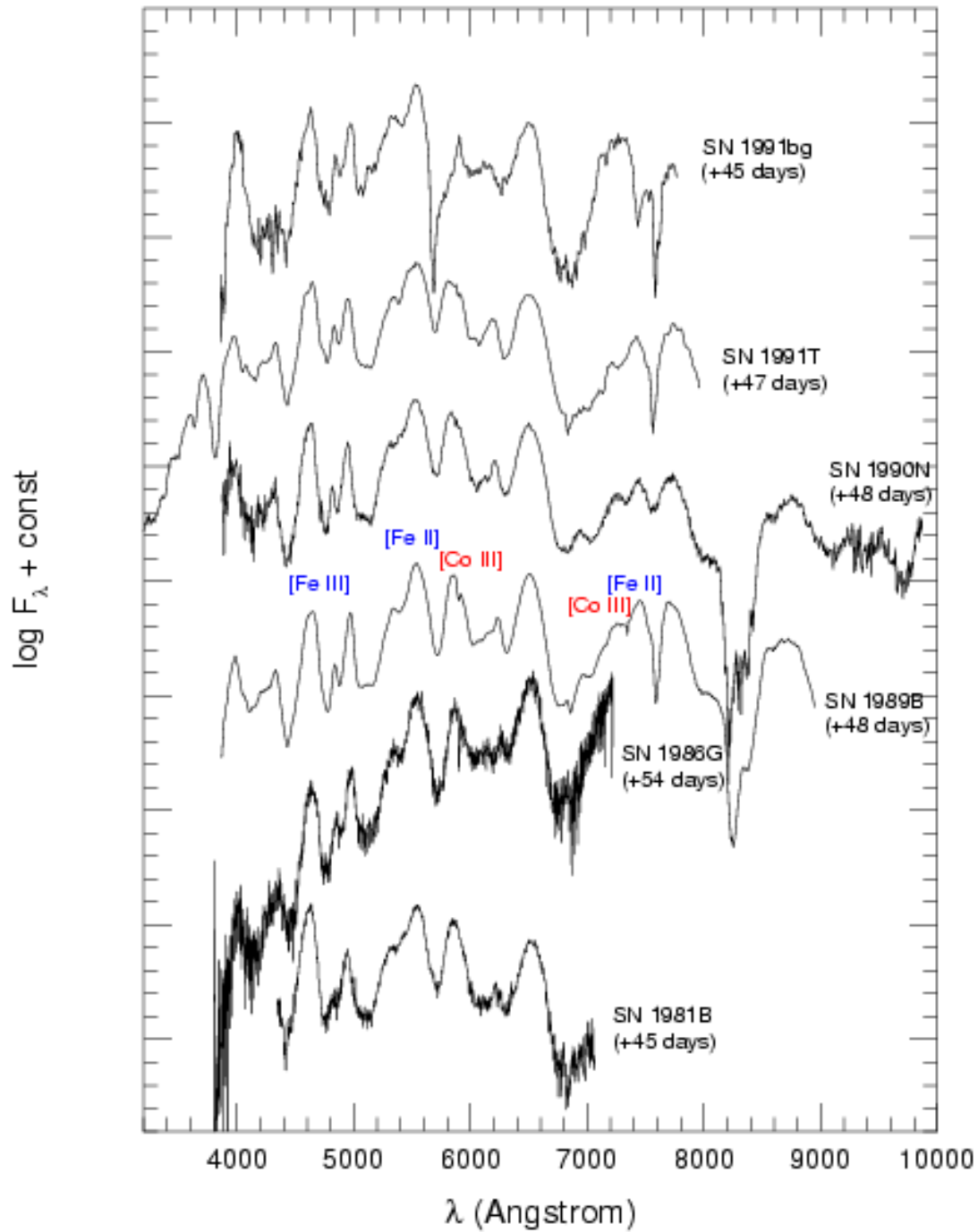
(Leibundgut et al. 1993)



# Supernova Spectroscopy

Type Ia

(Leibundgut et al. 1993)

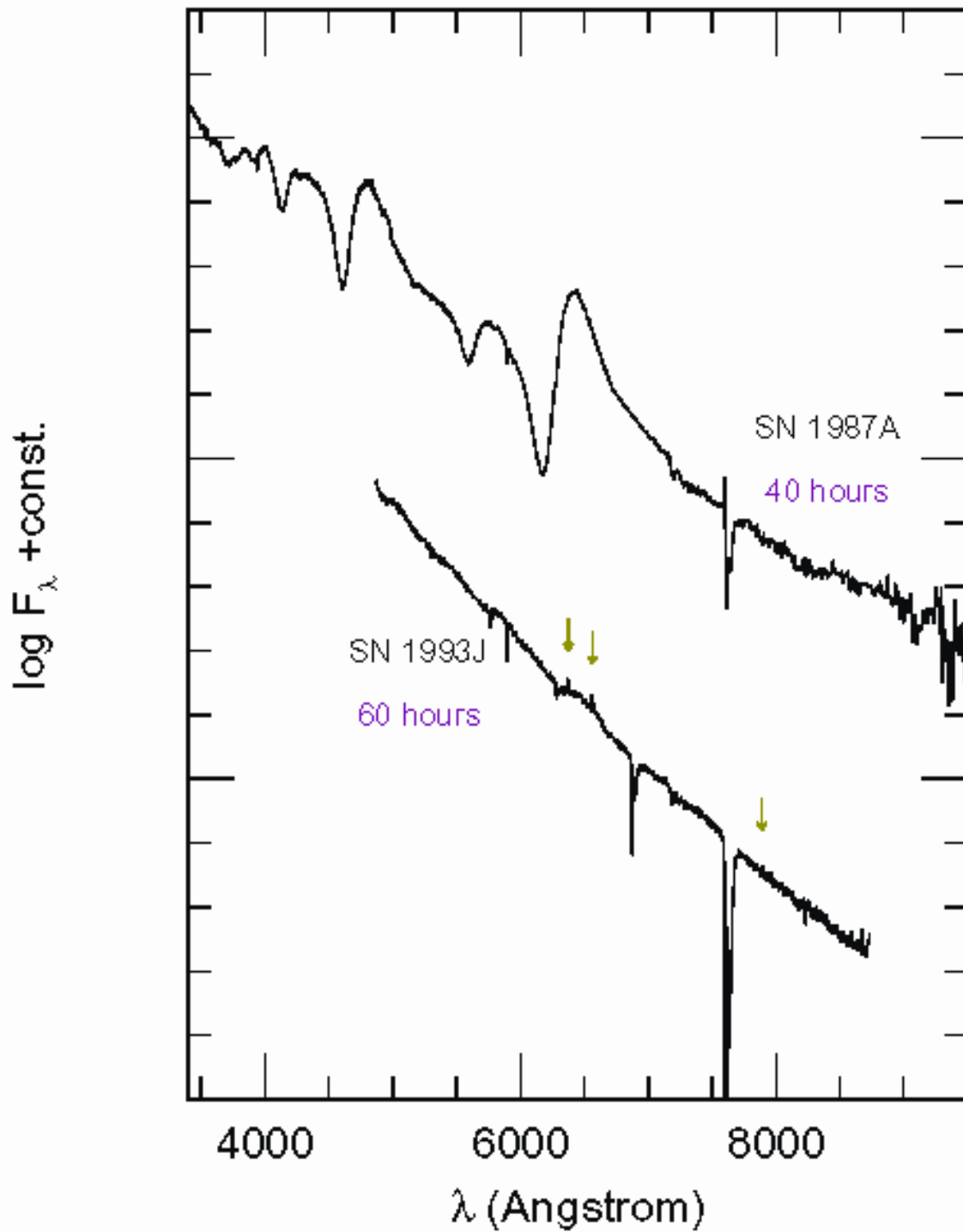


# Supernova Spectroscopy

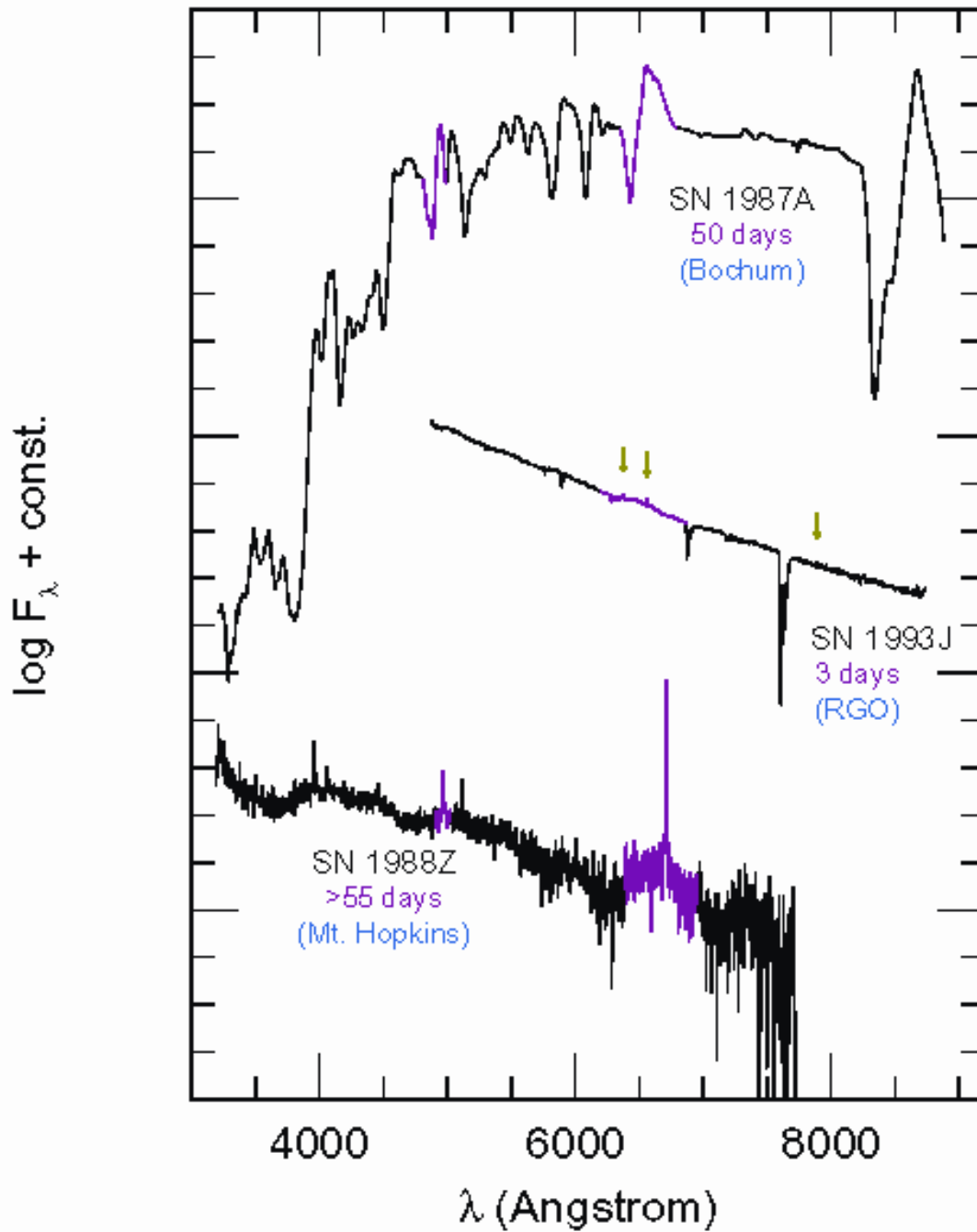
Type Ia

# Supernova Spectroscopy

Type II



## Type II Supernovae



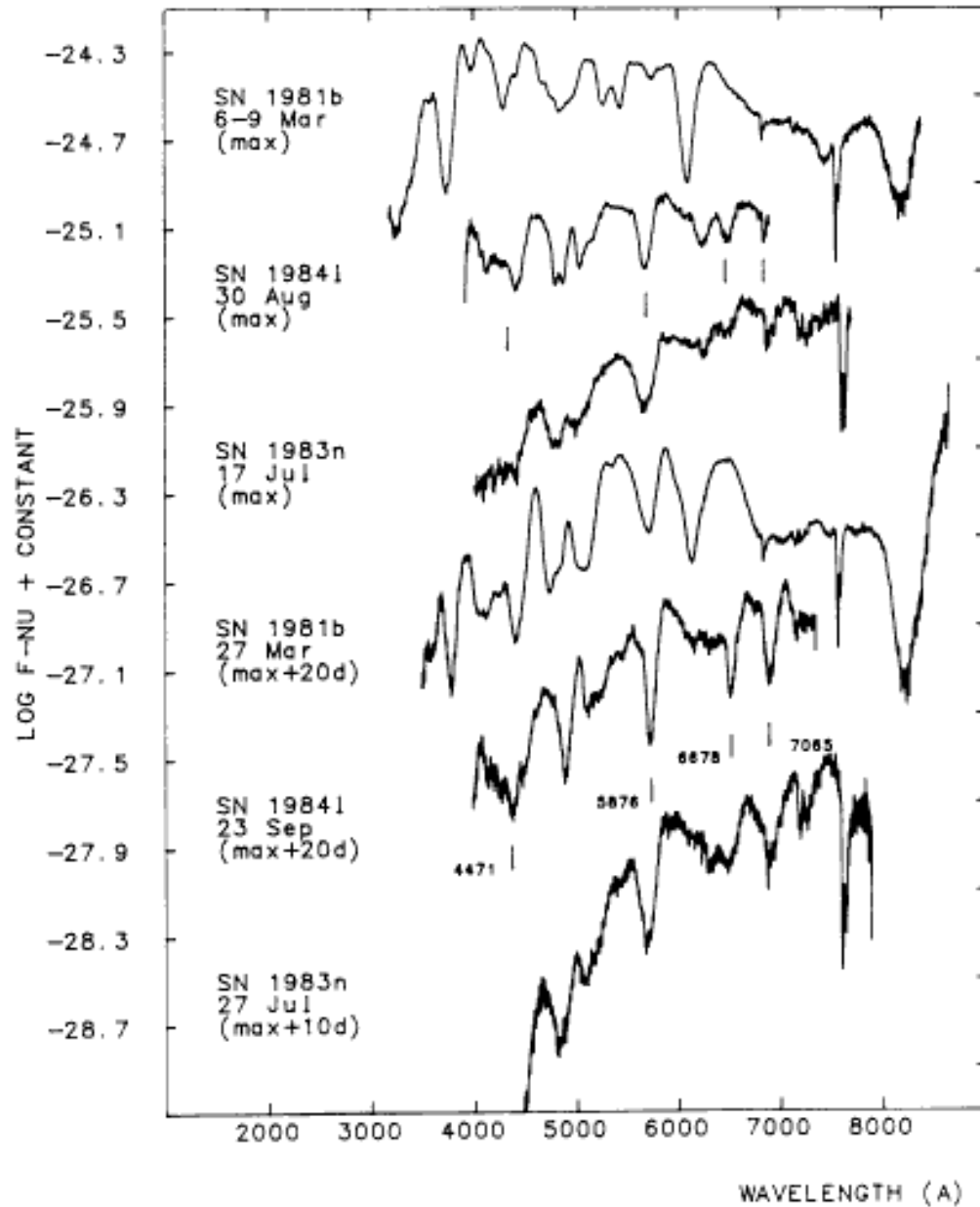
# Supernova Spectroscopy

Type II



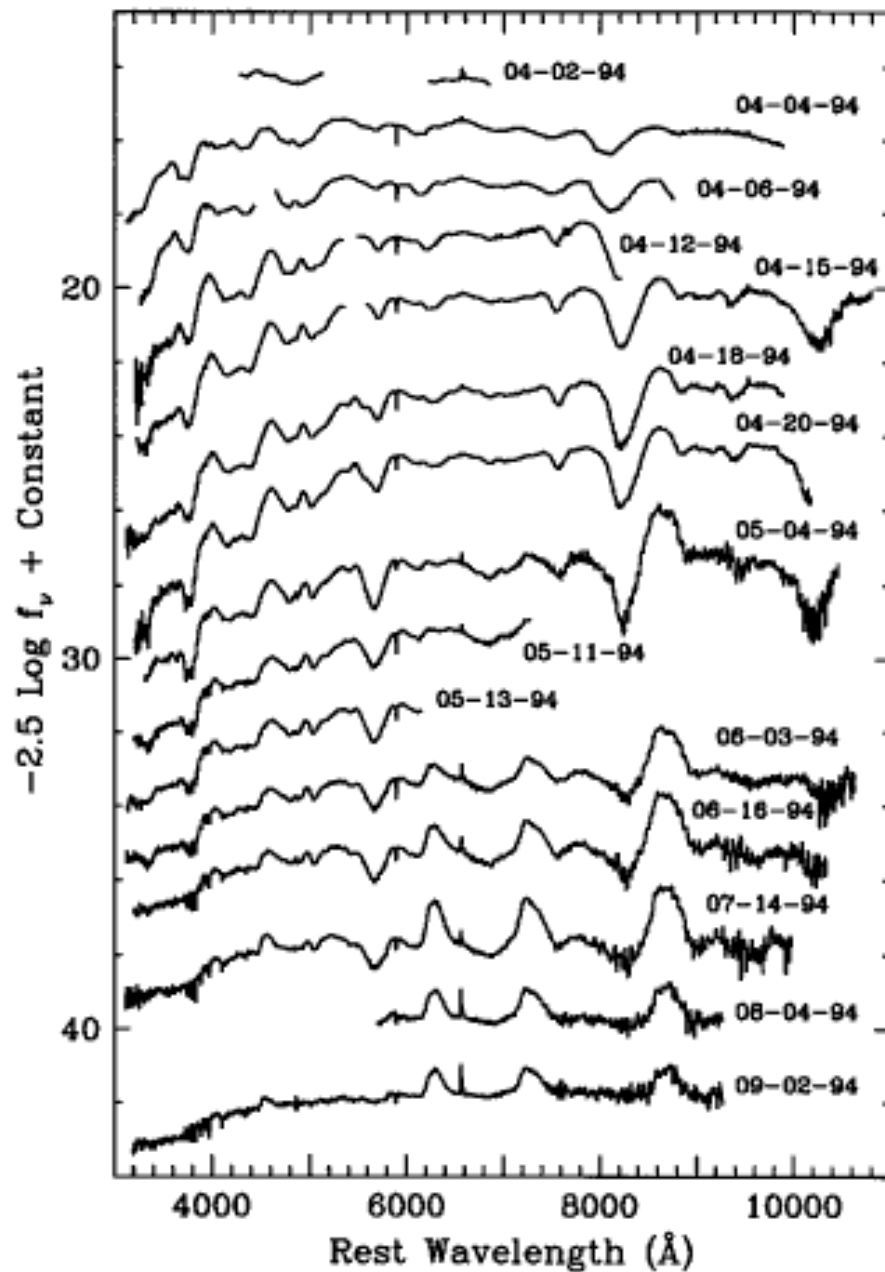
# Supernova Spectroscopy

Type Ib



# Supernova Spectroscopy

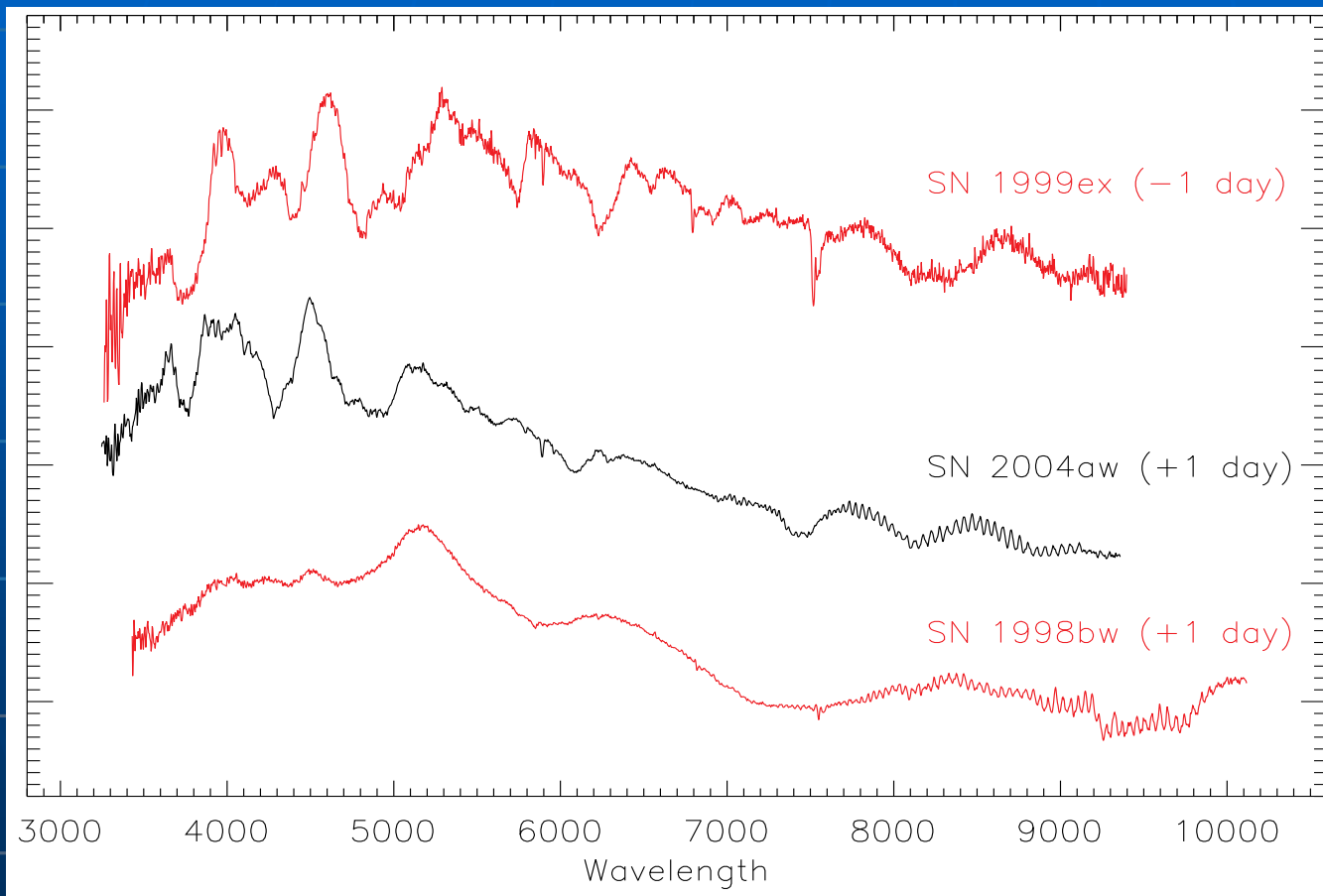
Type Ic



SN 1994I (Filippenko et al.)

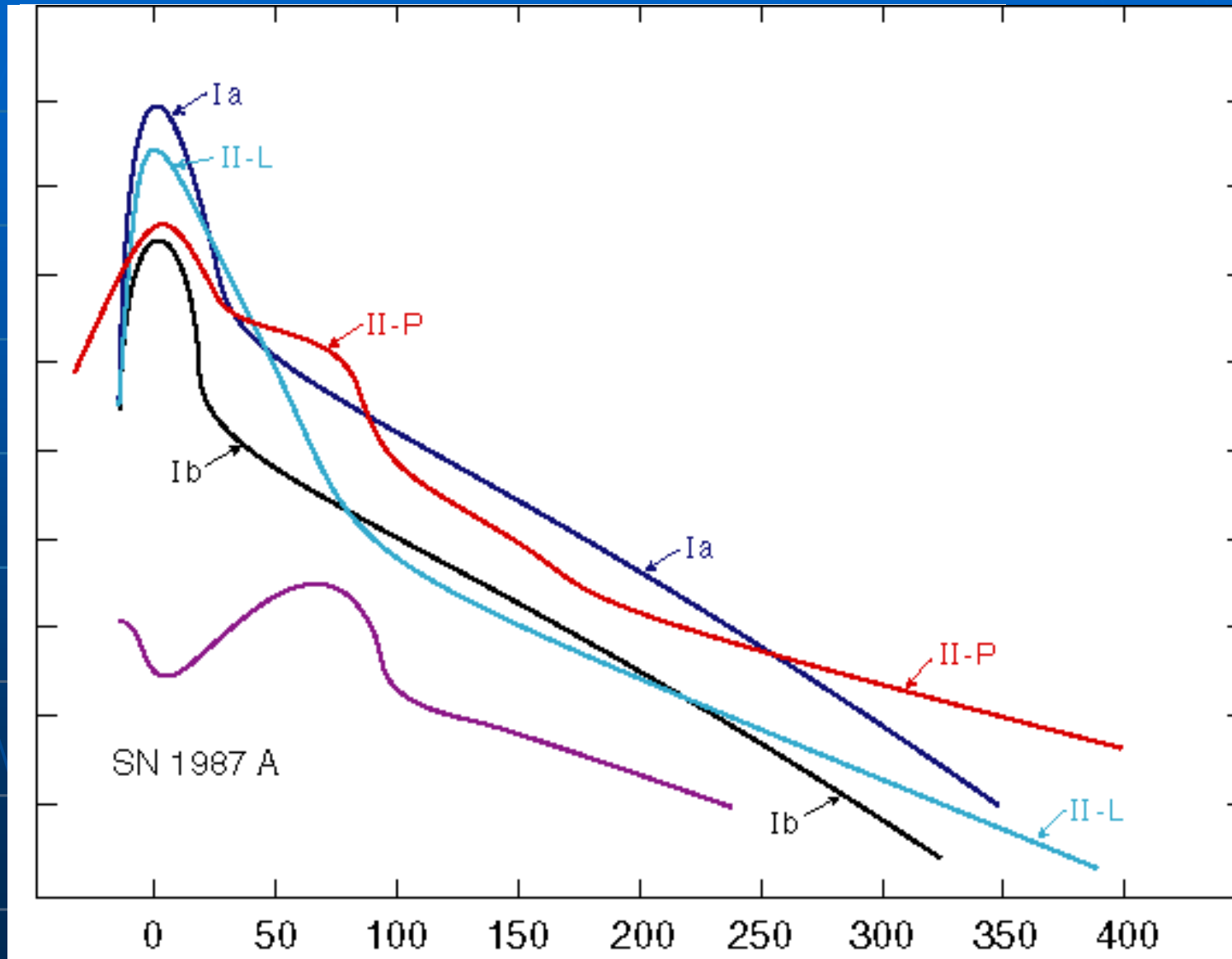
# Supernova Spectroscopy

Type Ic pec



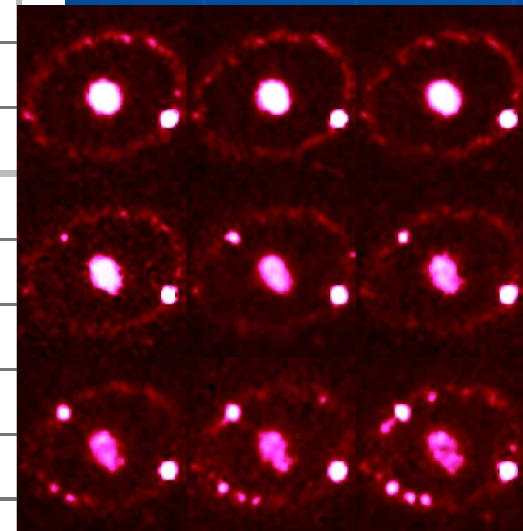
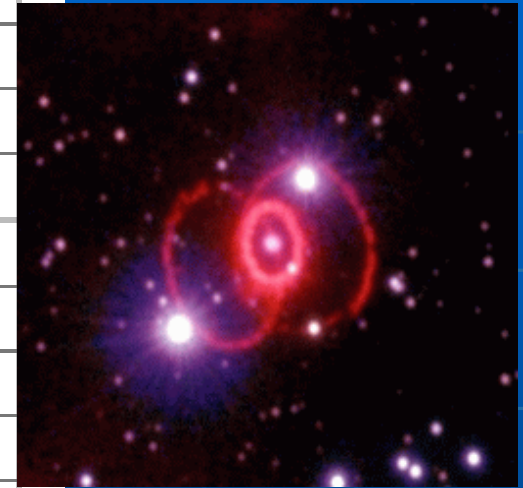
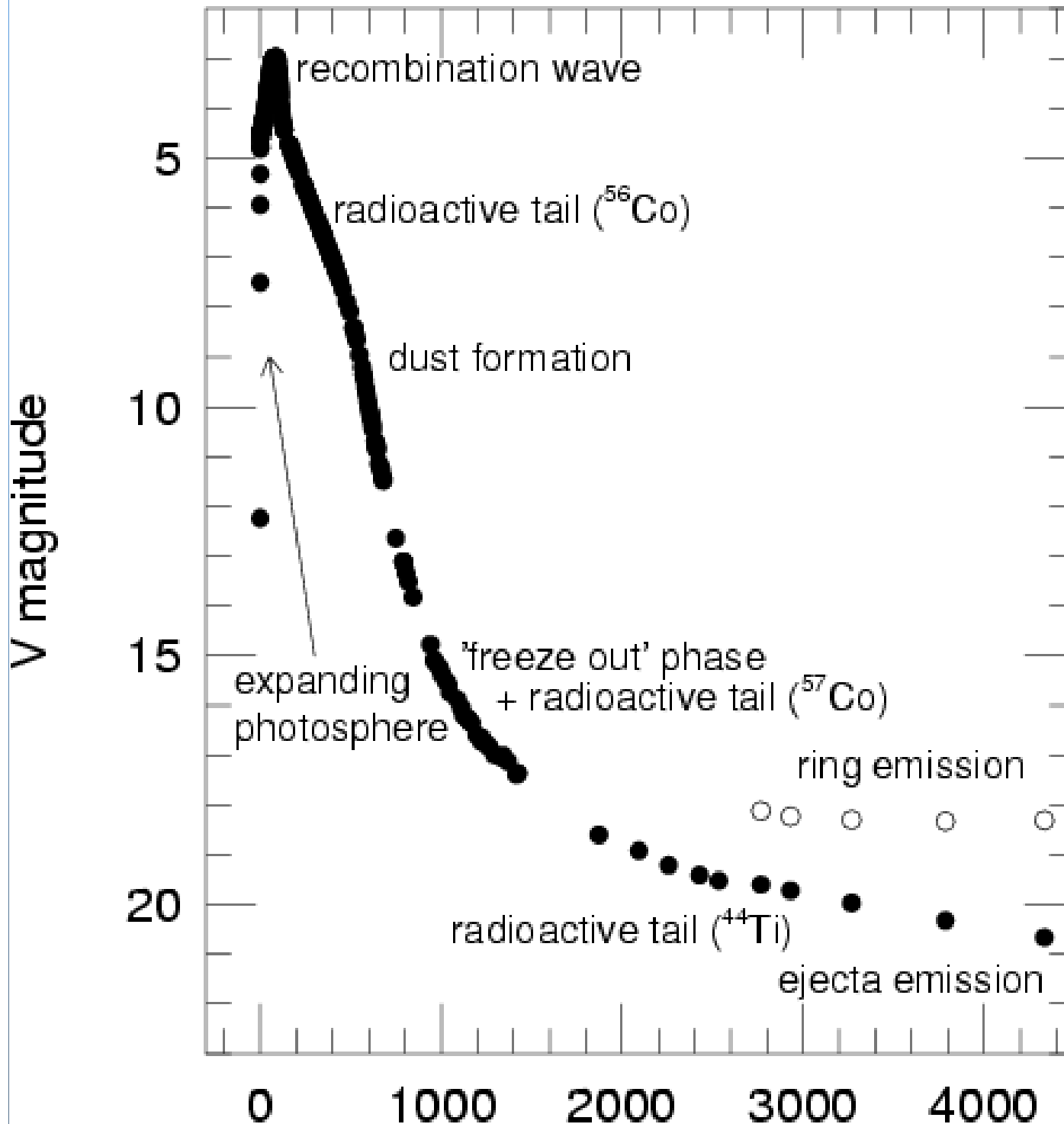
(Taubenberger et al. 2005)

# Supernova light curves



l. (2001)

# Core-collapse light curve



Suntzeff (2003)

# Energy sources for light curves

## <sup>n</sup> shock

- breakout
- kinetic energy

## <sup>n</sup> cooling

- due to expansion of the ejecta

## <sup>n</sup> radioactivity

- nucleosynthesis

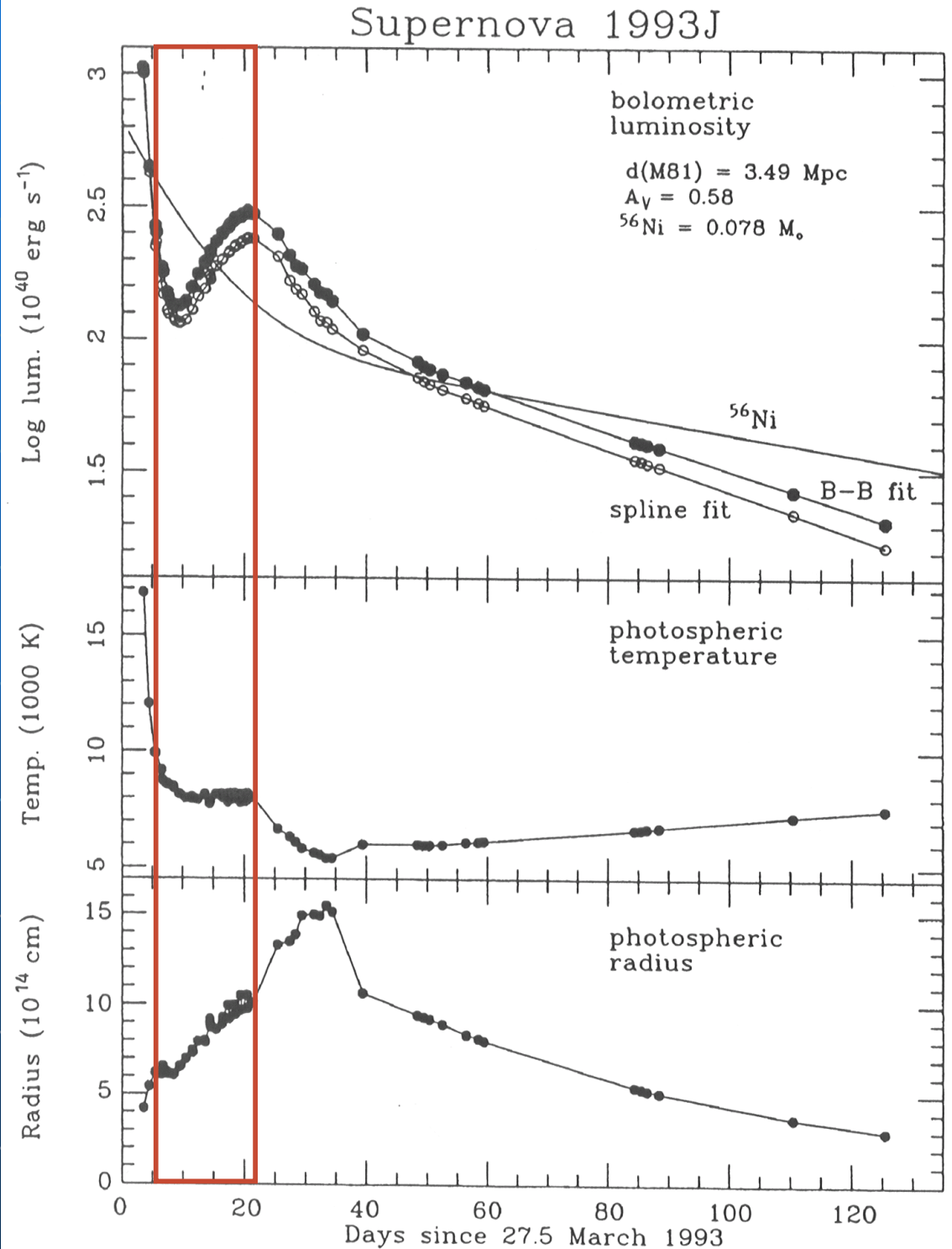
## <sup>n</sup> recombination

- of the shock-ionised material

# Expansion

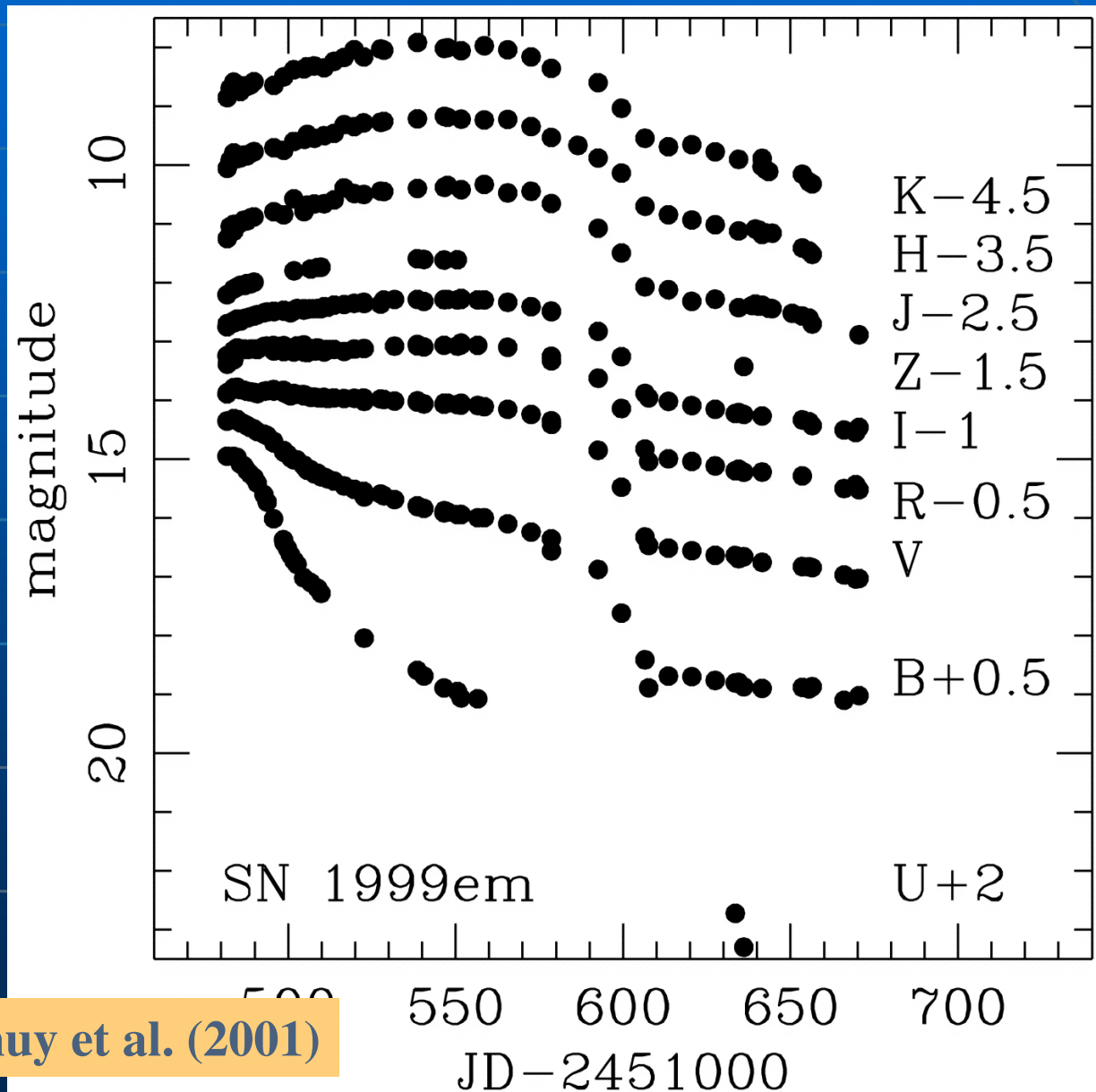
## n Brightness increase

- increased surface area
- slow temperature decrease



# Recombination

- n Balance of the recombination wave and the expansion of the ejecta
  - leads to an extended plateau phase



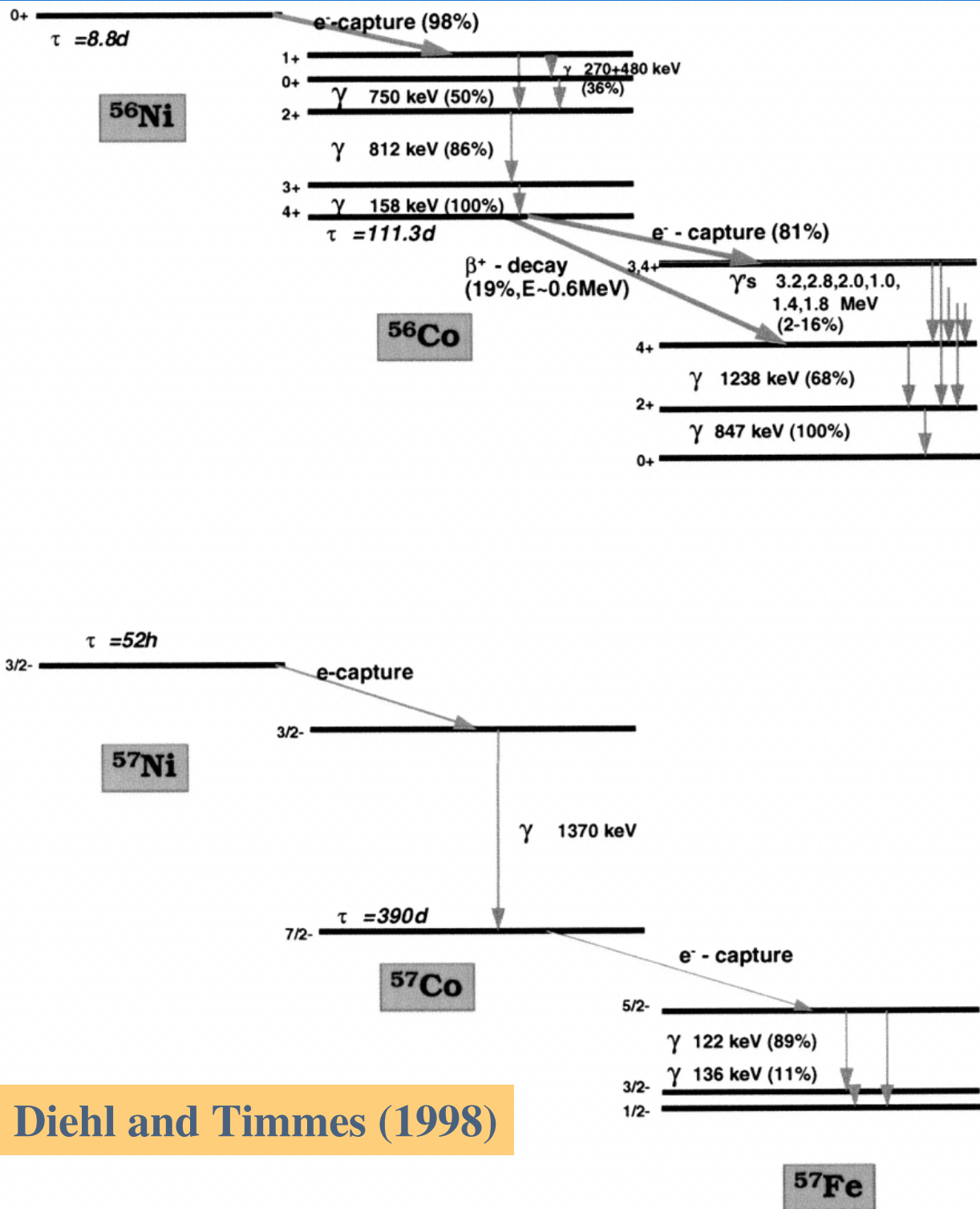
Hamuy et al. (2001)



# Radioactivity

n Isotopes of Ni and other elements

- conversion of  $\gamma$ -rays and positrons into heat and optical photons

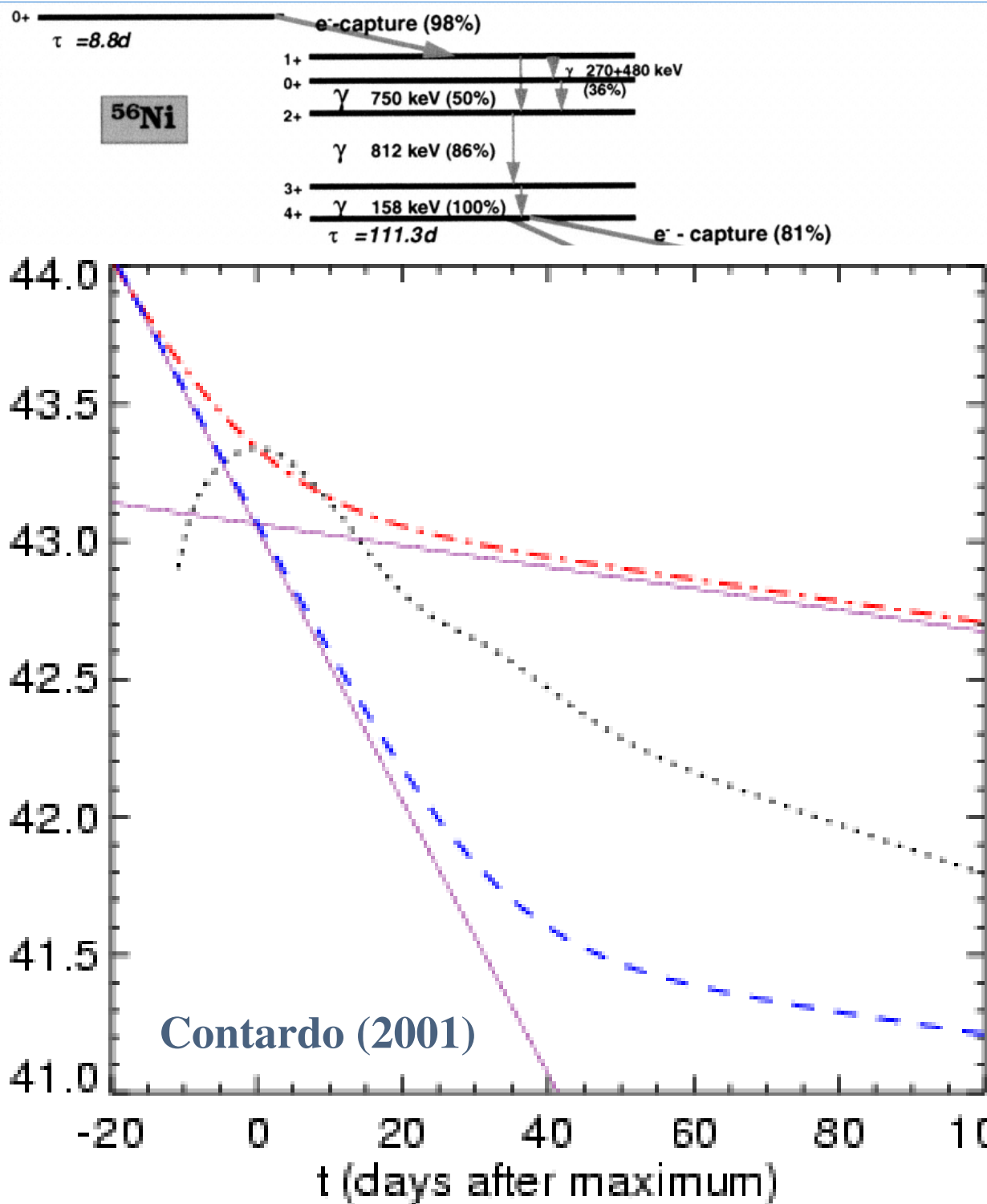


Diehl and Timmes (1998)

# Radioactivity

n Isotopes of Ni and other elements

- conversion of  $\gamma$ -rays and positrons into heat and optical photons



# Supernova types: Summary

## n Thermonuclear SNe

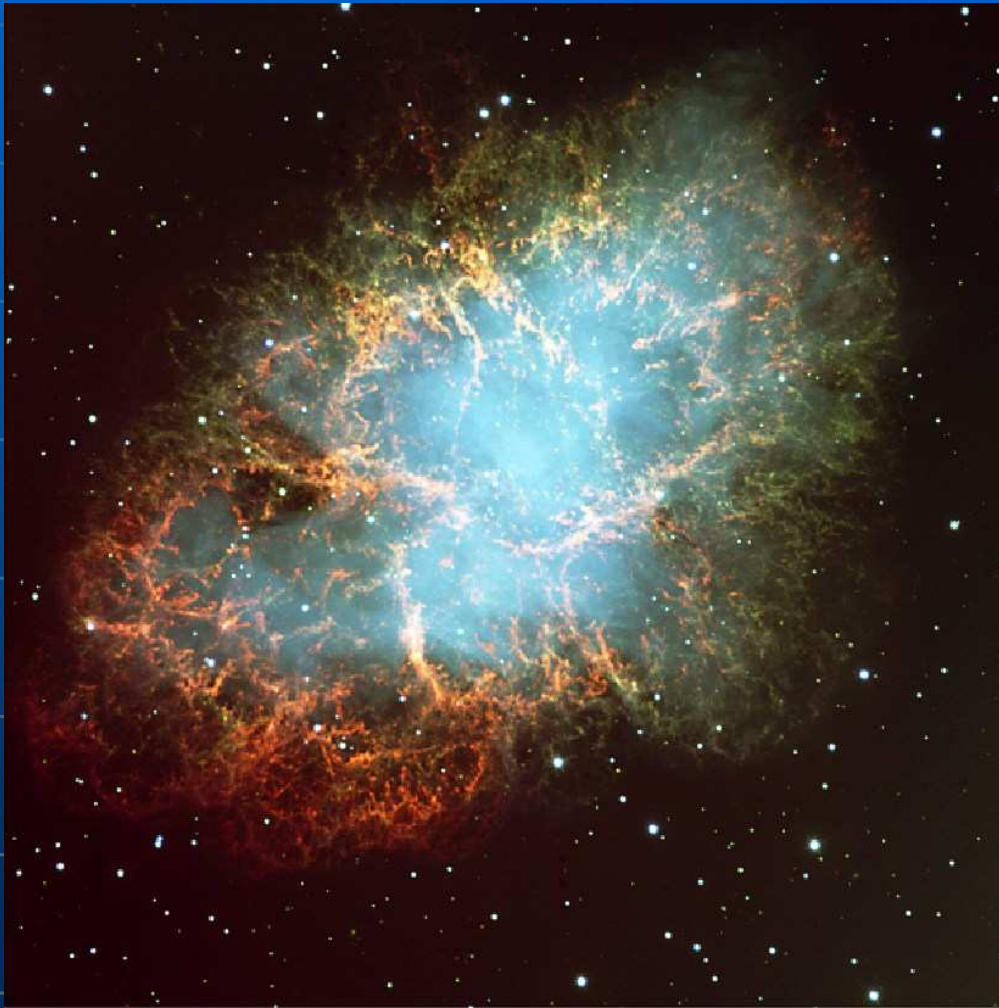
- from low-mass stars ( $<8M_{\odot}$ )
- highly evolved stars (white dwarfs)
- explosive C and O burning
- binary systems required
- complete disruption

## n Core-collapse SNe

- high mass stars ( $>8M_{\odot}$ )
- large envelopes (still burning)
- burning due to compression
- single stars (binaries for SNe Ib/c?)
- neutron star

# Core-collapse Supernovae

(In part “borrowed” from a lecture by Ewald Müller)



## Prototype:

Crab nebula with pulsar  
(constellation Orion)

Remnant of a supernova  
observed in 1054

# 30 Doradus region in the Large Magellanic Cloud

(d ~ 160 000 light years)



© Anglo-Australian Observatory

**Supernova 1987A**  
7:35 UT 23.2.1987

**Blue Supergiant**  
**Sanduleak 69.202**

# A few observational facts

(core collapse supernovae, i.e. SNe II, Ib, Ic)

very bright events:

$$L \sim 10^{10} L_{\text{sun}}$$

fast expanding ejecta:

$$v \sim 10^4 \text{ km/s}$$

energies: electromagnetic:

$$\sim 10^{49} \text{ erg}$$

kinetic:

$$\sim 10^{51} \text{ erg}$$

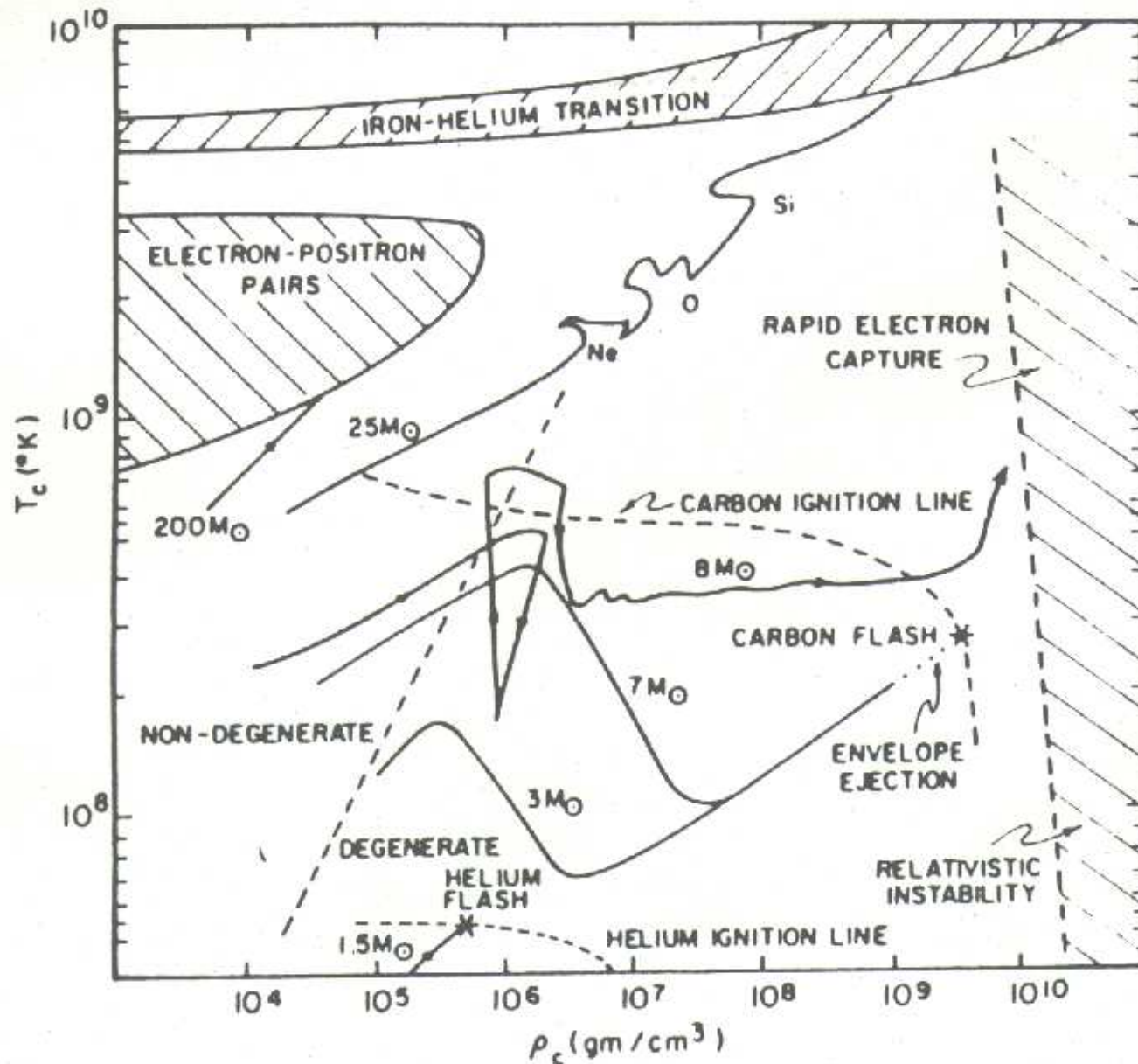
neutrinos (SN1987A):

$$\sim 3 \cdot 10^{53} \text{ erg}$$

progenitor star destroyed (SN 1987A, SN 1993J)

compact remnant (as far as we know)

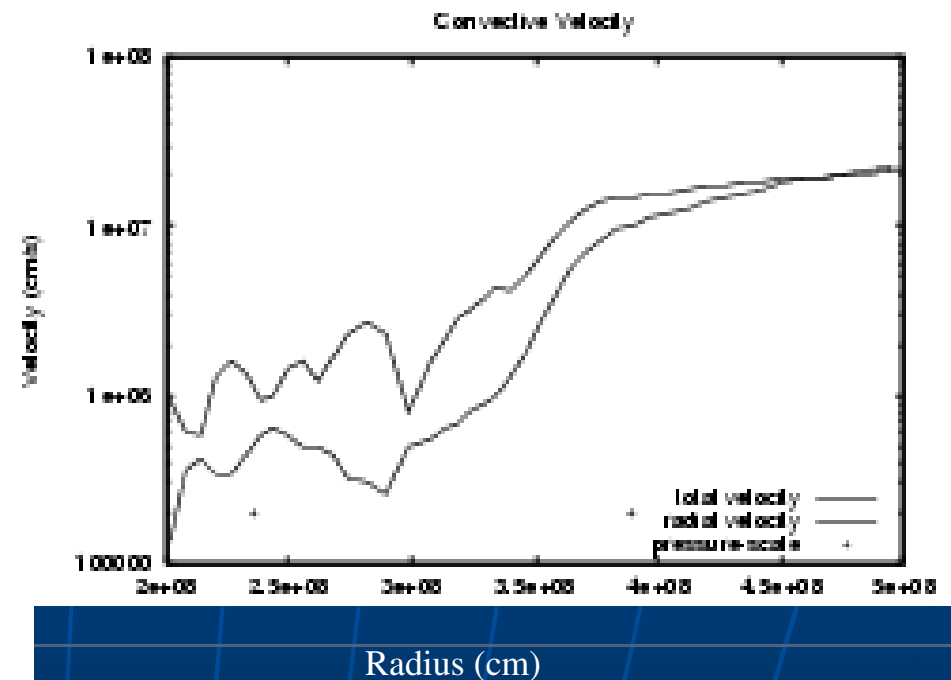
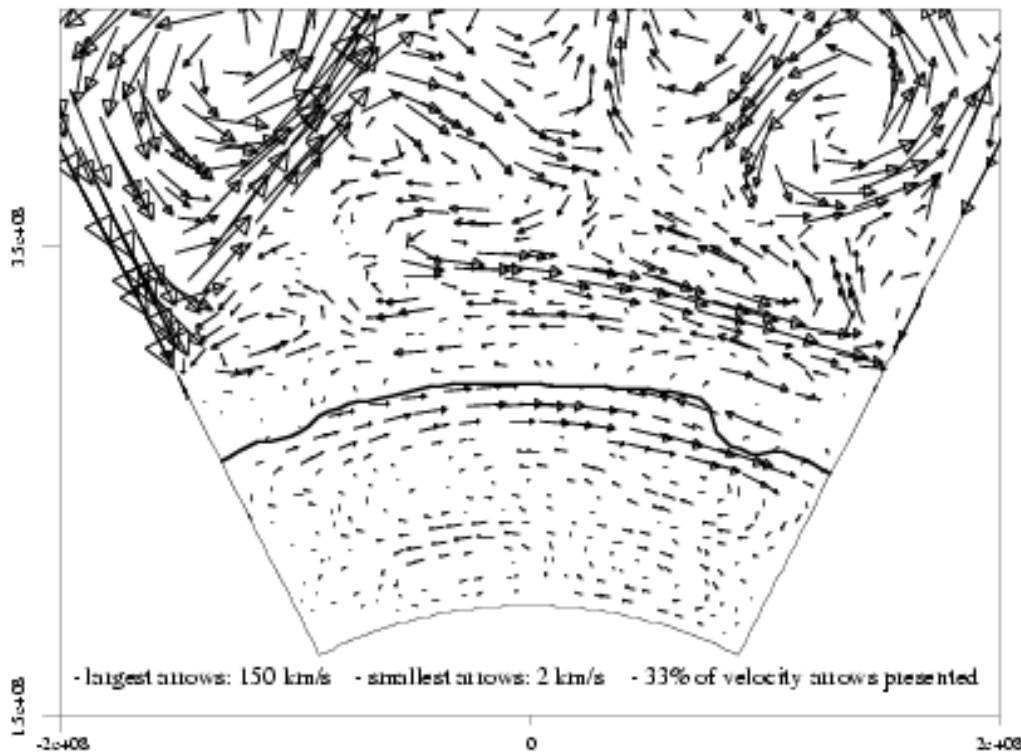
# Evolution of massive stars



For models of the explosions:

"Fe"-core masses and their entropies have to be known!

# Problems with massive star evolution: Non-local time-dependent convection!



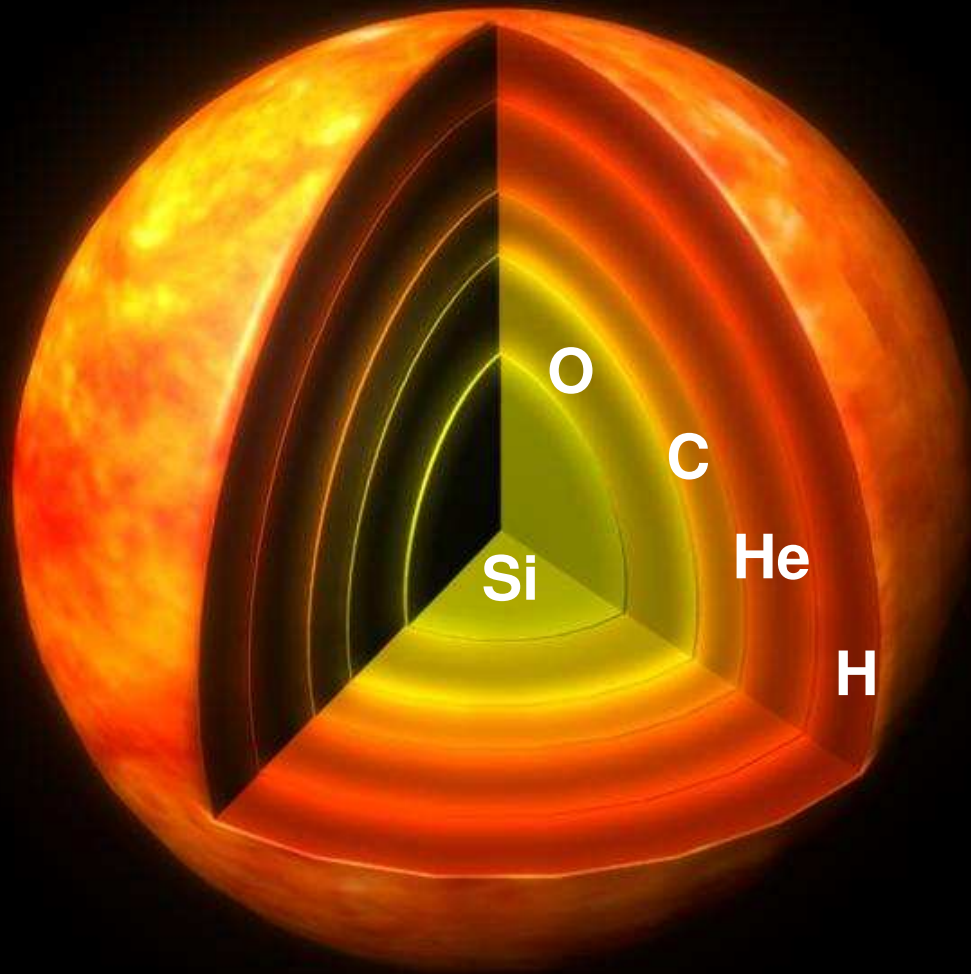
Hydrostatic O-burning  
(Asida & Arnett, 2000)

(See also Brummell et al. 2002,  
Rogers et al. 2003, ....)



Onion-like structure  
of a presupernova  
star several million  
years after its birth:

mass:  $10 \dots 10^2 M_{\text{sun}}$   
radius:  $50 \dots 10^3 R_{\text{sun}}$



- shells of different  
composition are  
separated by active  
thermonuclear  
burning shells

- core Si-burning  
leads to formation  
of central iron core

Note: figure not drawn to scale!

# Energy sources for a core collapse supernova

## Gravitational binding energy

Formation of a compact object of  $\sim 1$  solar mass  
with a radius  $\sim 10\text{km}$

$$\rightarrow E_b \sim 3 \times 10^{53} (M/M_{\text{sun}})^2 (R/10\text{km})^{-1} \text{erg}$$

Fe-Ni core:  $\rho \sim 10^{10} \text{g/cm}^3$ ,  $T \sim 10^{10} \text{K}$

$\rightarrow P \sim P_e$  (relativistic degenerate Fermi gas)

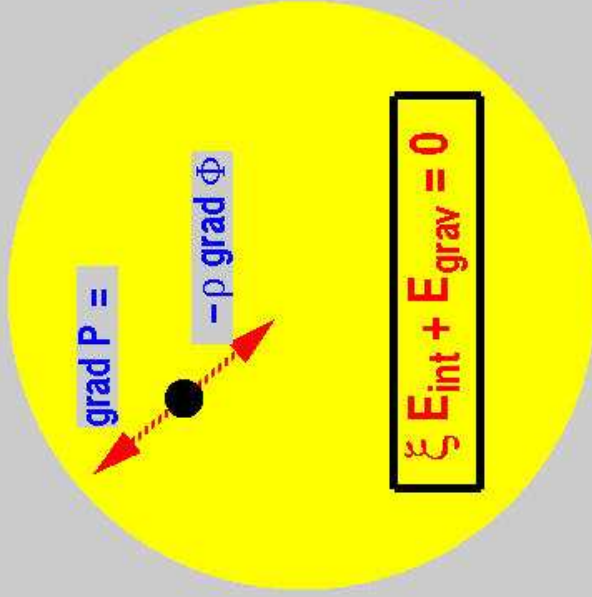
$\rightarrow$  maximum mass (Chandrasekhar)

## Core becomes unstable due to:

- a) electron captures
- b) photo-disintegrations

## Evolution towards gravitational collapse

stellar evolution mostly **hydrostatic**, i.e pressure and gravitational forces are in equilibrium



$$\xi E_{\text{int}} + E_{\text{grav}} = 0$$

virial theorem

$\xi := 3P/\rho u$  ideal gas:  $P = (\gamma-1) \rho u \rightarrow \xi = 3 (\gamma-1)$   
 relativ. Fermi gas:  $P = 1/3 \rho u \rightarrow \xi = 1$

total energy:

$$W := E_{\text{int}} + E_{\text{grav}} = (1-\xi) E_{\text{int}} = (\xi-1)/\xi E_{\text{grav}}$$

if  $\xi = 1 \rightarrow W = 0!$

## Evolution towards gravitational collapse

gas: finite temperature  $\rightarrow$  star radiates

energy conservation:

$$dW/dt + L = 0$$

luminosity

$$L = (\xi-1) dE_{\text{int}}/dt = -(\xi-1)/\xi dE_{\text{grav}}/dt$$

if  $L > 0 \rightarrow dE_{\text{grav}}/dt < 0 \leftarrow$

**contraction**  $\rightarrow dE_{\text{int}}/dt > 0$

contraction with  $\gamma = 5/3$  ( $\xi = 2$ ):

50% of liberated energy are radiated away

50% of liberated energy heat the star

$\rightarrow$  **star has negative specific heat!**

Blue Giant (Red Giant:  $\times 100$ )

30 000 000 km

Fe-Ni core

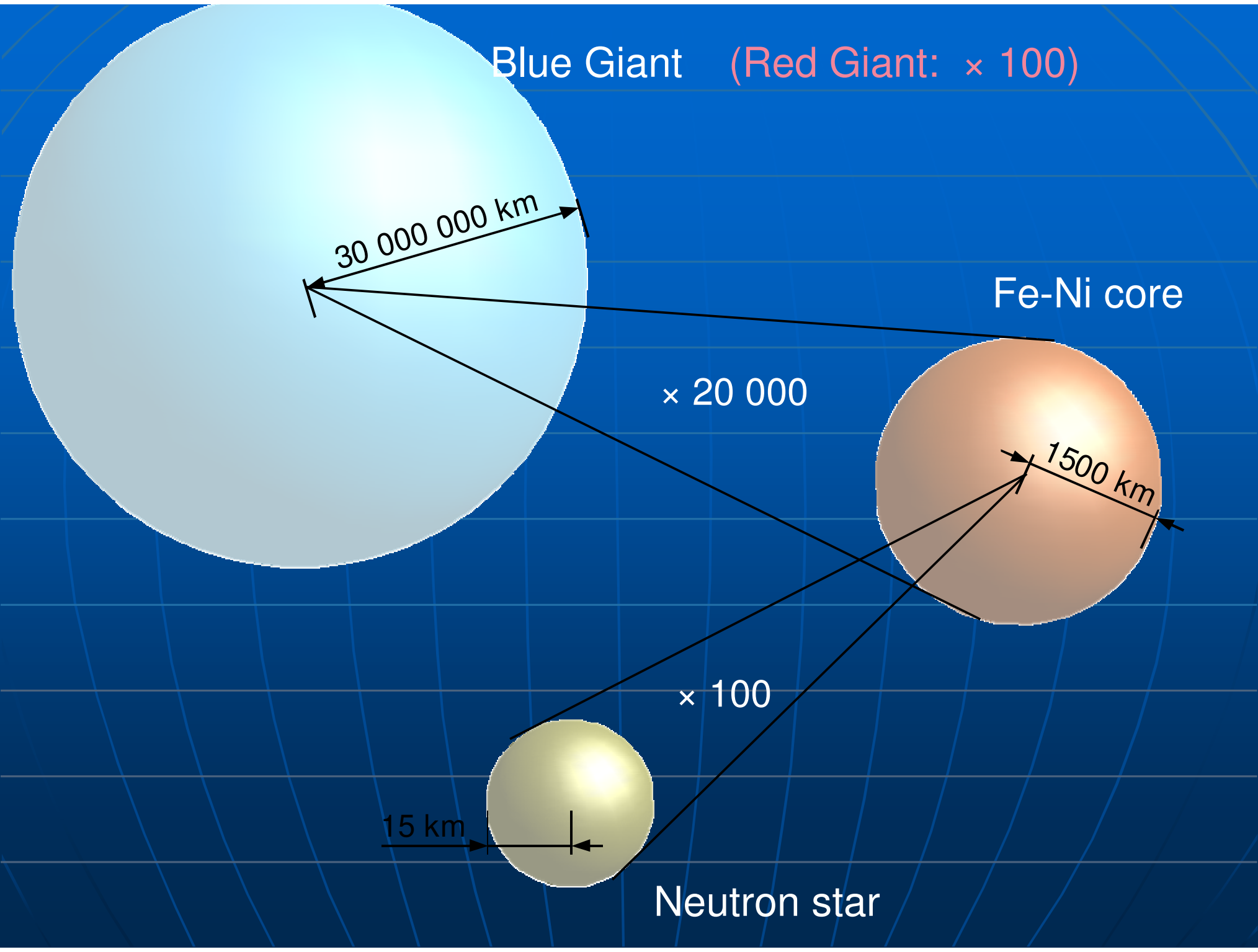
$\times 20\ 000$

1500 km

$\times 100$

15 km

Neutron star



## Simulations of core collapse supernovae challenging, because of:

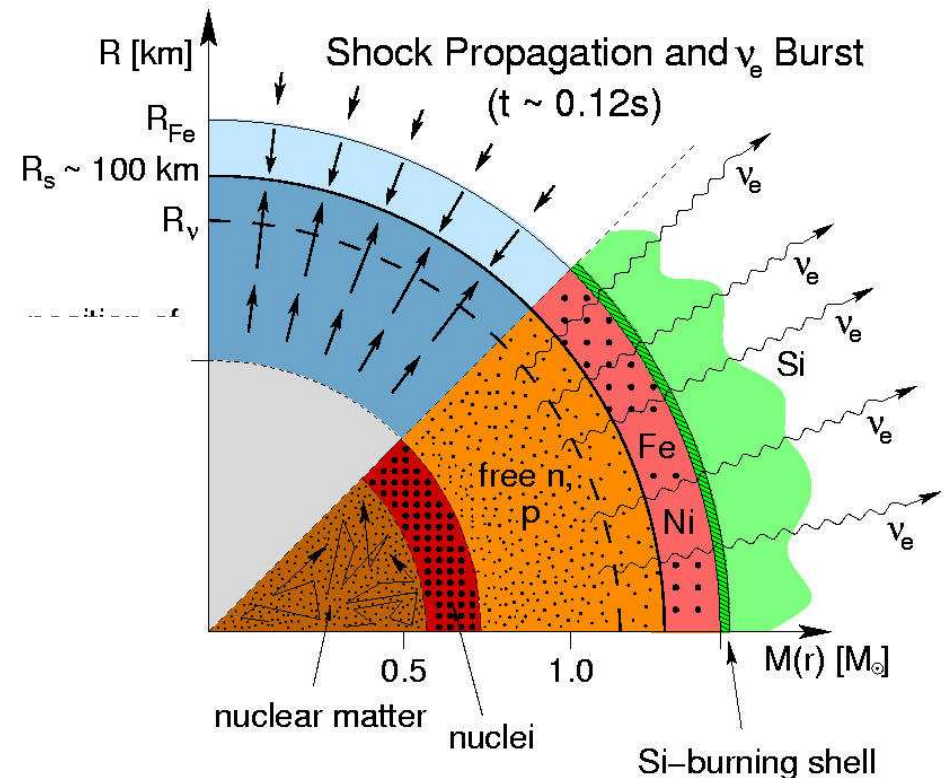
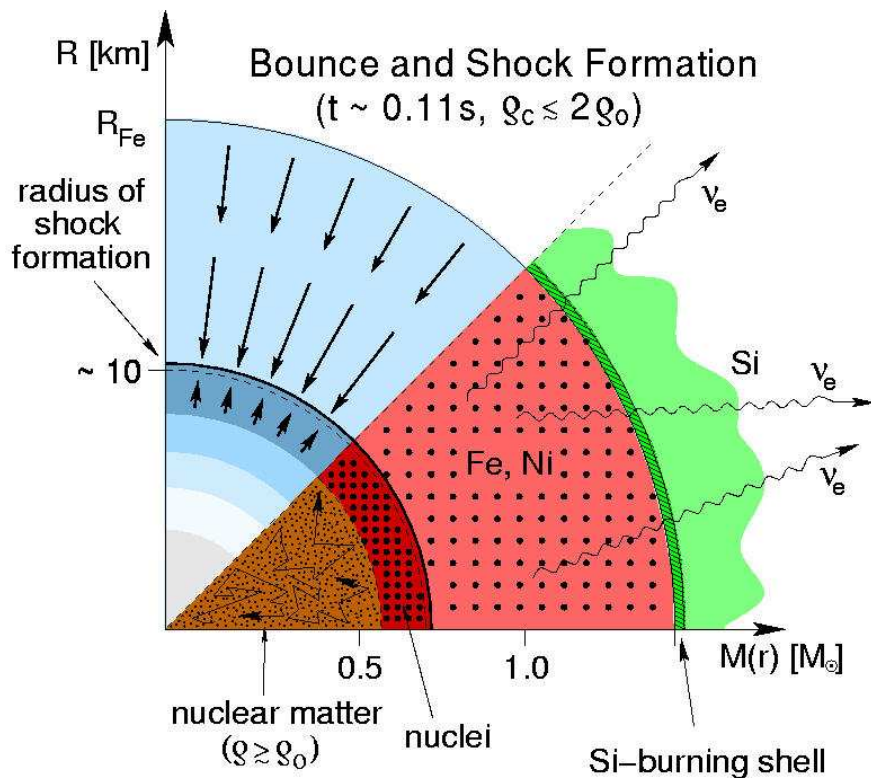
a) **neutrino transport** (fermions, multi-flavor)  
(semi-transparent region: Boltzmann solver)

b) very **different time** and **length scales**  
→ adaptive mesh refinement (AMR)

c) **multi-dimensional** flow problem

# Core collapse supernovae:

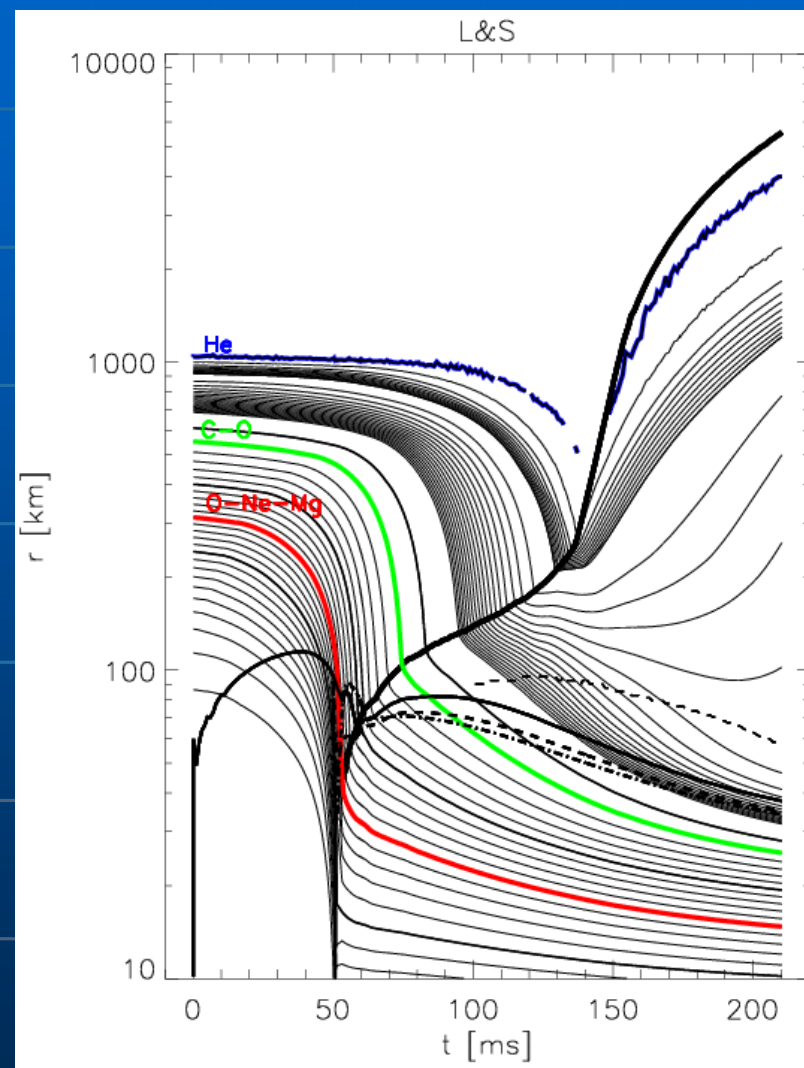
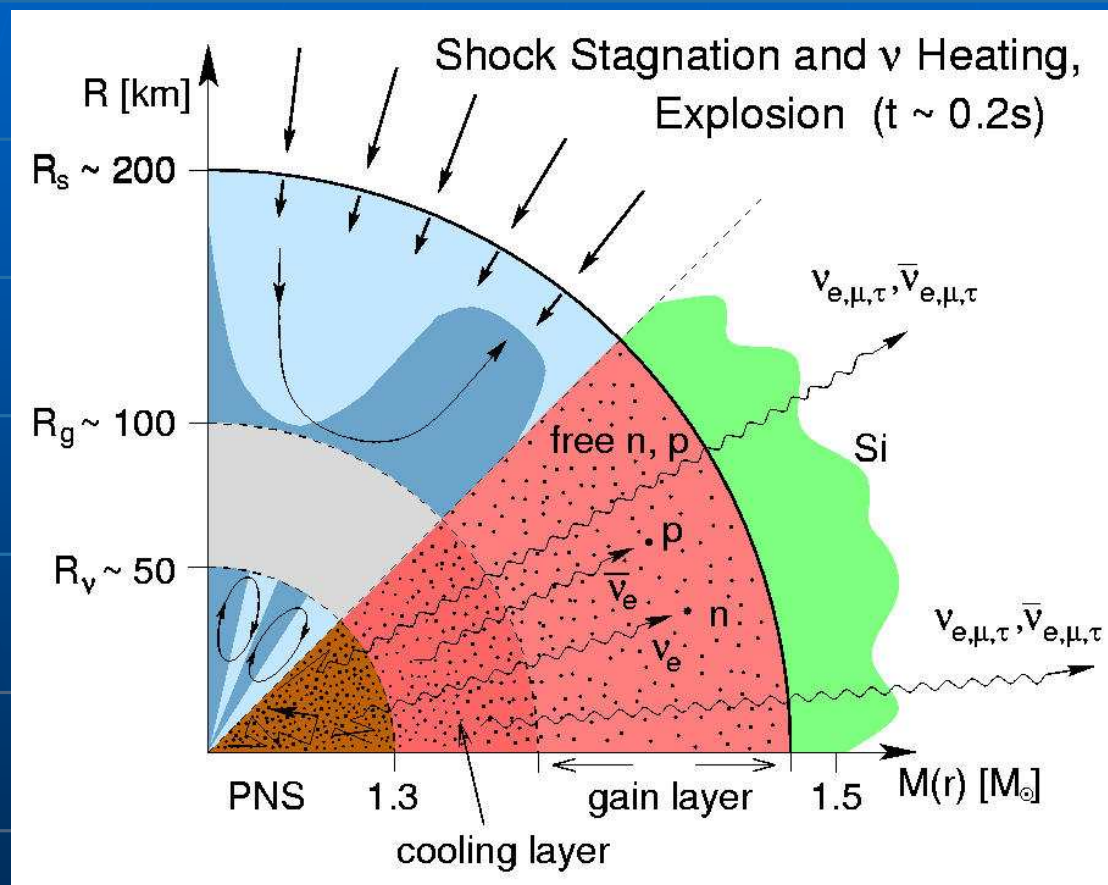
- Prompt explosion mechanism does not work (explored during the 1970's and 1980's; commonly accepted early 1990's)



- Shock wave forms close to sonic point ( $M \sim 0.7 M_{\text{sun}}$ )  
initial energy:  $(5 \dots 8) \times 10^{51}$  erg

- Severe energy losses during shock propagation (8 MeV/nucleon or  $1.6 \times 10^{51}$  erg/ $0.1M_{\text{sun}}$ )

- Current paradigm: neutrino-driven delayed explosions (discovered through computer simulations by Wilson '82, and first analyzed by Wilson & Bethe '95)



In its simplest form: Seems to work for low-mass core only! (Kitaura et al '05)

∅ Observations imply: non-radial flow and mixing are common in core collapse supernovae

∅ Theoretical models based on delayed explosion mechanism predict non-radial flow and mixing due to:

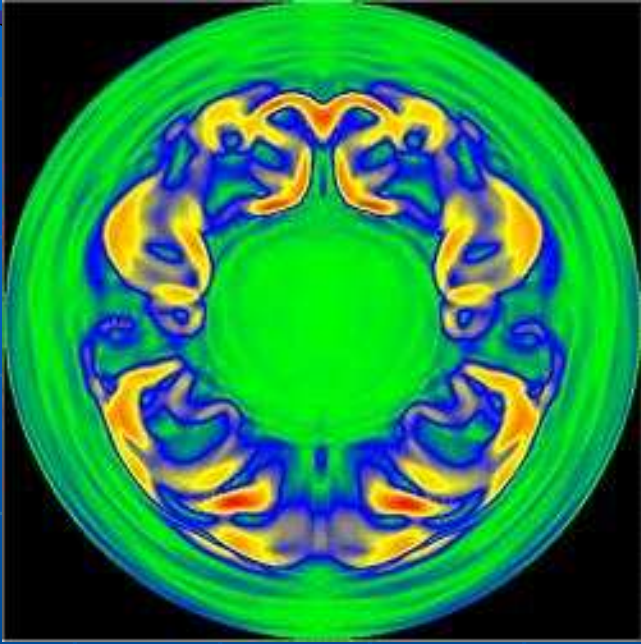
- Ledoux convection inside the proto-neutron star (deleptonization and neutrino diffusion)

- convection inside neutrino heated hot bubble (neutrino energy deposition behind the shock)

- Rayleigh-Taylor instabilities in stellar envelope (non-steady shock propagation; hot bubble)

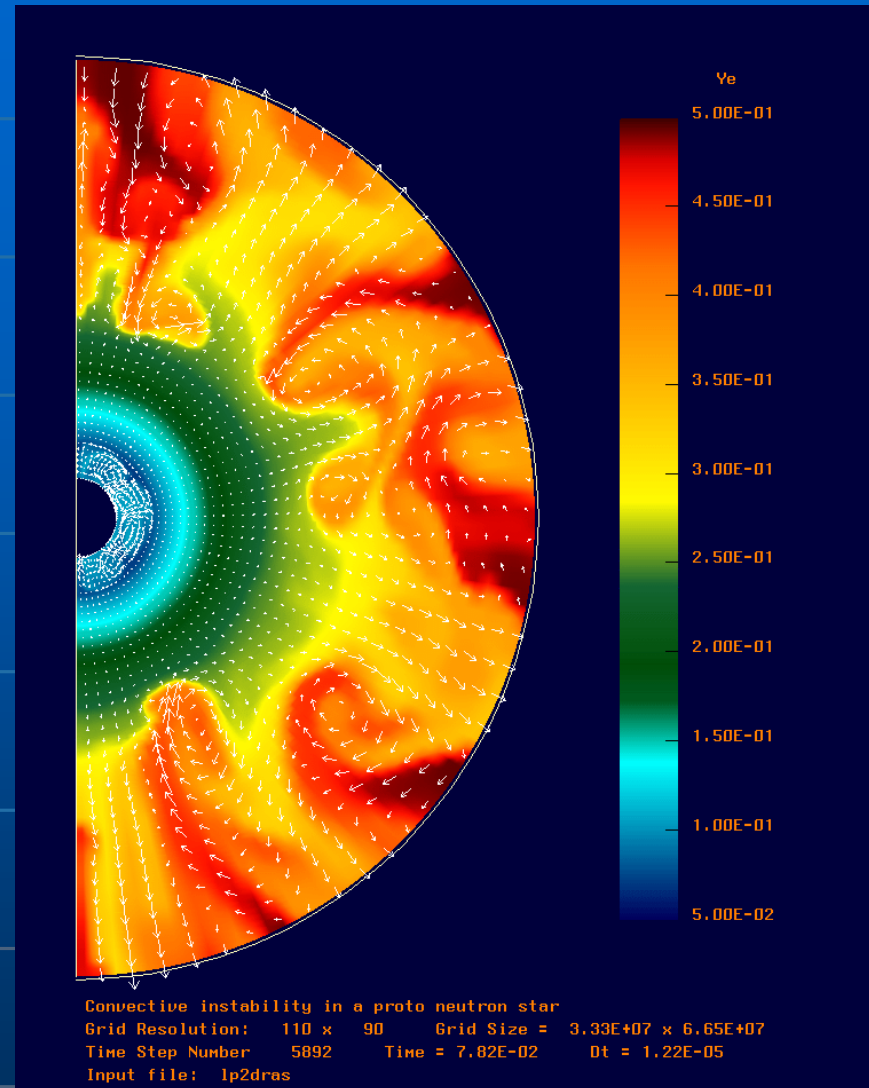


# Core collapse supernovae need multidimensional modeling !



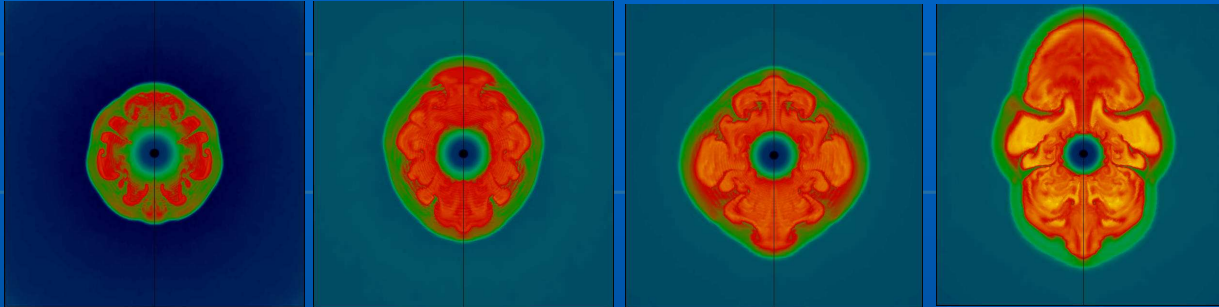
Ledoux convection inside proto-neutron star due to negative lepton and entropy gradients (Keil, Janka & Müller '96)

- asymmetric  $\nu$ -emission (few sec) and flow ( $\sim 100$  s?)

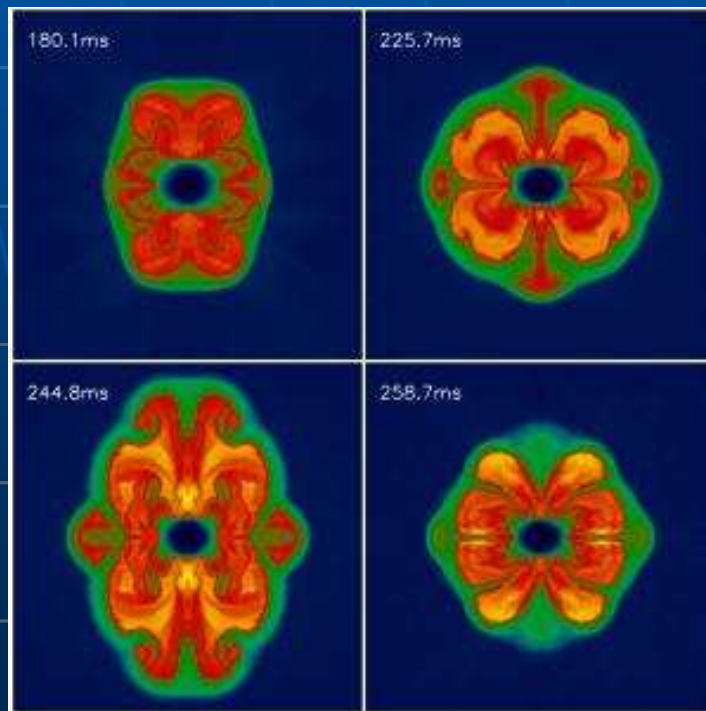


Convection in the surface layers of the proto-neutron star and in the hot bubble 78 ms after core bounce (Janka & Müller '96)

- State-of-the-art hydrodynamic simulations with Boltzmann  $\nu$ -transport, realistic EOS, relativistic gravity, and realistic progenitors



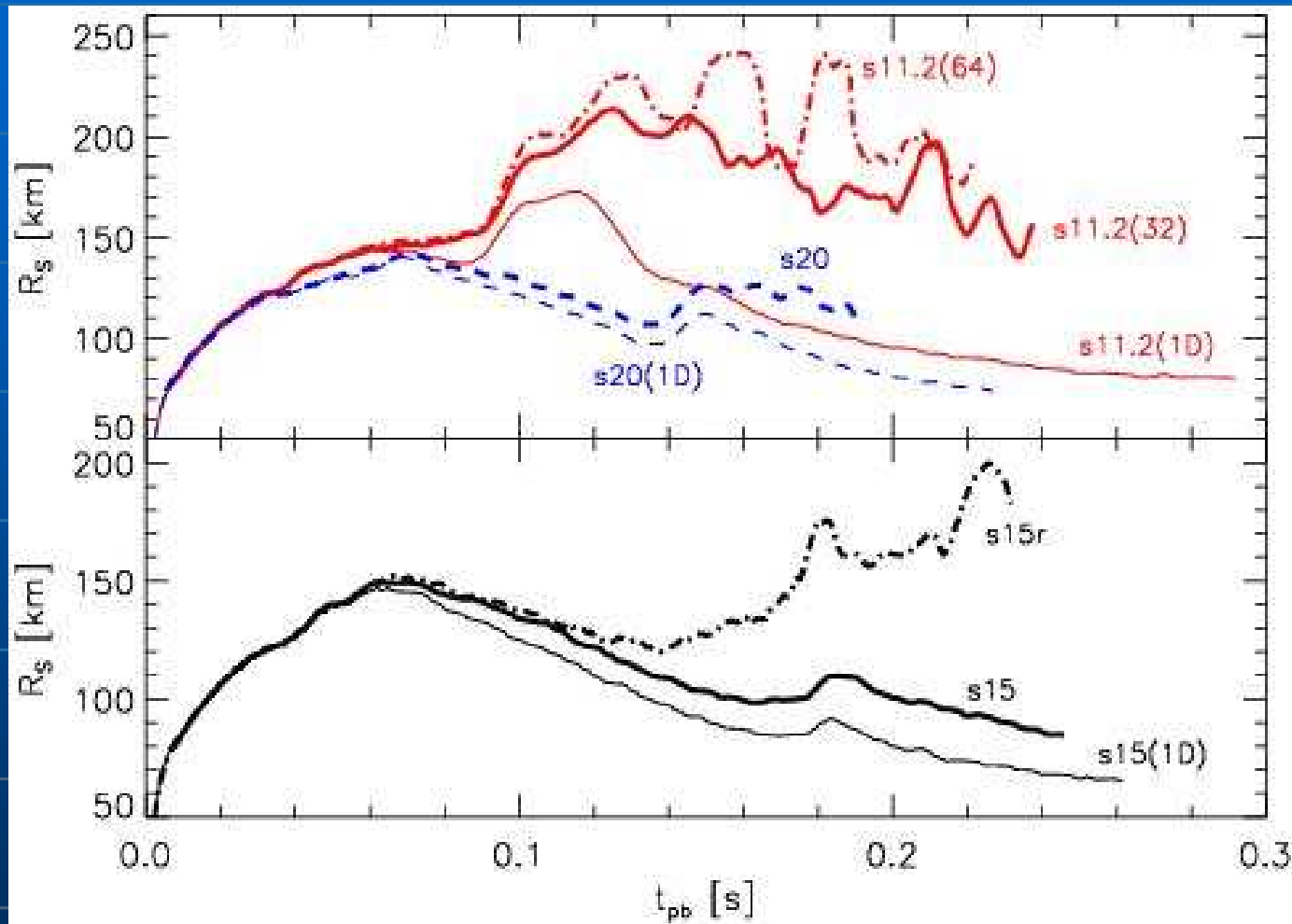
Snapshots, 2D run of a non rotating axisymmetric  $11.2 M_{\text{sun}}$  progenitor (Buras, Rampp & Janka 2003)



Snapshots, 2D run of a rotating axisymmetric  $15 M_{\text{sun}}$  progenitor  
( $b_{\text{initial}} = 0.05\%$  ,  $\omega_{i,c} = 0.5 \text{ s}^{-1}$  ; Heger et al 2003)

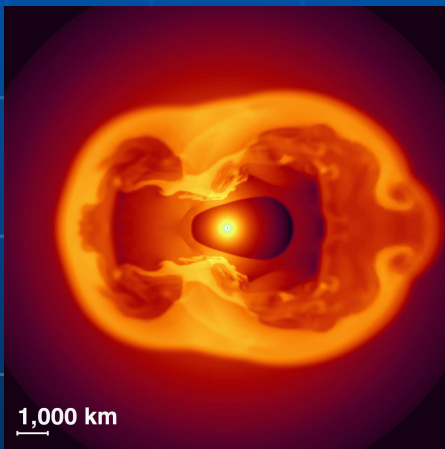
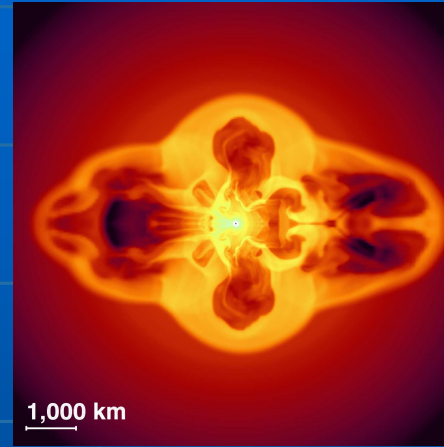
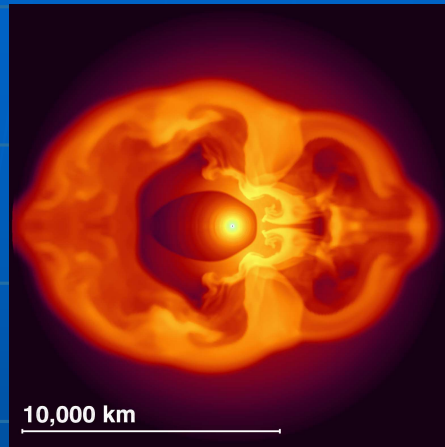
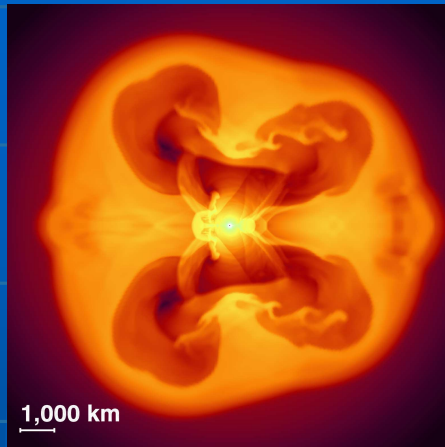
(Buras, Rampp, Janka & Kifonidis 2003)

# Core Collapse Supernovae: But ...

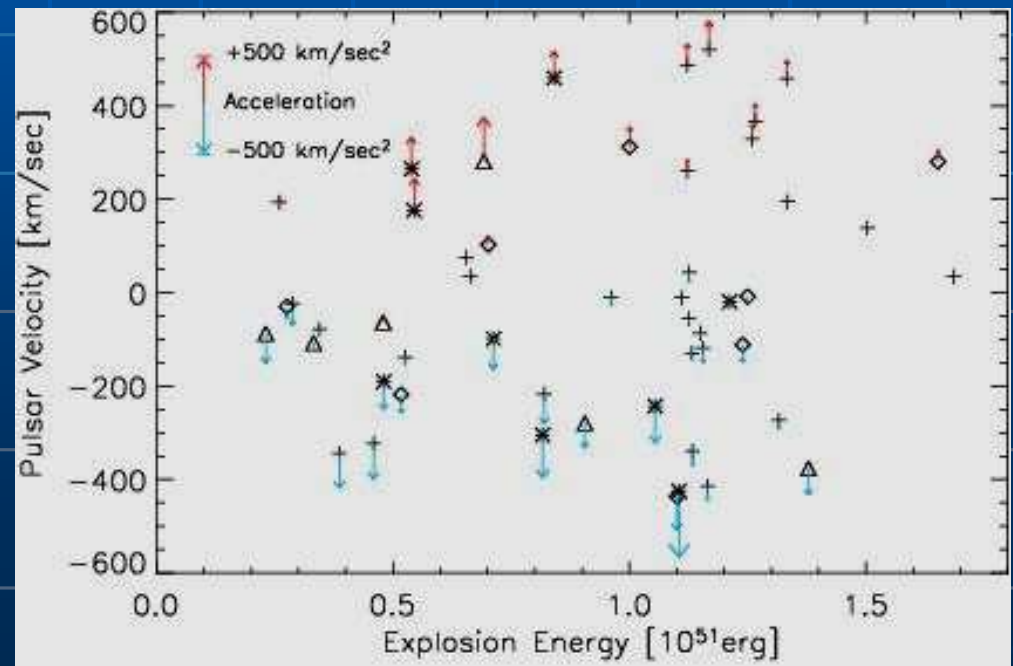


Buras et al. (2003): *No explosions (in 2-D) !!!*

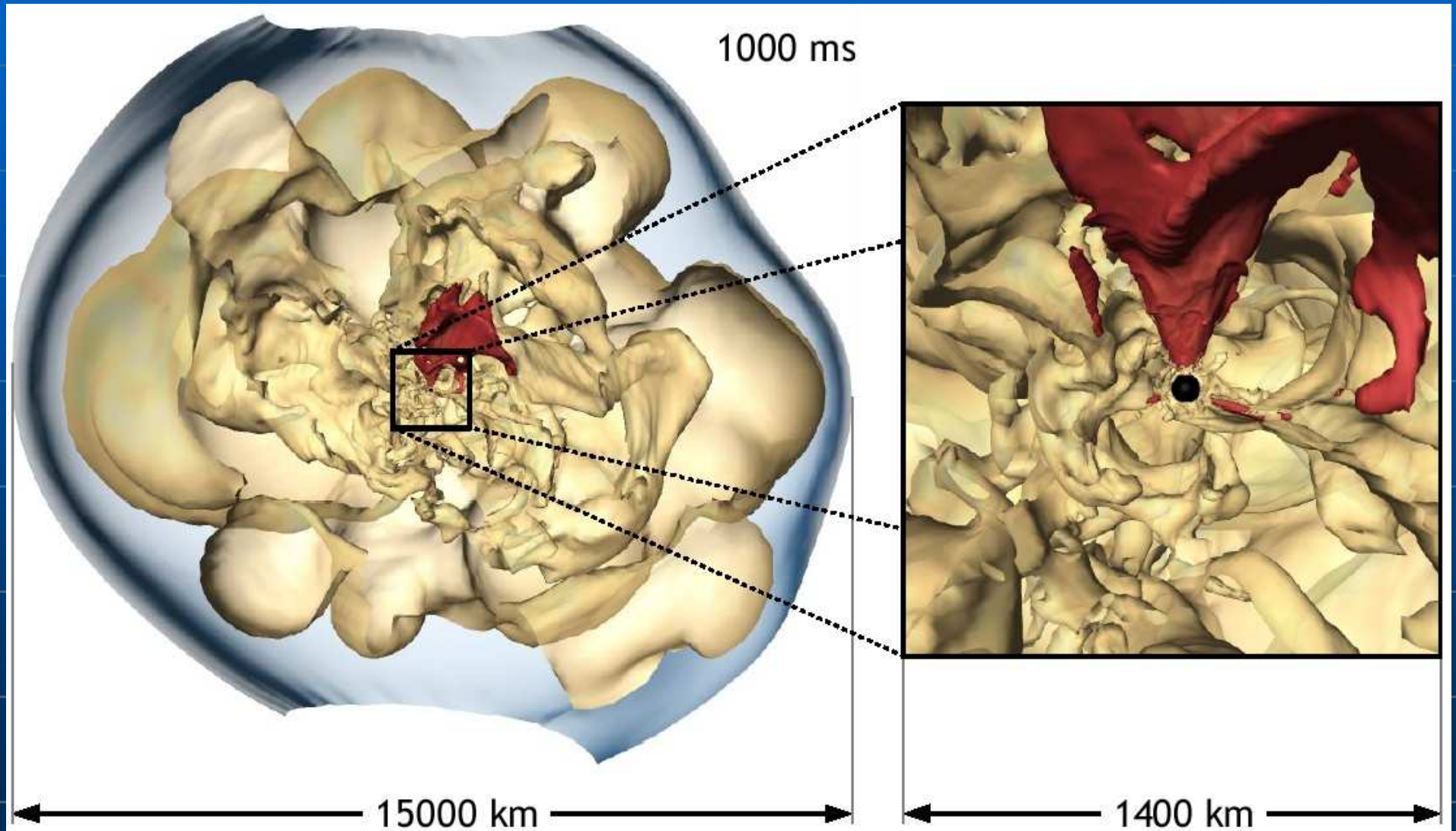
- 2D simulations show growth of dipolar ( $l=1$ ) mode in post-shock layer  $\rightarrow$  neutron star kicks (Scheck et al. 2003)



Density distribution 1 sec  
after core bounce



- Global dipolar oscillations of the post-shock layer also seen in recent 3D simulations neglecting (Blondin et al. '03) or simplifying (Scheck et al. '04) the treatment of  $\nu$ -transport



3D core collapse simulation: shock,  $Y_e = \text{const}$  & downflow to NS (Scheck 2004)

**t = 0.002 sec**

**Density**

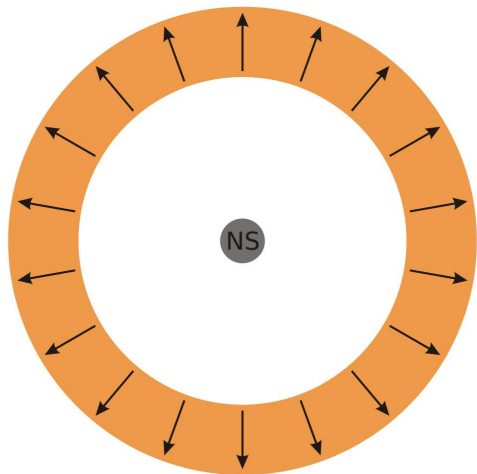


L. Scheck

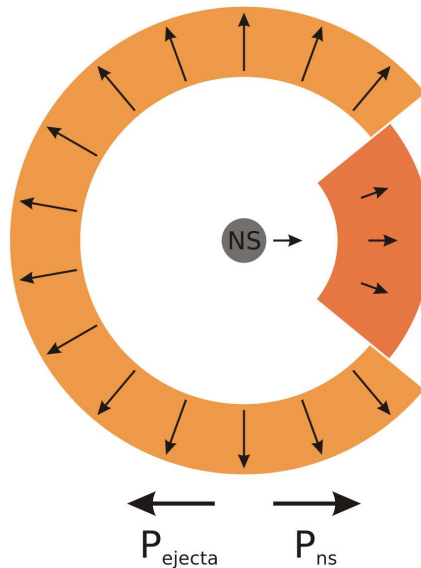
**100 km**



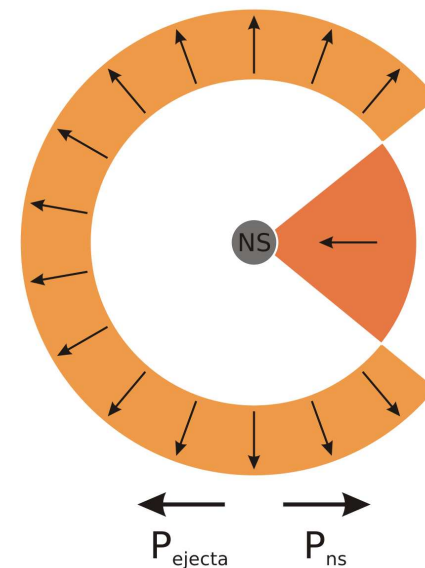
**Entropy**



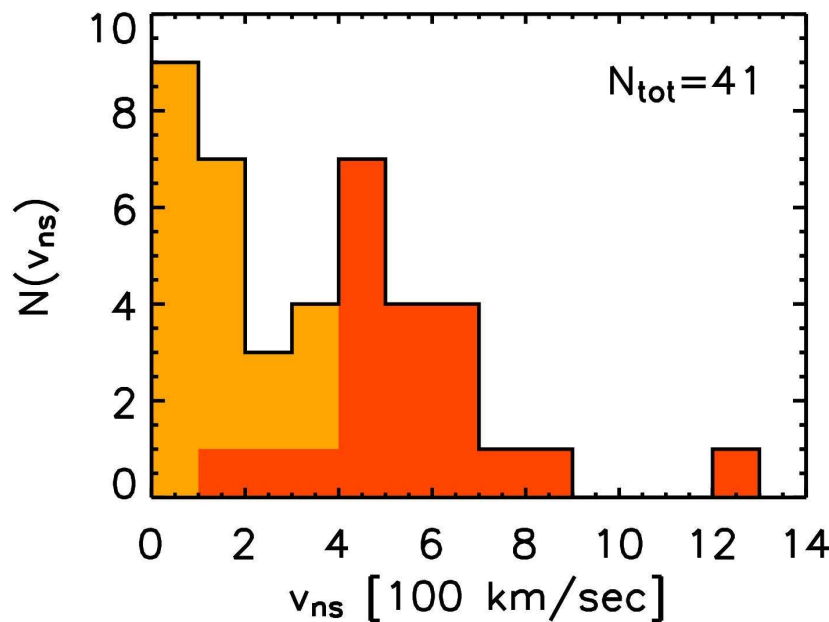
spherical explosion:  
no kick



anisotropic explosion: kick due  
to **gravitational acceleration**



anisotropic explosion: kick due  
to **anisotropic accretion**



Large set of  
simulations shows  
bi-modal kick  
velocity distribution  
(Scheck 2005)

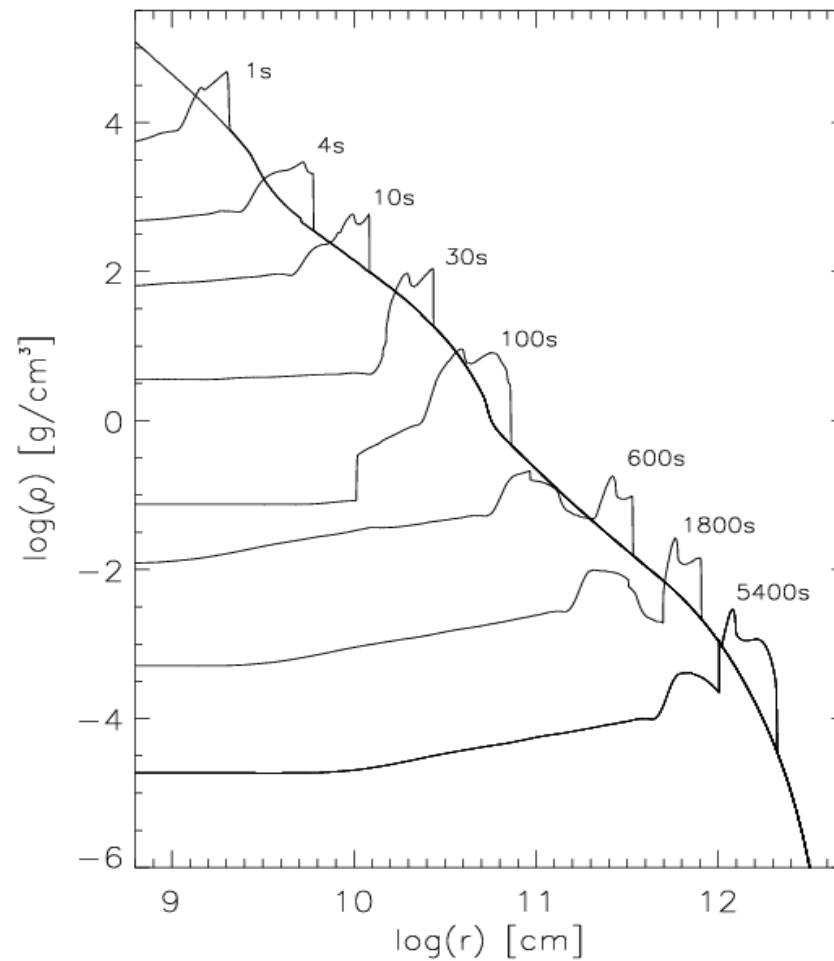


$T = 0$  msec

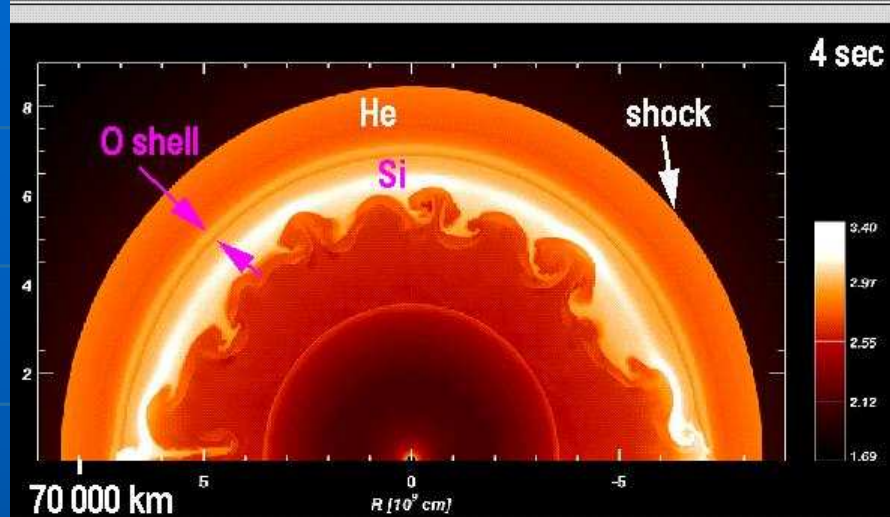


# Core Collapse Supernovae: Further evolution

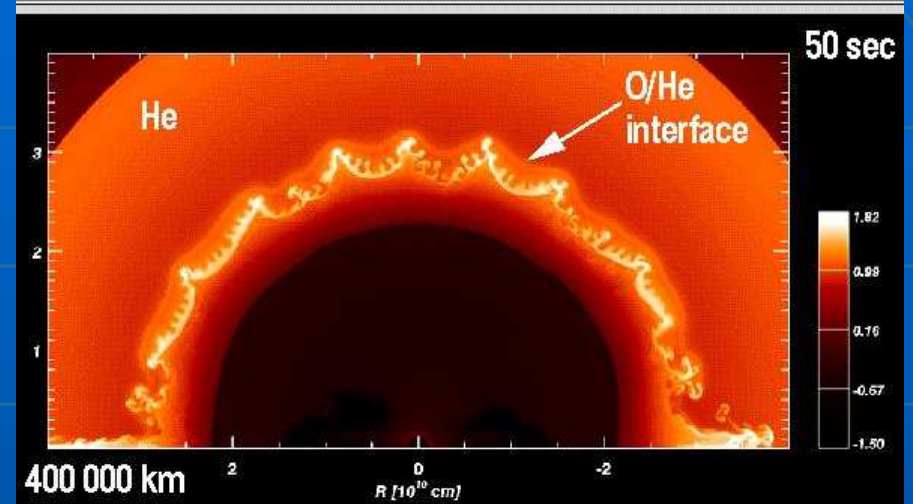
**Unsteady shock propagation through stellar envelope** --> **Rayleigh Taylor unstable regions**



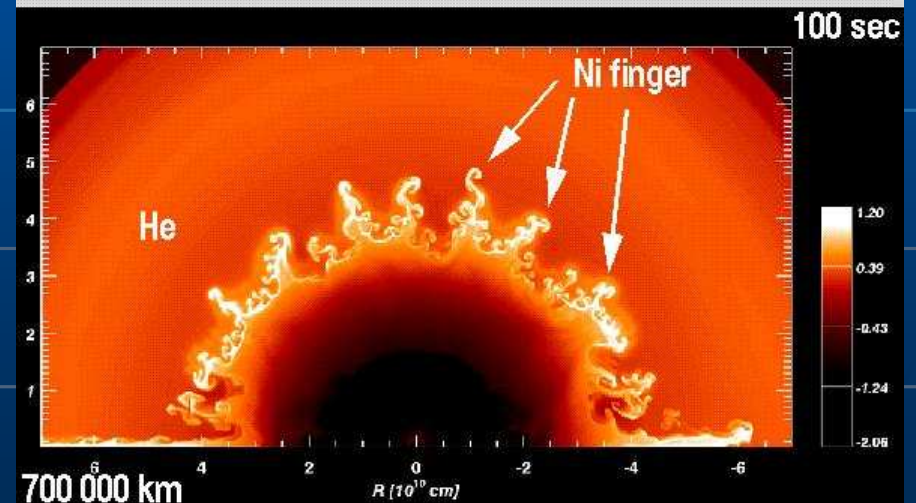
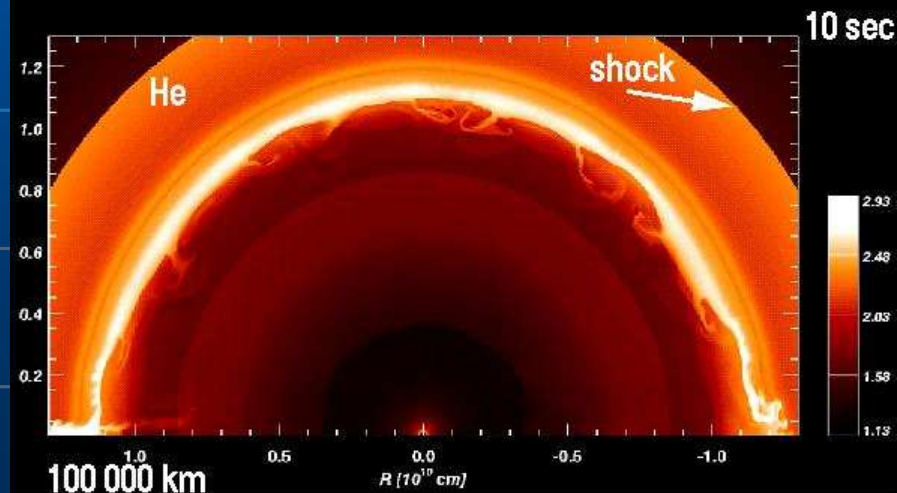
# n Instabilities, mixing and nucleosynthesis



density



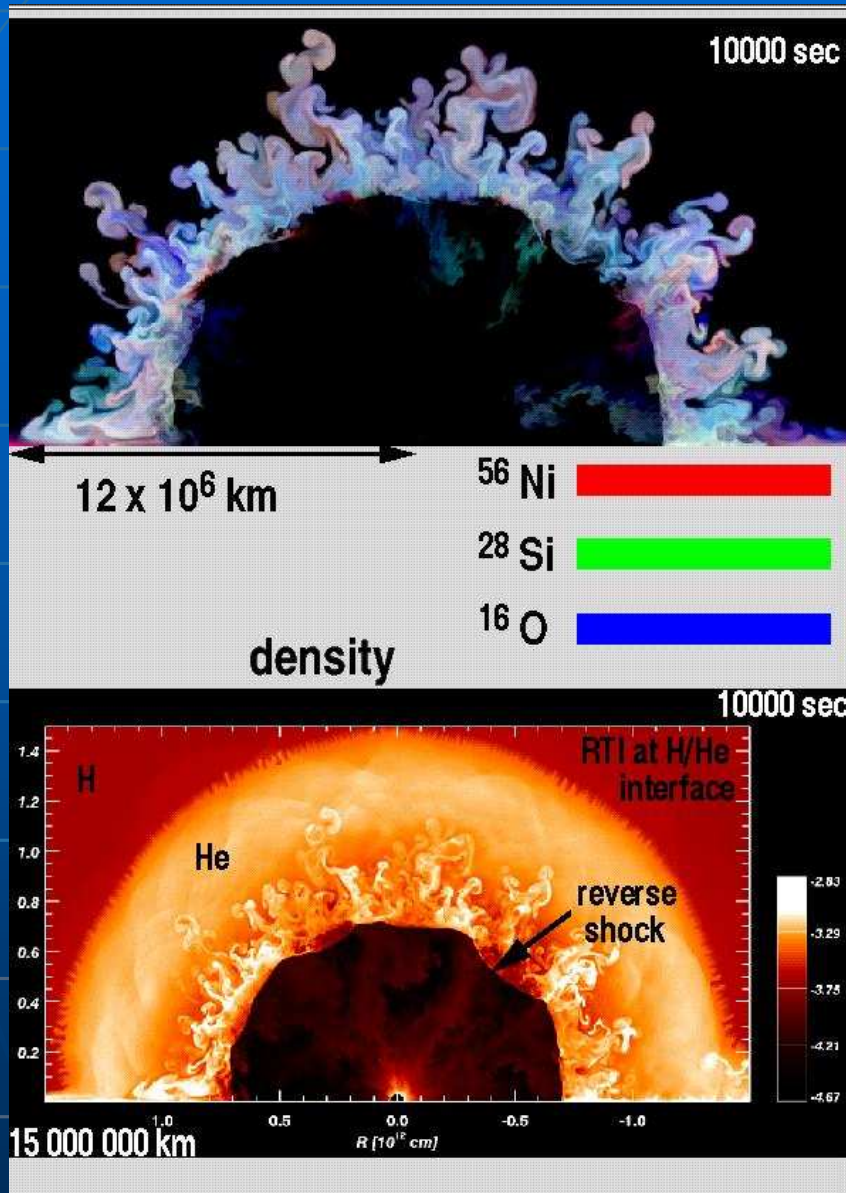
density



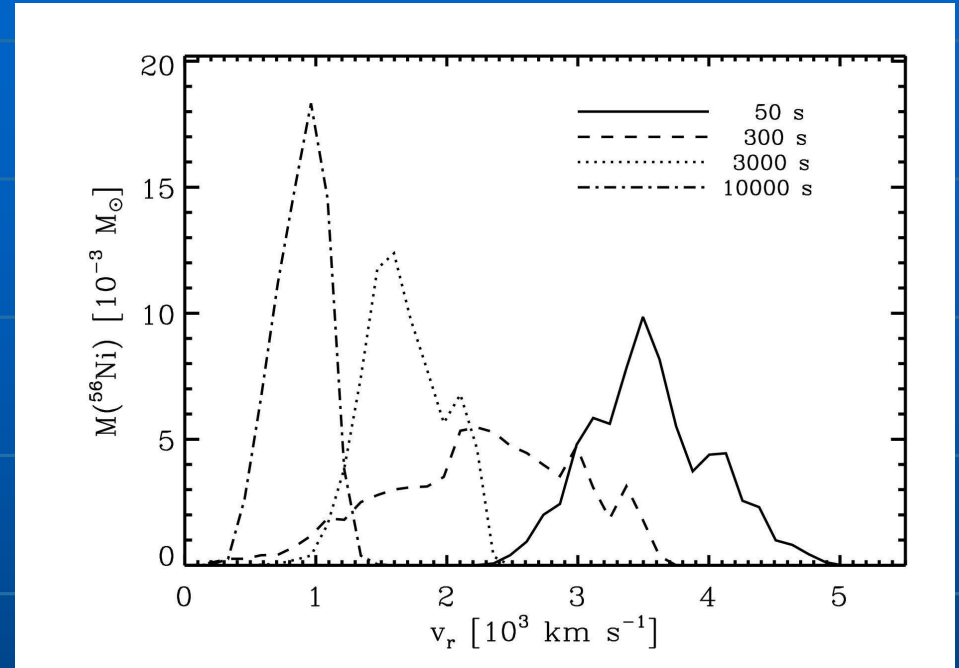
AMR simulation of shock propagation through stellar envelope (Kifonidis, Plewa, Janka & Müller 2003)

1 sec

# n Instabilities, mixing and nucleosynthesis

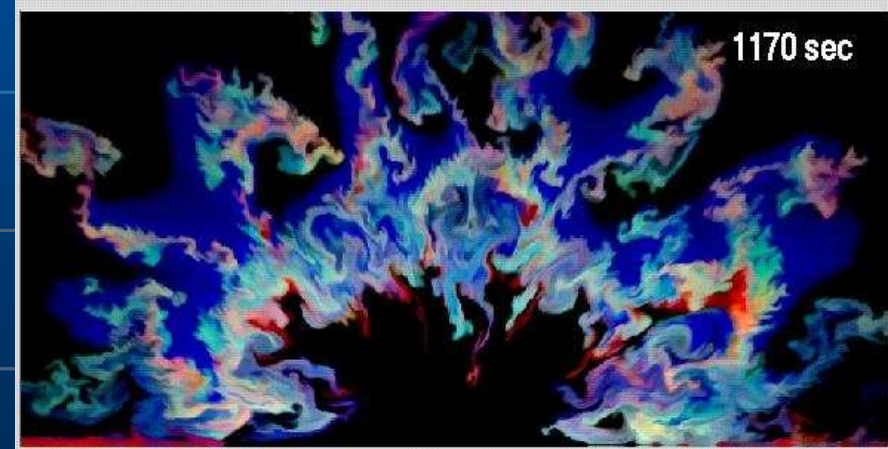
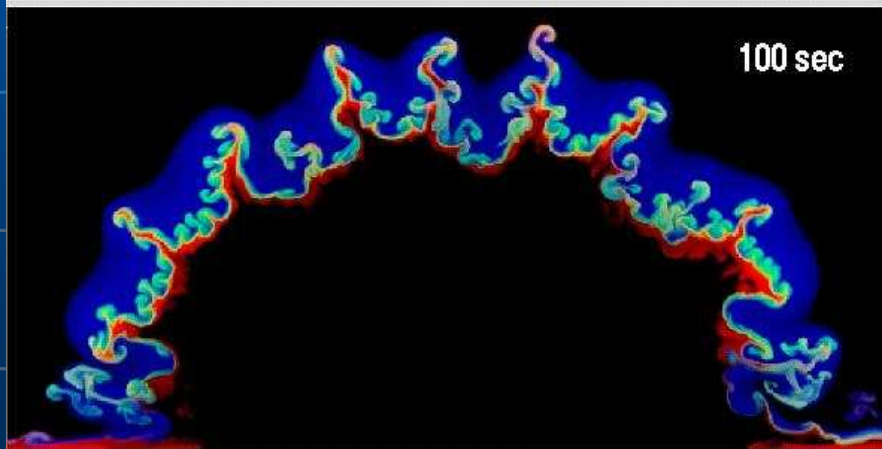
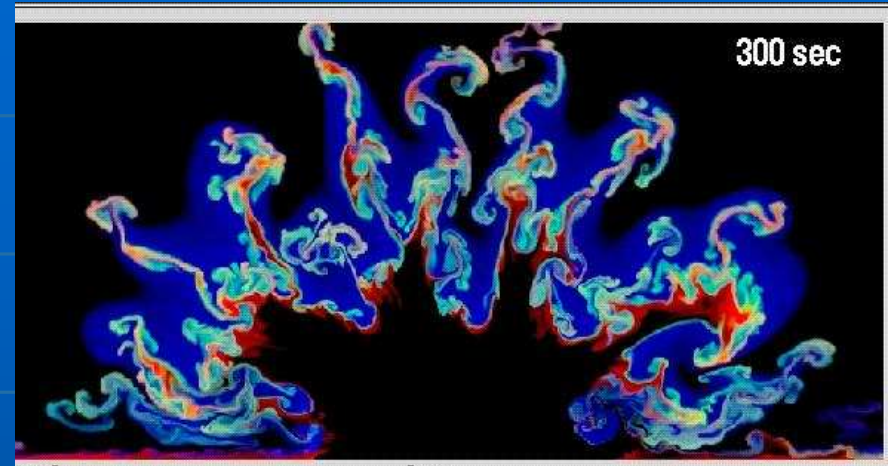
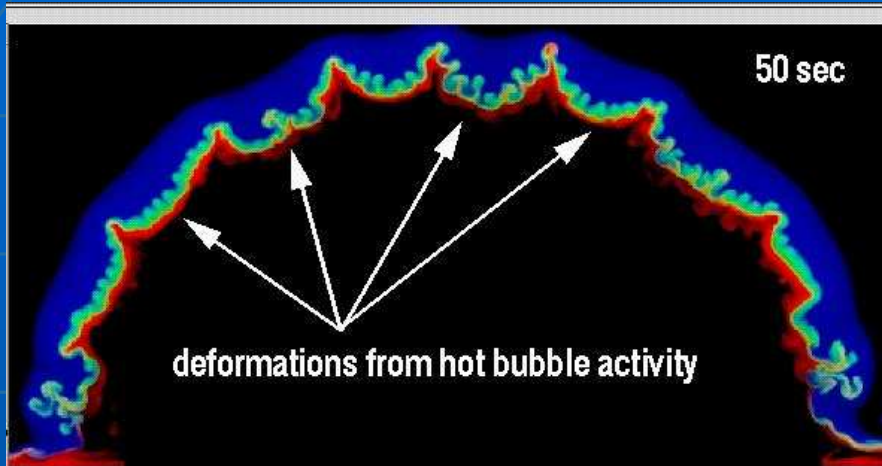


AMR simulation of shock propagation through stellar envelope (Kifonidis, Plewa, Janka & Müller 2003)



- results of simulations in accordance with observations of SNe Ib/Ic
- simulations do not reproduce large velocities of Fe/Ni observed in SN 1987A

# n Instabilities, mixing and nucleosynthesis (cont.)

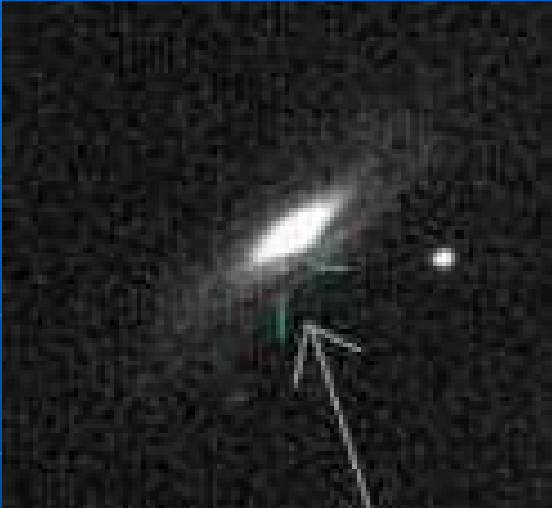


AMR simulation of shock propagation through stellar envelope (Kifonidis, Plewa, Janka & Müller 2003)

## Summary (Part I)

- q Core-collapse supernova explosions are triggered by neutrino interactions with matter and hydrodynamic instabilities and/or rotation (magnetic fields?).
- q Even the best models available predict weak explosions only.
- q What is the missing physics?
- q “Artificially” triggered explosion models predict nuclear abundances in fair agreement with observations.

# Thermonuclear (Type Ia) Supernovae



## Example:

SN 2002bo in NGC 3190;

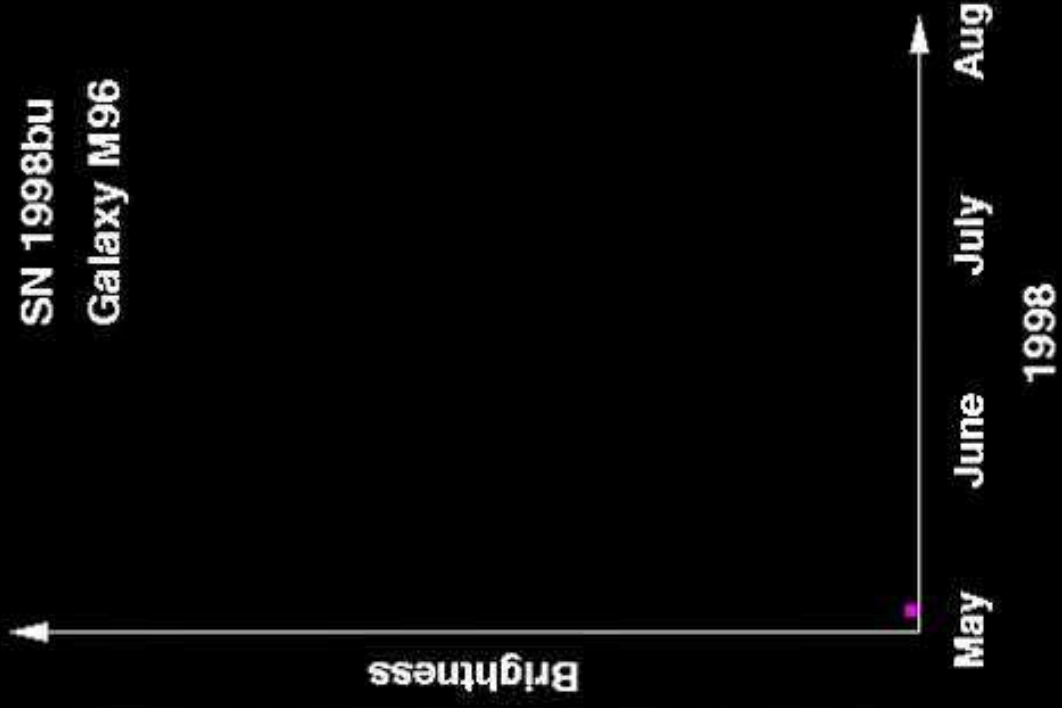
Discovered: March 9, 2002

B-maximum: March 22, 2002



(RTN/ESC)

SN 1998bu  
Galaxy M96





# The “standard model”

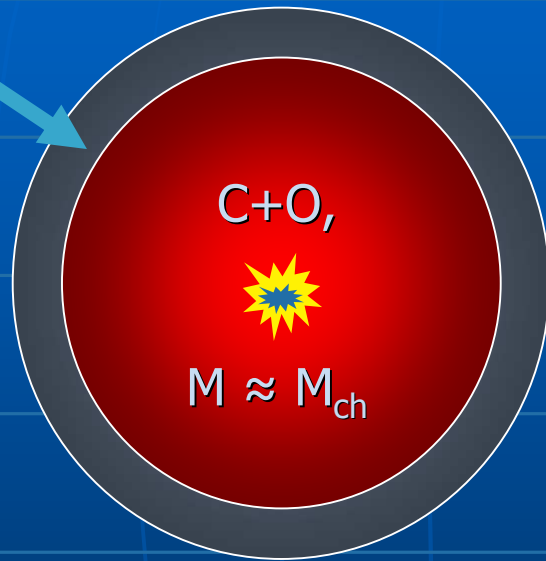


- ∅ White dwarf in a binary system
- ∅ Growing to the Chandrasekhar mass by mass transfer



# The "standard model"

He (+H)  
from binary  
companion



Density  $\sim 10^9 - 10^{10}$  g/cm

Temperature: a few  $10^9$  K

Radii: a few 1000 km

Explosion energy:

*Fusion of*

*C+C, C+O, O+O*

*⇒ "Fe"*

Laminar burning

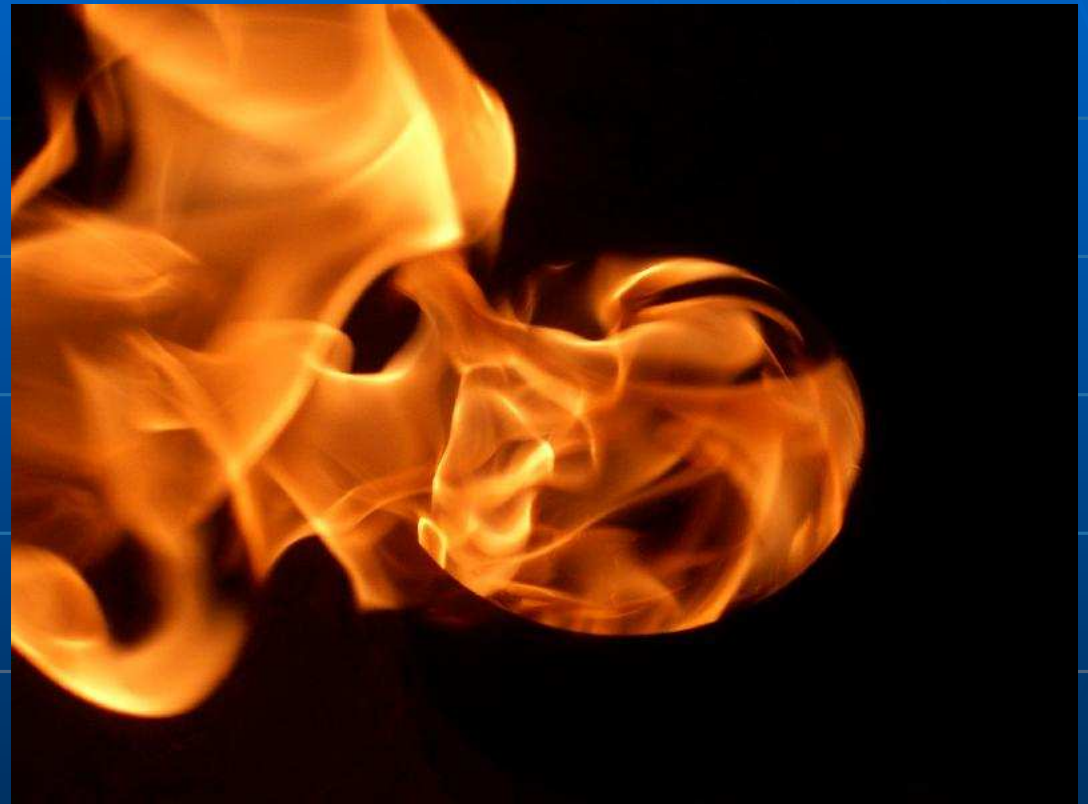
velocity:

*$U_L \sim 100$  km/s  $\ll U_S$*

***Too little is burned!***

# The physics of turbulent combustion

- ∅ Everyday experience:  
*Turbulence increases the burning velocity.*
- ∅ In a star:  
Reynoldsnumber  $\sim 10^{14}$  !
- ∅ In the limit of strong turbulence:  $U_B \sim V_T$  !
- ∅ Physics of thermonuclear burning is very similar to premixed chemical flames.



## A couple of definitions:

Kolmogorov (length) scale

$$\eta := (v^3/\varepsilon)^{1/4}$$

(Turbulent) Reynolds number

$$Re := v'/s_L \cdot l_F$$

(Turbulent) Damköhler number

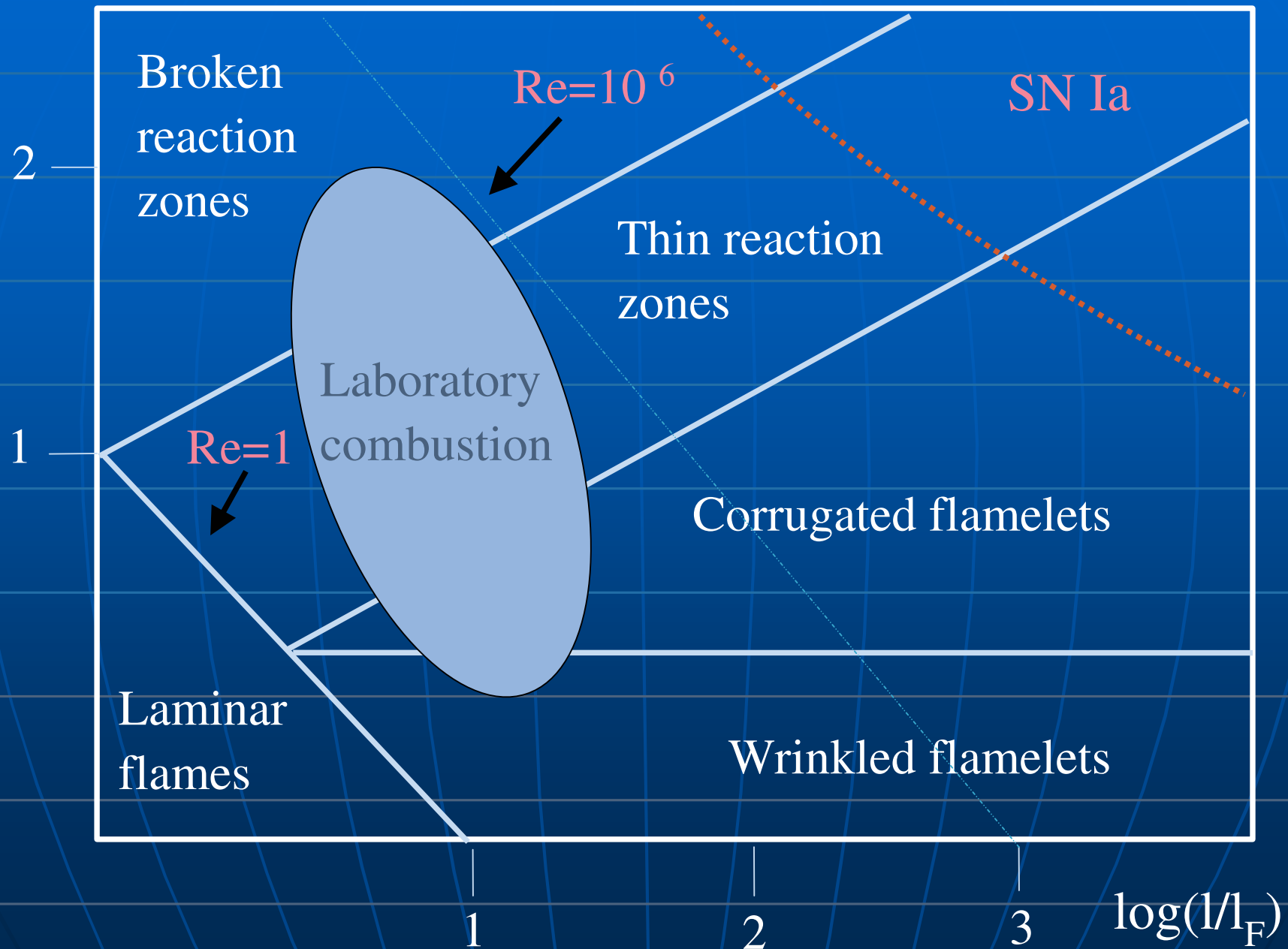
$$Da := s_L/v' \cdot l_F$$

(Turbulent) Karlovitz number

$$Ka := l_F^2/\eta^2$$

$$\Rightarrow Re = Da^2 \cdot Ka^2$$

$\log(v'/s_L)$



# Burning regimes of pre-mixed flames

## 1. Cellular burning, wrinkled flamelets

$$u_{\text{cell}} = s_L [1 + \varepsilon(\mu)] ; \mu = \rho_b / \rho_u ,$$

$$\varepsilon(\mu) \approx 0.41 (1 - \mu)^2$$

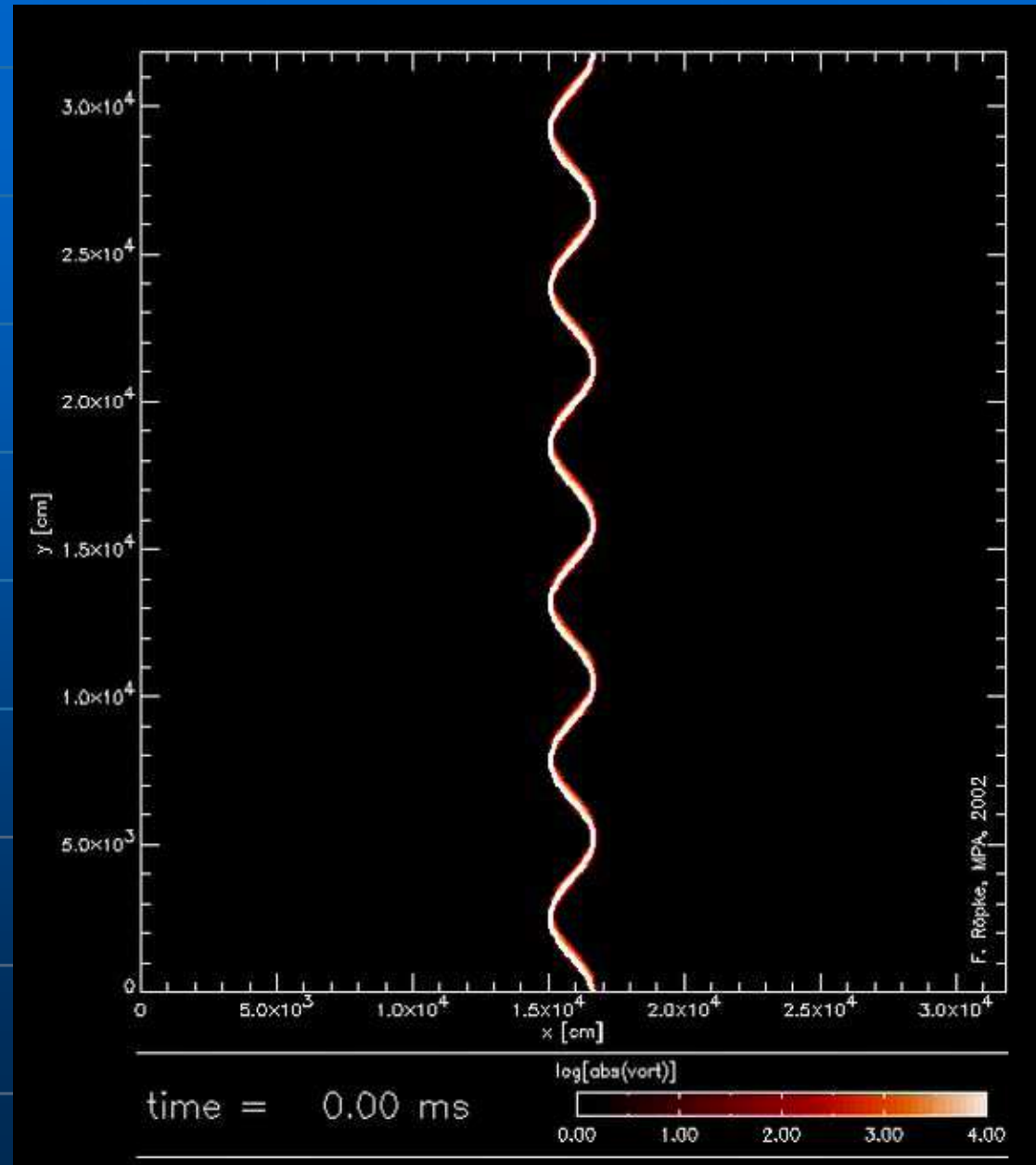
Or: “Fractal model”

$$u_{\text{cell}}(l) = s_L (l/l_{\text{crit}})^{D-1}$$

The Landau-Darrieus  
instability and its  
interaction with  
turbulence:

Quiescent fuel

(Röpke et al., 2003a)

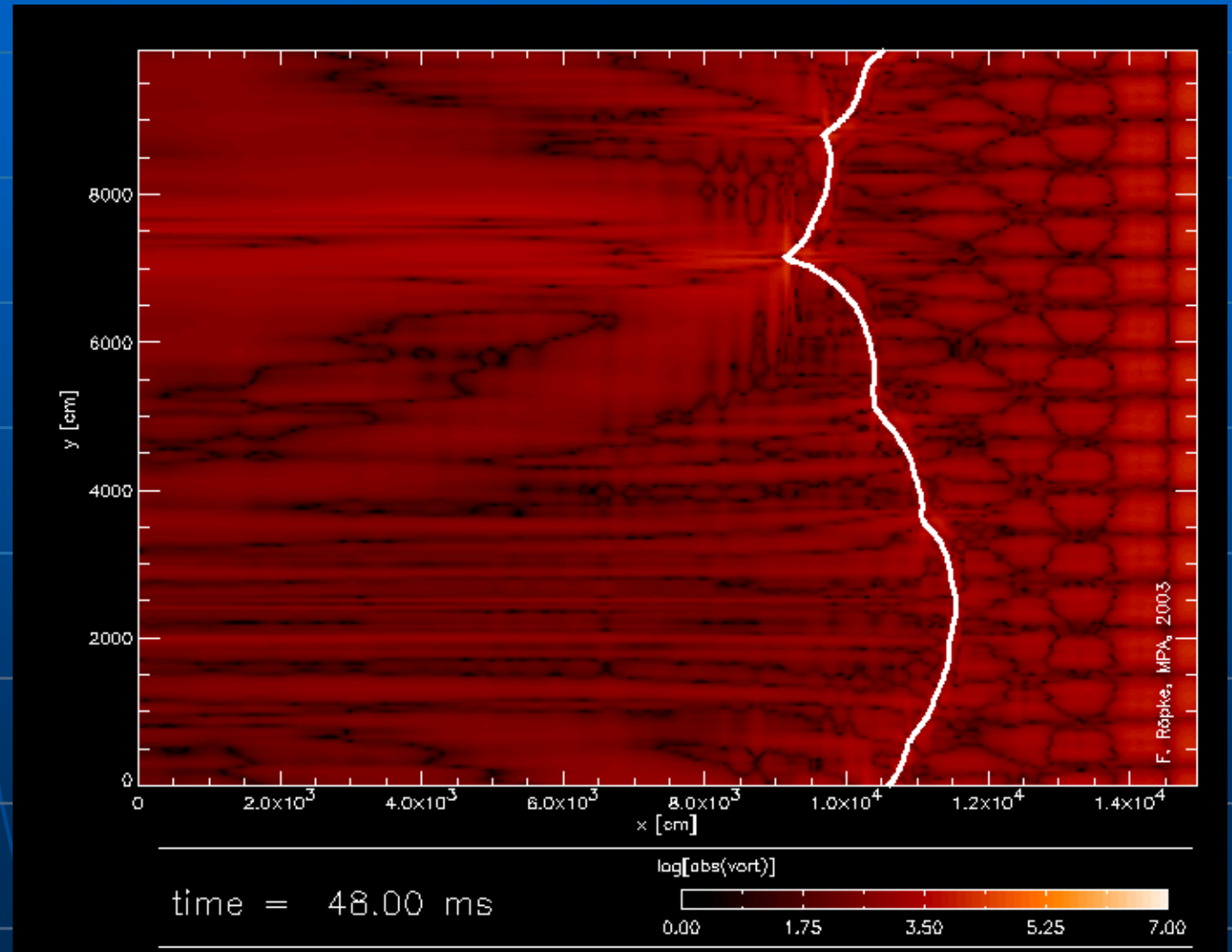




# The Landau-Darrieus instability and its interaction with turbulence:

Weak vortical  
flow

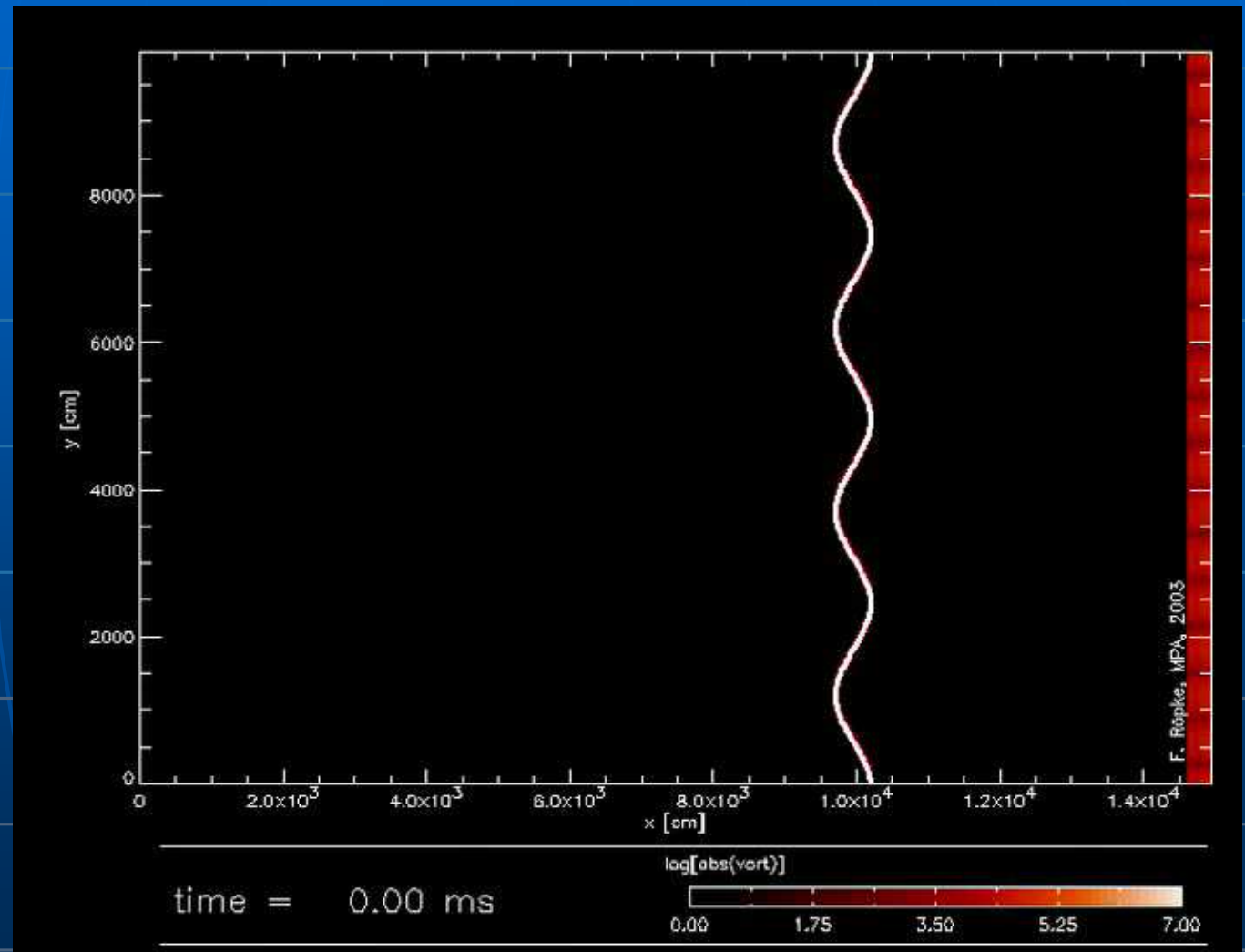
(Röpke et al.,  
2003b)



# *The Landau-Darrieus instability and its interaction with turbulence:*

*Strong vortical flow*

(Röpke et al.,  
2003b)



# Burning regimes of pre-mixed flames

## 2. The corrugated flamelet regime

Transition at the “Gibson scale”:

$$v(l_{\text{Gibs}}) = u_{\text{cell}}(l_{\text{Gibs}})$$

In the limit of strong turbulence:

$$s_{\text{turb}}(l) \approx v'(l), \quad l > l_{\text{Gibs}} \quad (\text{independent of } s_L!!!)$$

$$d_{\text{turb}} \approx l \quad (\text{“turbulent flame brush”})$$

# Fully developed turbulence?

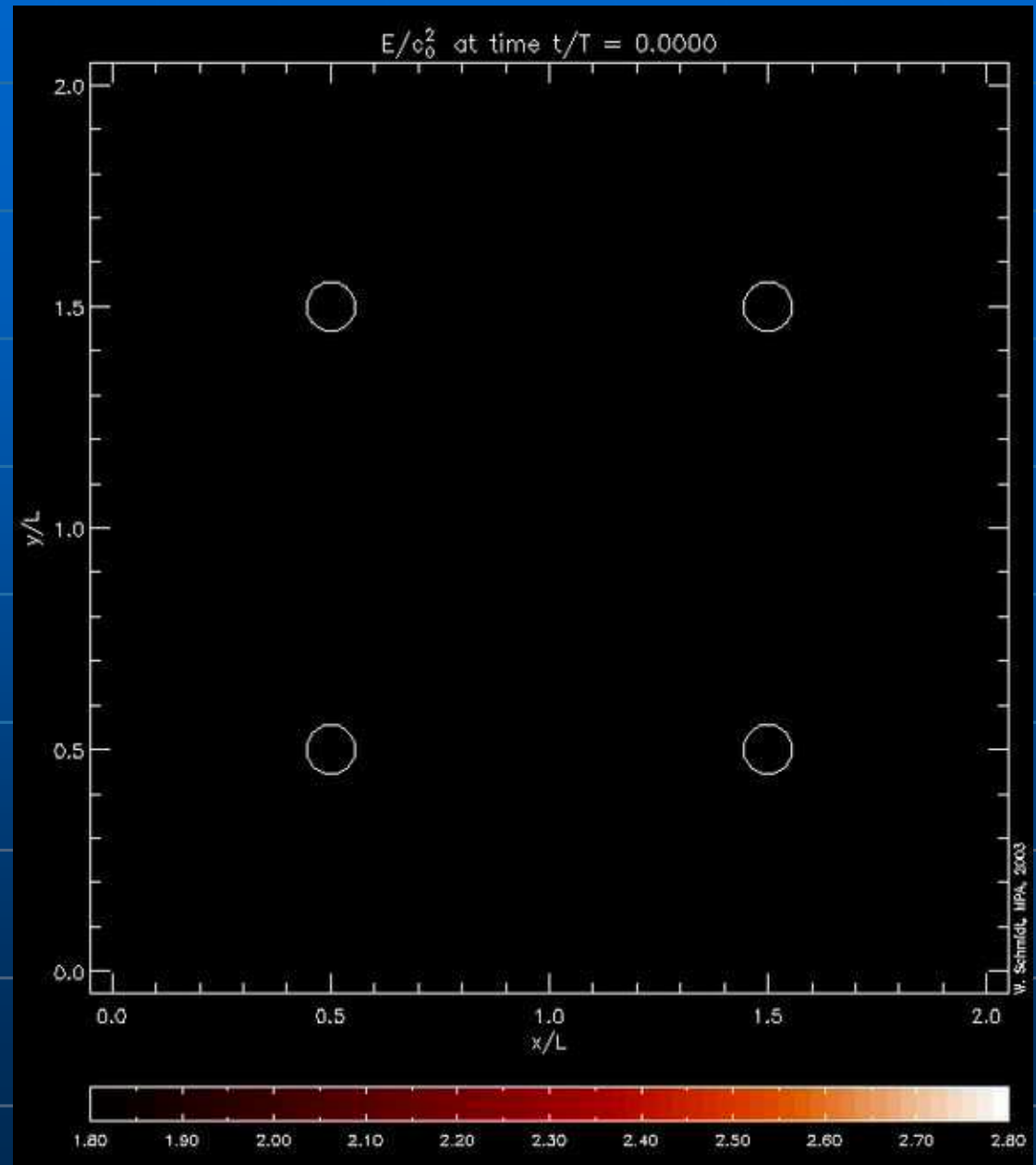
3-D “direct”  
numerical simulations  
of flames moving in  
white dwarf matter:  
*Energy*

$$\rho = 2.9 \cdot 10^9 \text{ g cm}^{-3}$$

$$V/s_{lam} = 4$$

$$V/c_0 = 0.043$$

(Schmidt et al., 2004)



# Fully developed turbulence?

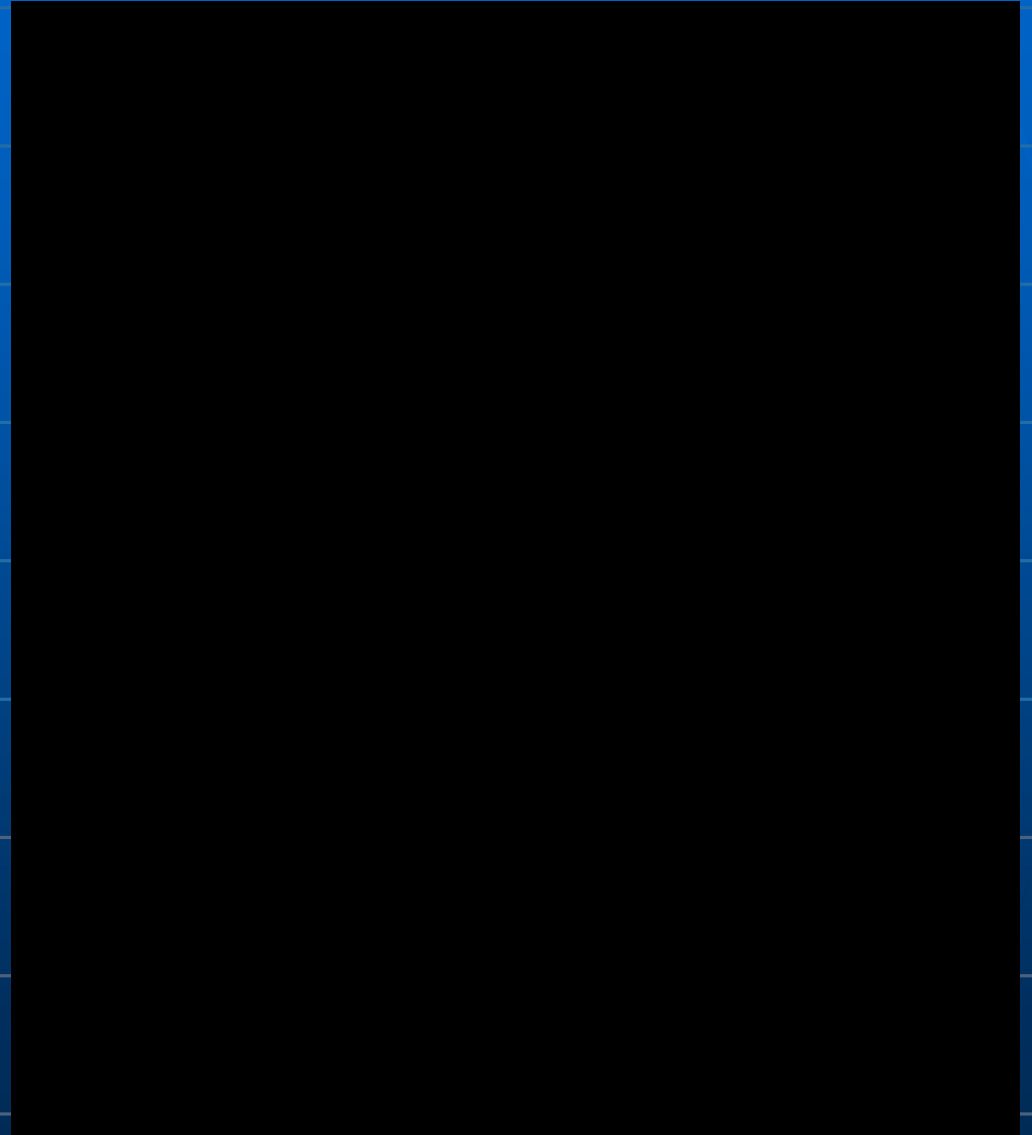
3-D “direct”  
numerical simulations  
of flames moving in  
white dwarf matter:  
*Vorticity*

$$\rho = 2.9 \cdot 10^9 \text{ g cm}^{-3}$$

$$V/s_{lam} = 4$$

$$V/c_0 = 0.043$$

(Schmidt et al., 2004)



# Fully developed turbulence?

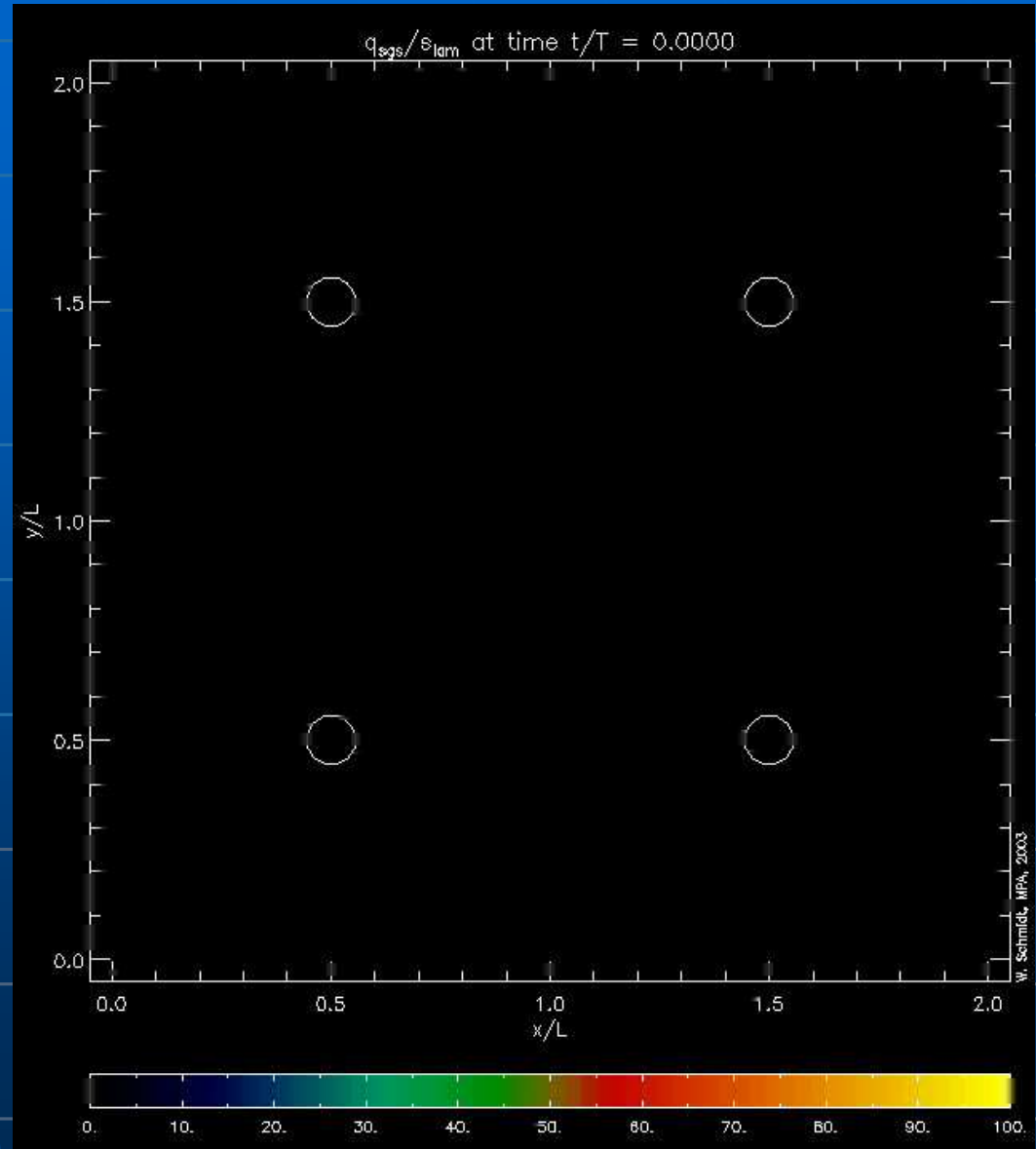
3-D “direct”  
numerical simulations  
of flames moving in  
white dwarf matter:  
*Subgridscale energy*

$$\rho = 2.9 \cdot 10^9 \text{ g cm}^{-3}$$

$$V/s_{lam} = 4$$

$$V/c_0 = 0.043$$

(Schmidt et al., 2004)



# Burning regimes of pre-mixed flames

## 3. The distributed-burning

Turbulent eddies interact with the flame:

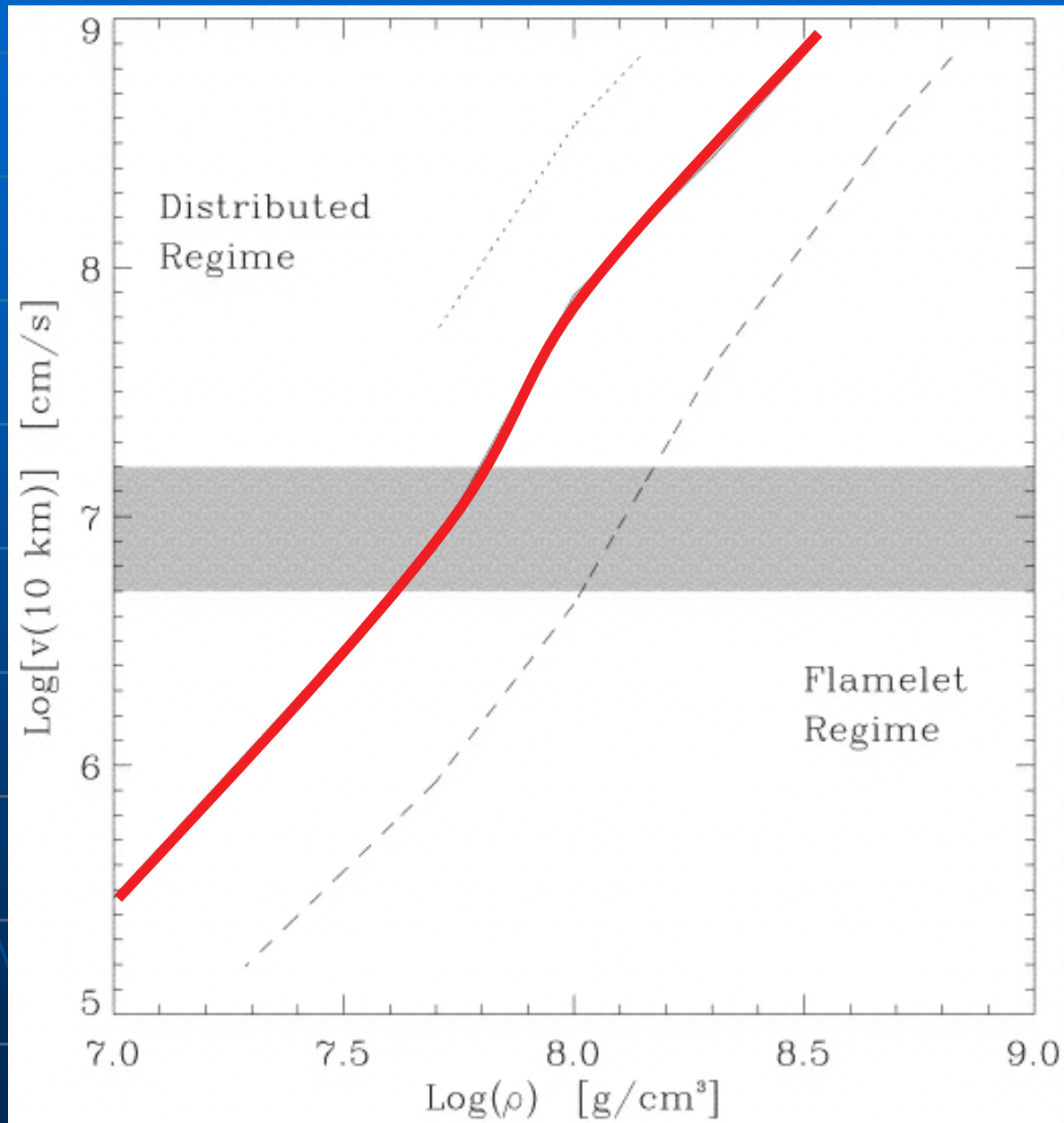
$$l_F \geq l_{\text{Gibs}}$$

Rough estimate (“Damköhler scaling”):

$$s_{\text{turb}}/s_L \approx \text{const} (D_t/D)^{1/2} \text{ (dependent on } s_L \text{ !!!)}$$

$$\text{const} = O(1)$$

# Application to type Ia supernova



Niemeyer &  
Woosley (1997)



# Burning regimes of pre-mixed flames

## 4. The Rayleigh-Taylor regime

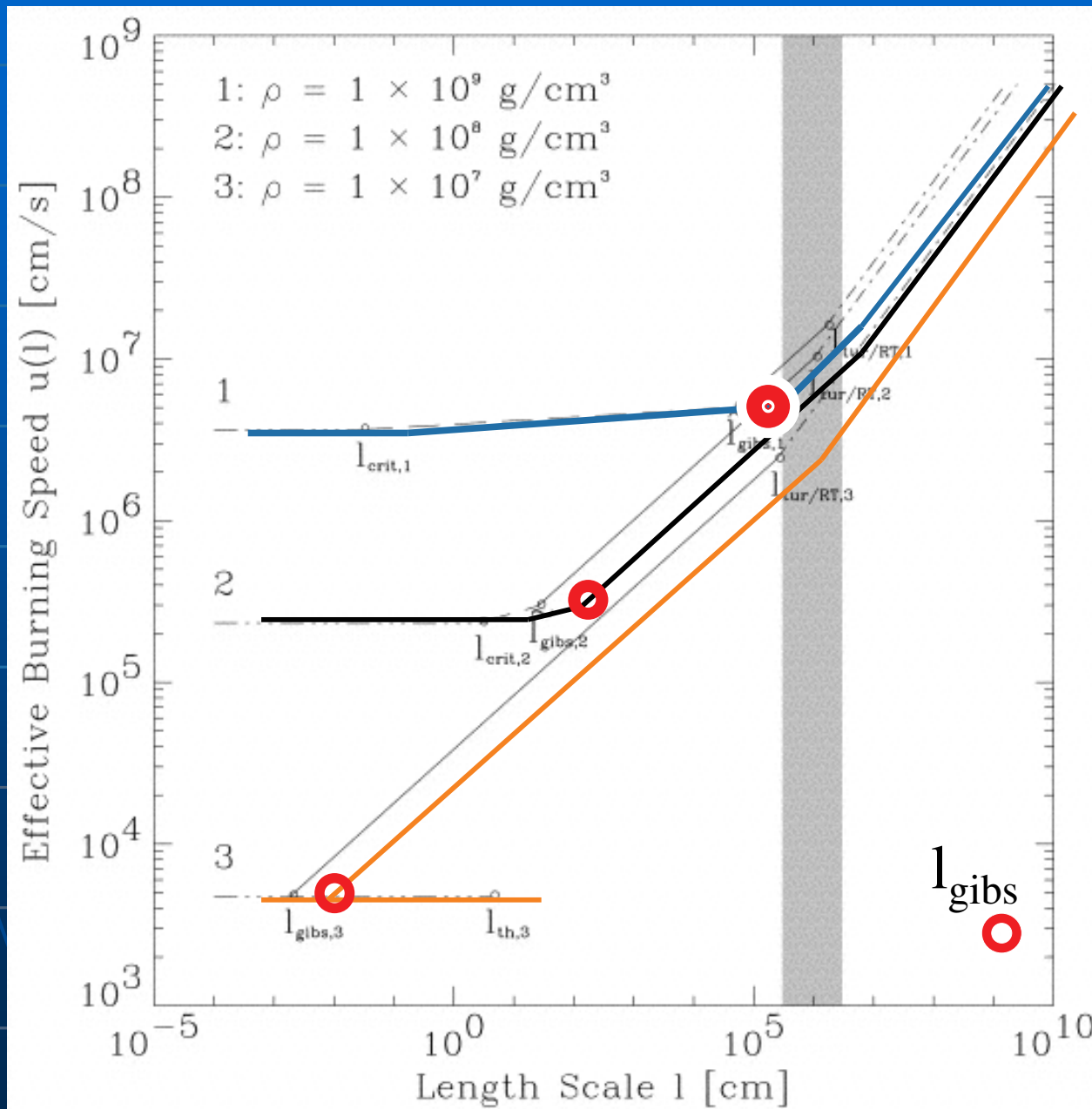
$$v_{RT} = B \sqrt{(g_{eff} l)} ; B \approx 0.5 ; g_{eff} = At \cdot g$$

Sharp-Wheeler model:

$$r_{sw} \approx 0.05 g_{eff} t^2 ; v_{sw} \approx 0.1 g_{eff} t ;$$

$$l_{tur/RT} \approx 10^6 \text{ cm}$$

# Effective burning velocities in SN Ia



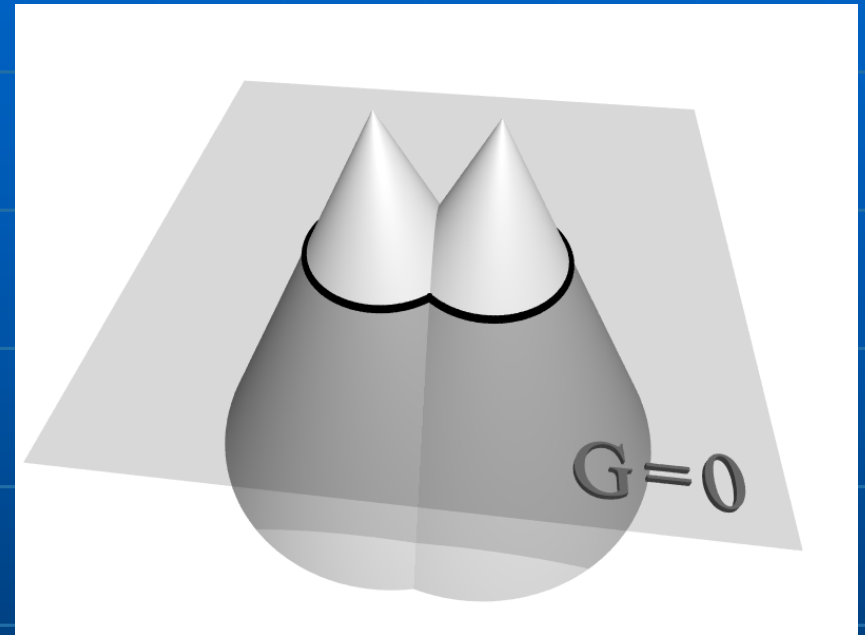
Niemeyer &  
Woosley  
(1997)

# How to model thermonuclear flames?

- q The "flames" cannot be resolved numerically.
- q The amplitudes of turbulent velocity fluctuations in the length scale of the flame are determined on the integral scale.



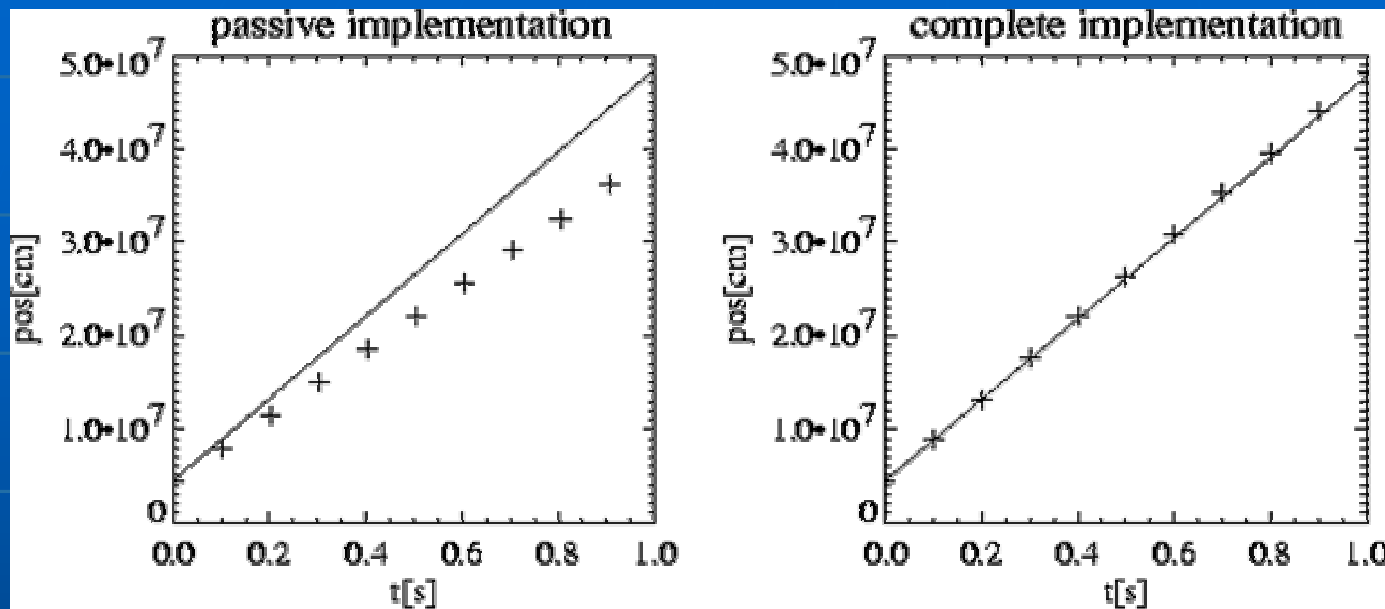
*"LES" + "Level Set"*



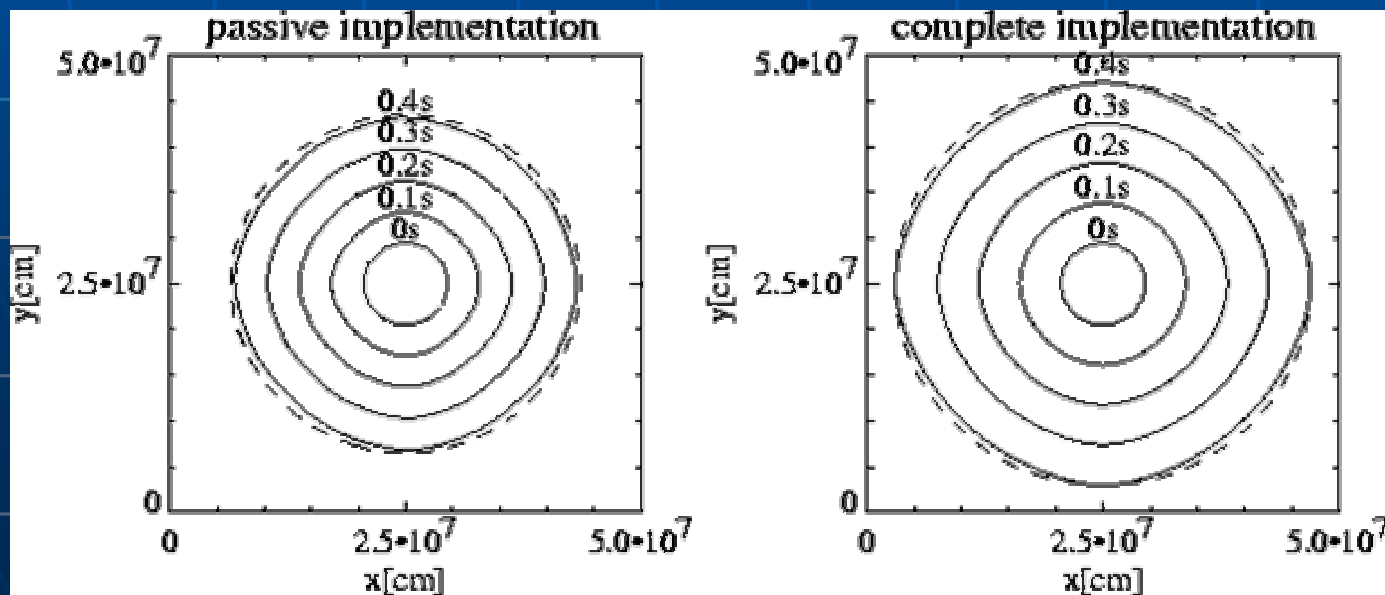
$$\partial G / \partial t = -\mathcal{D}_f \nabla G$$

$$\mathcal{D}_f = \mathbf{v}_u + s_{\text{tur}} \mathbf{n}; \quad |\nabla G| = 1$$

# Some test of the code



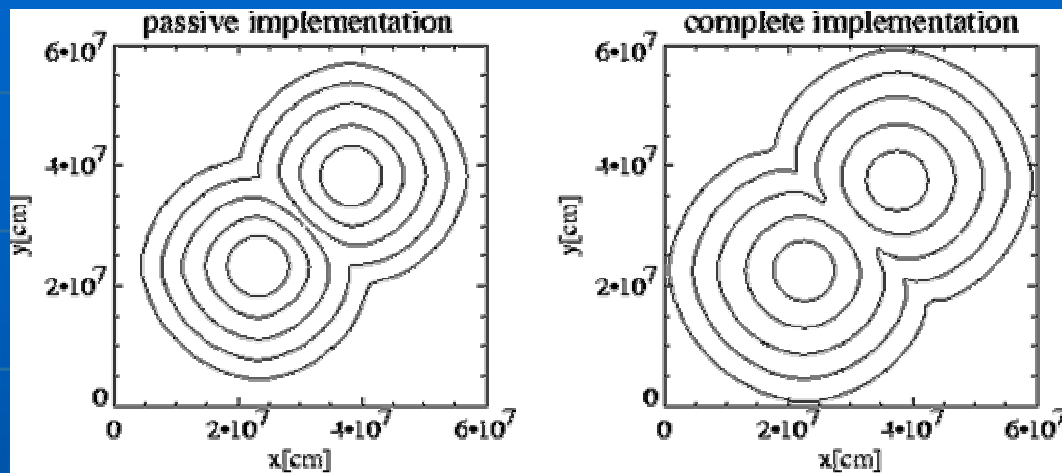
Planar flame



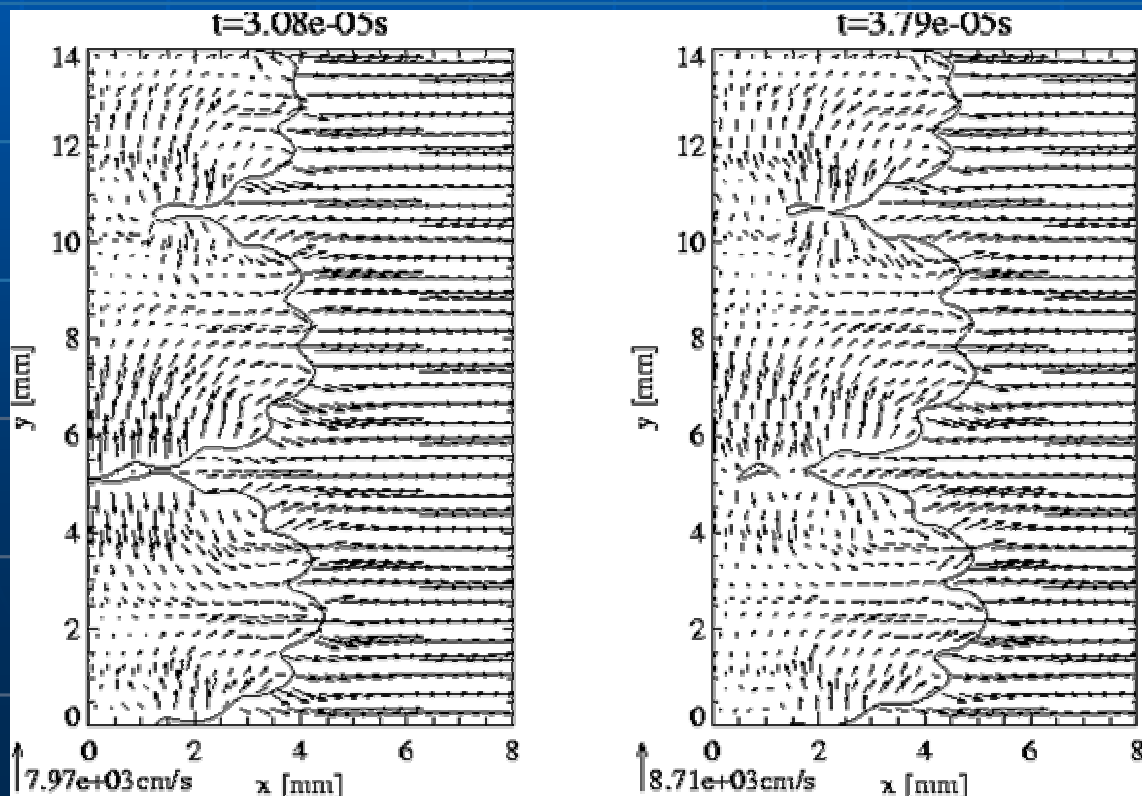
Circular flame

Reinecke et al.  
(1999)

# Some test of the code (ctn.)



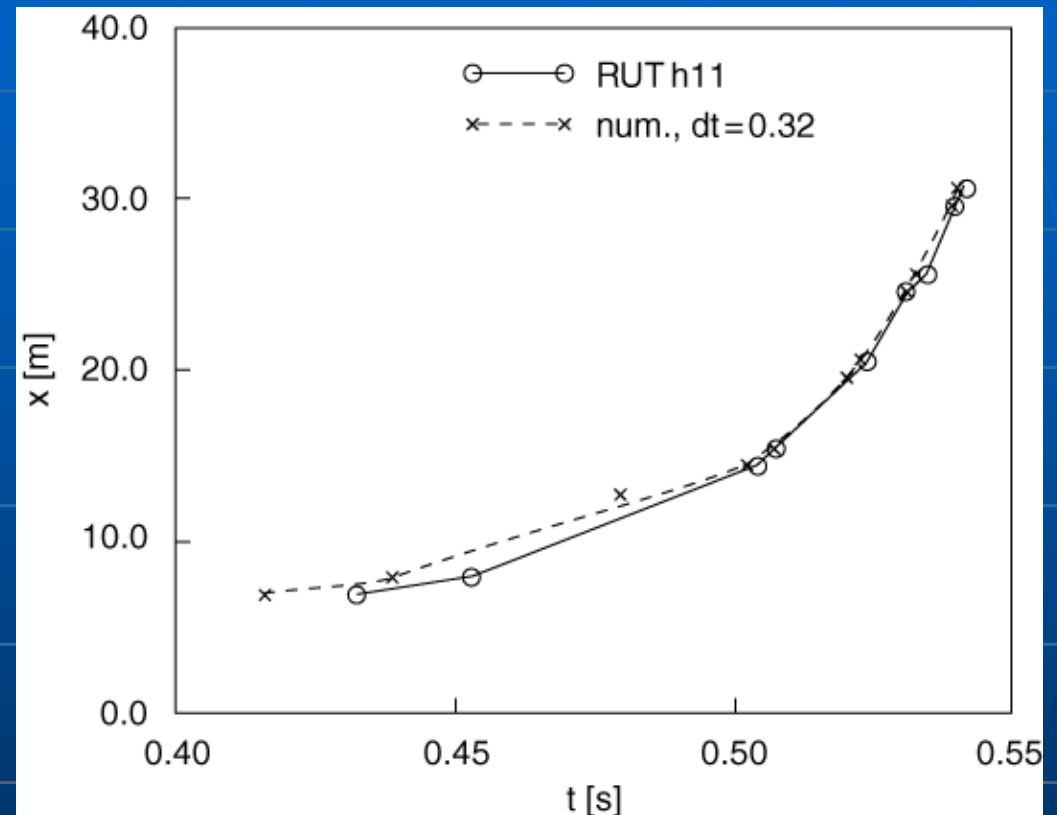
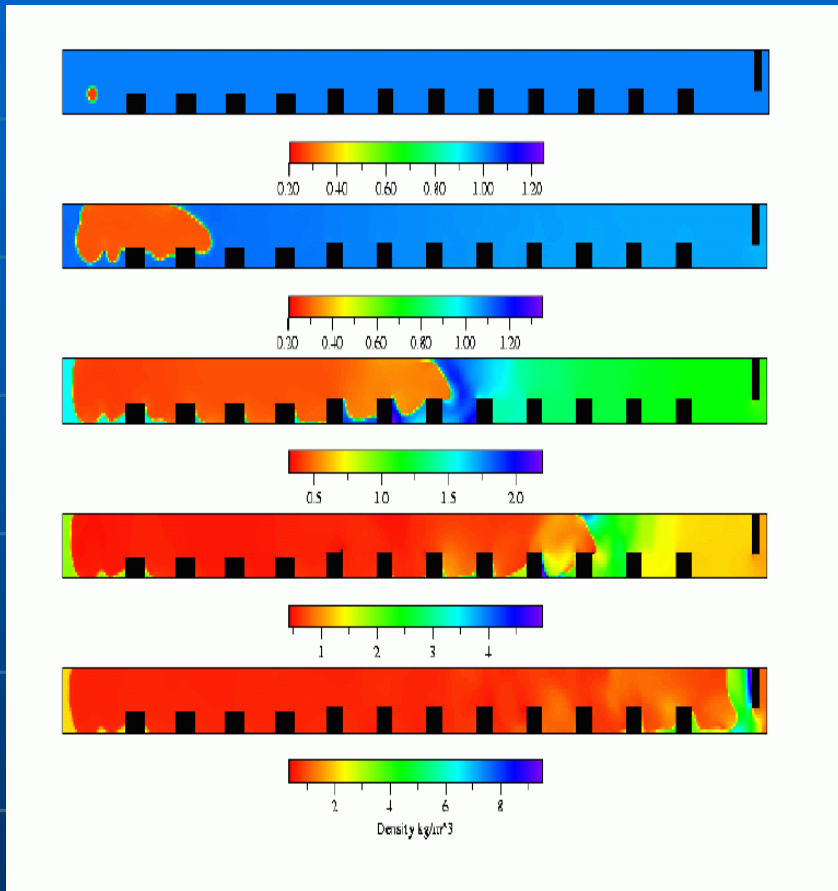
Merging circular flames



Hydrogen-in-air flames

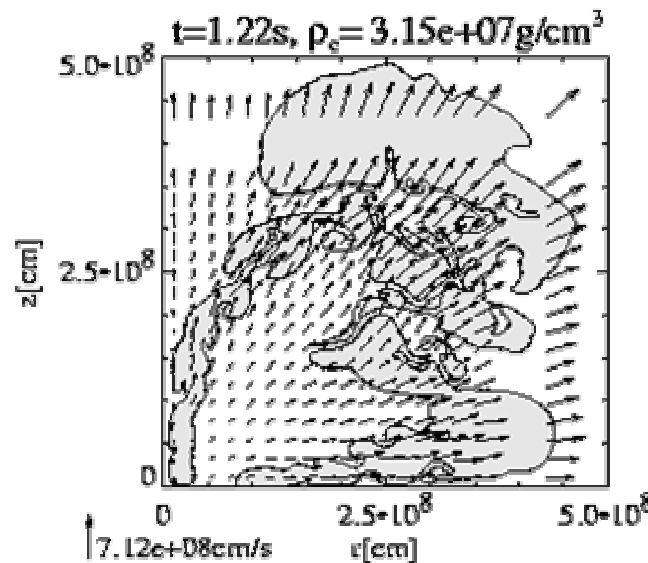
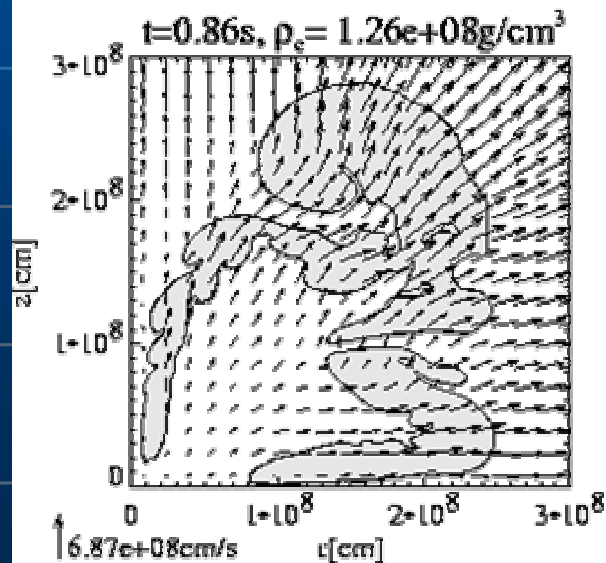
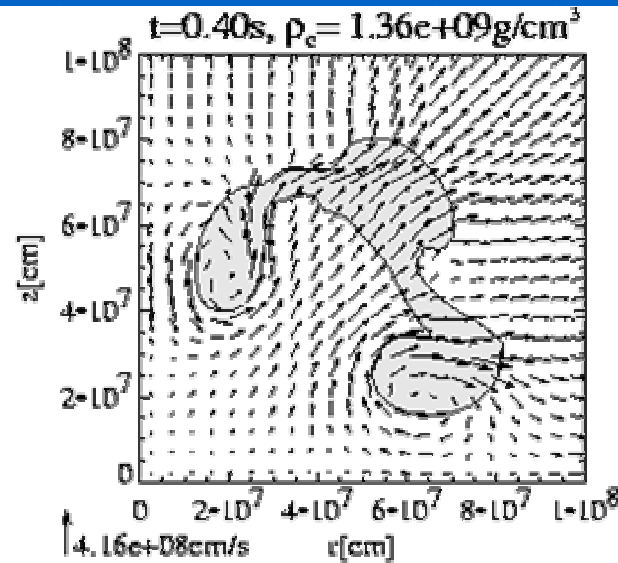
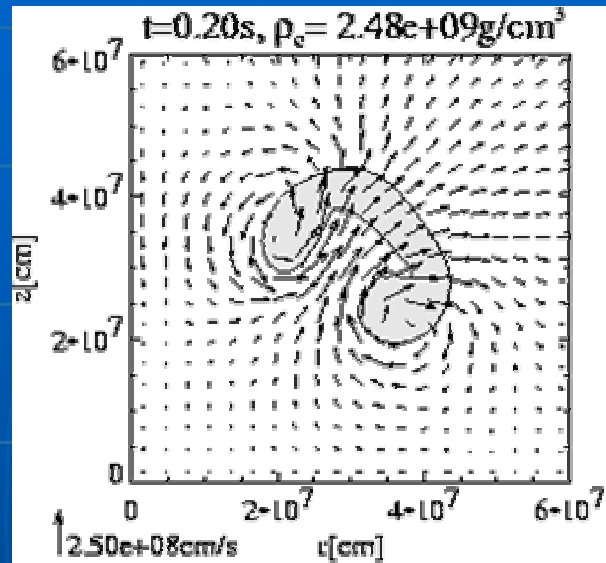
Reinecke et al. (1999)

# Other laboratory flames



The method can reproduce terrestrial experiments well!  
(Smiljanowski et al. 1997)

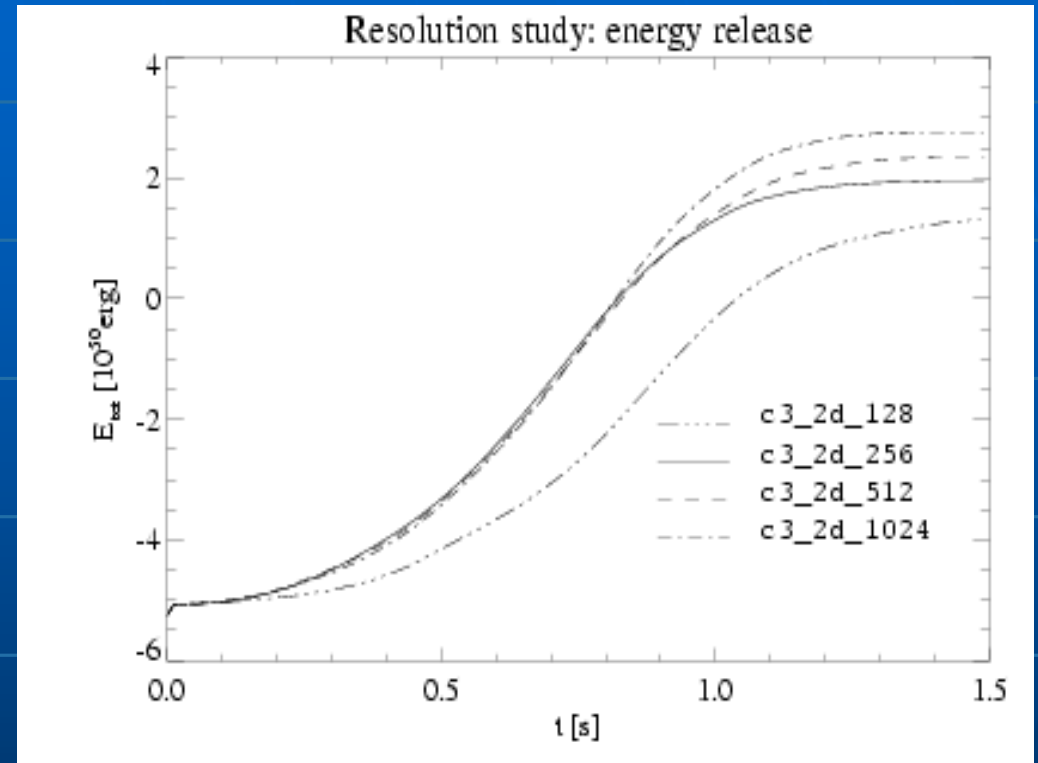
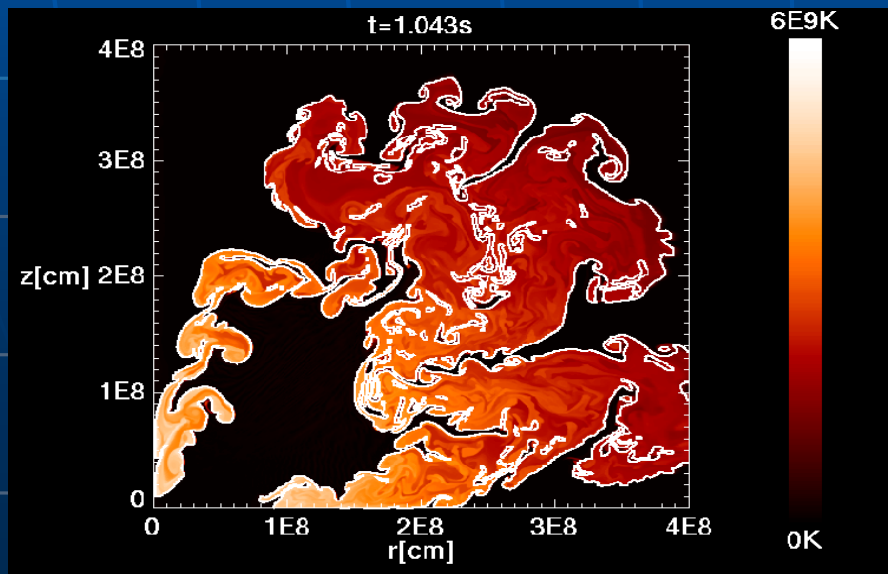
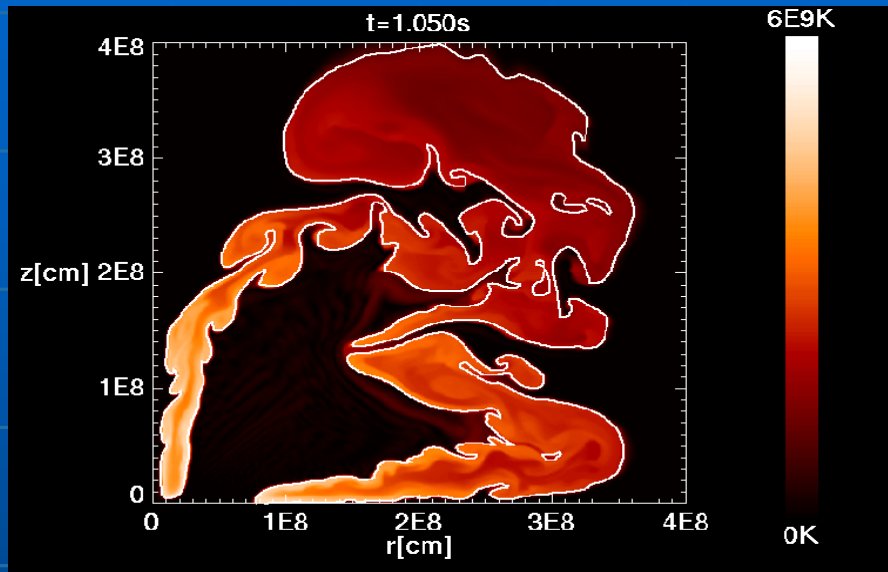
# Application to the SN Ia problem



One rising  
blob (in 2D)

Reinecke et al.  
(1997)

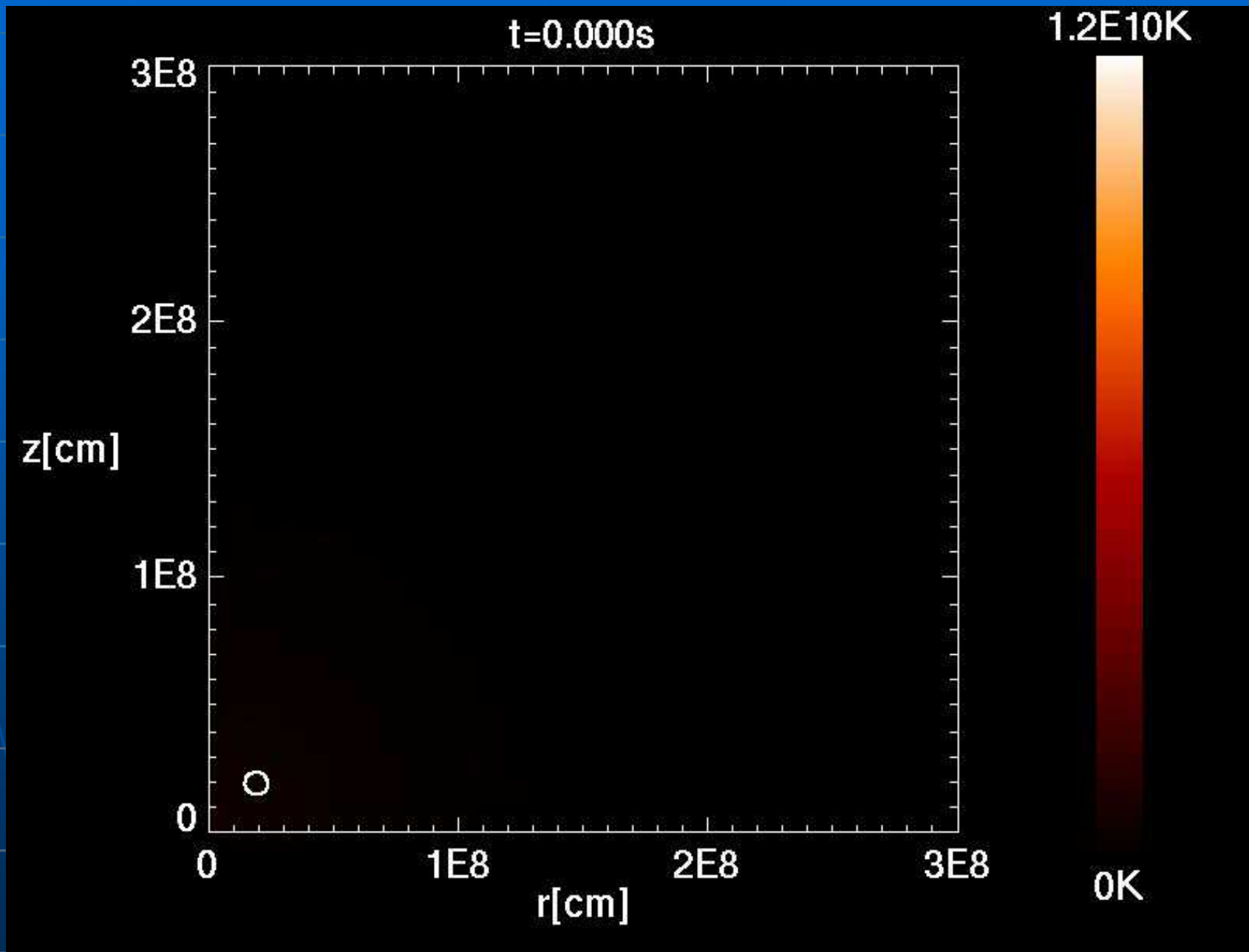
# Convergence tests in 2D



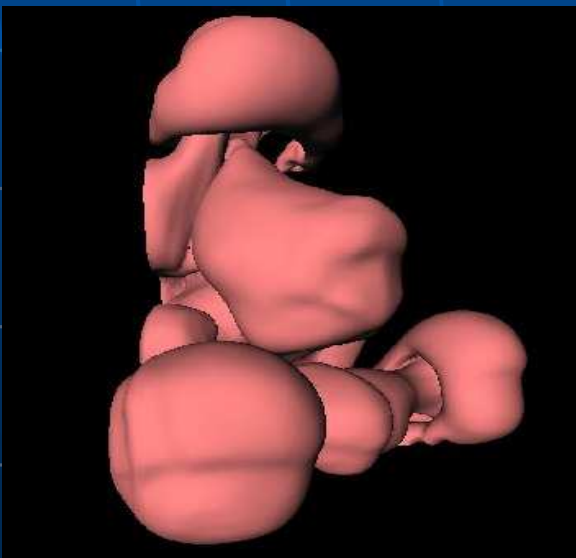
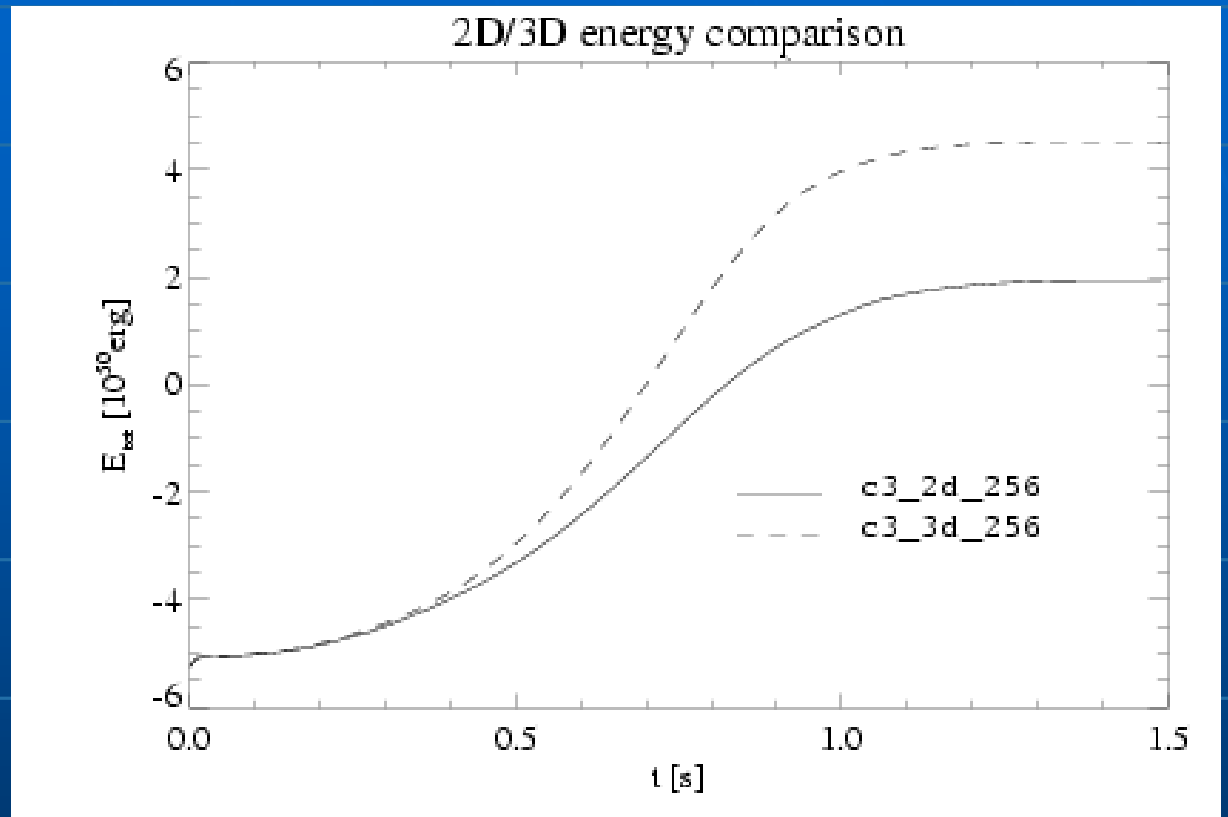
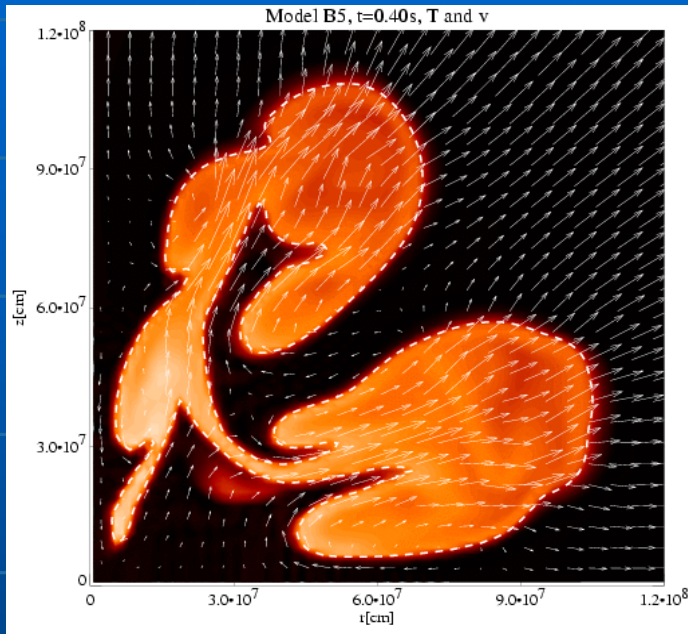
Global results are independent of the numerical resolution!

Reinecke et al. (1999, 2002)





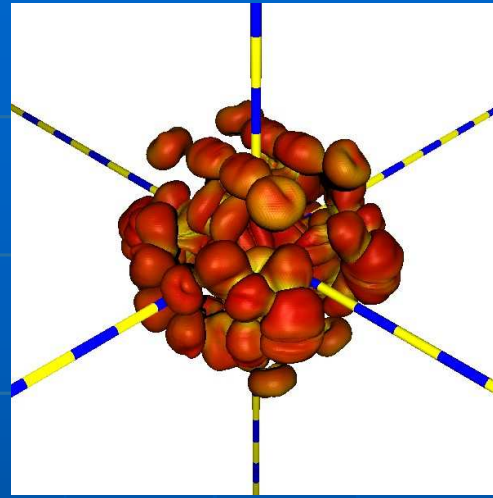
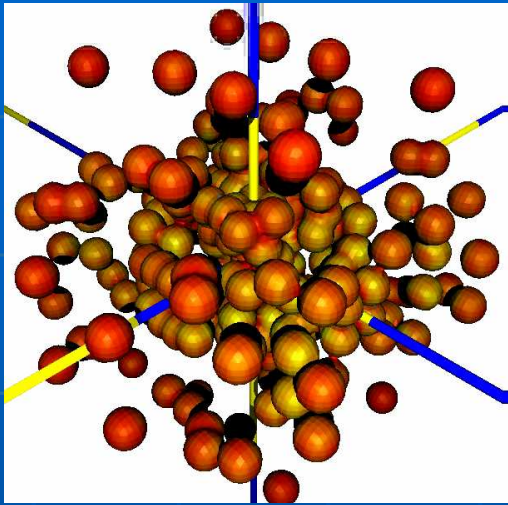
# 2D $\Rightarrow$ 3D



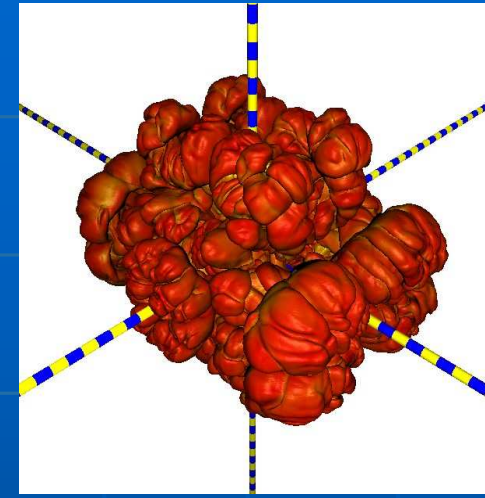
Because of larger surface area:  
More energy is produced!

Reinecke et al. (2001)  
(See also Gamezo et al., 2003)

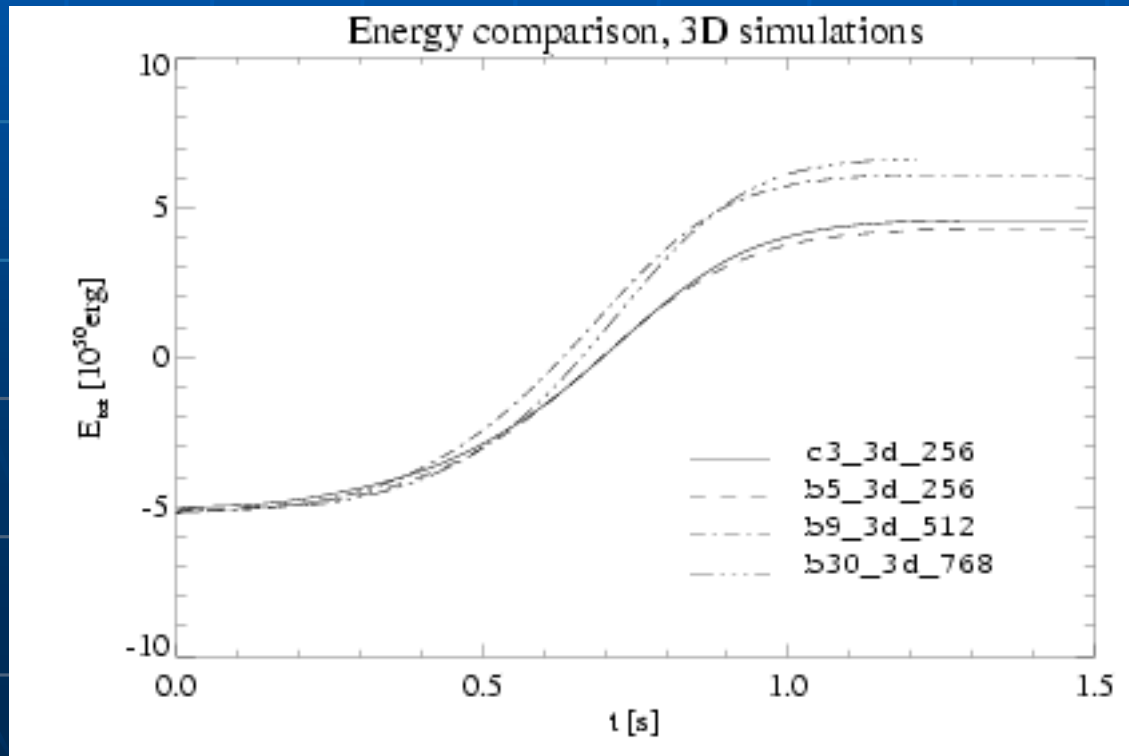
# 3D models: The best we could do until now!



0.25s



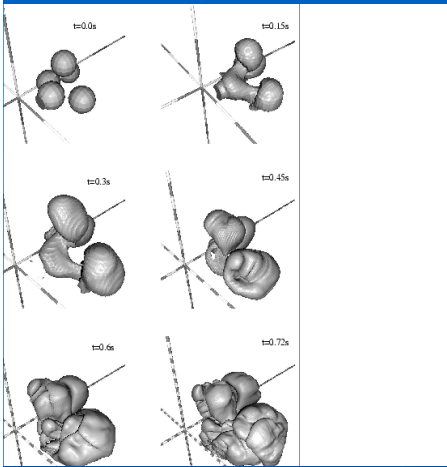
0.6s



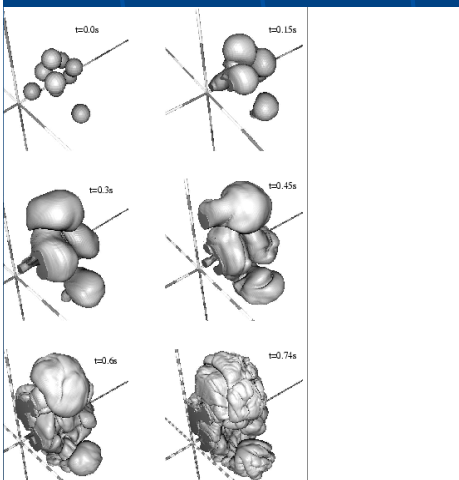
Mod b30\_3d

(Reinecke et al., 2003)

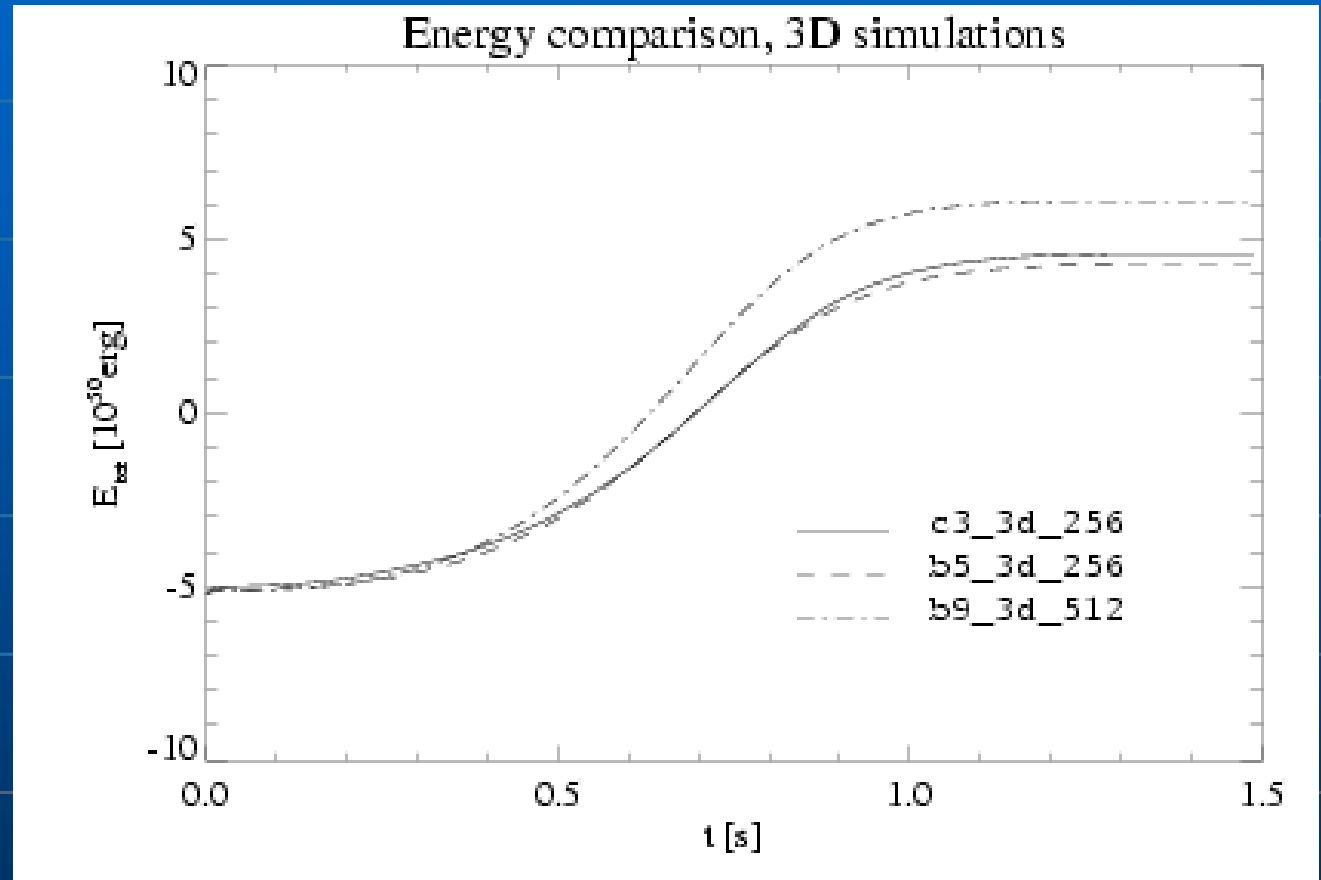
# Modeling Flames in 3D: Dependence on initial conditions?



Mod.  
b5\_3d



Mod.  
b9\_3d



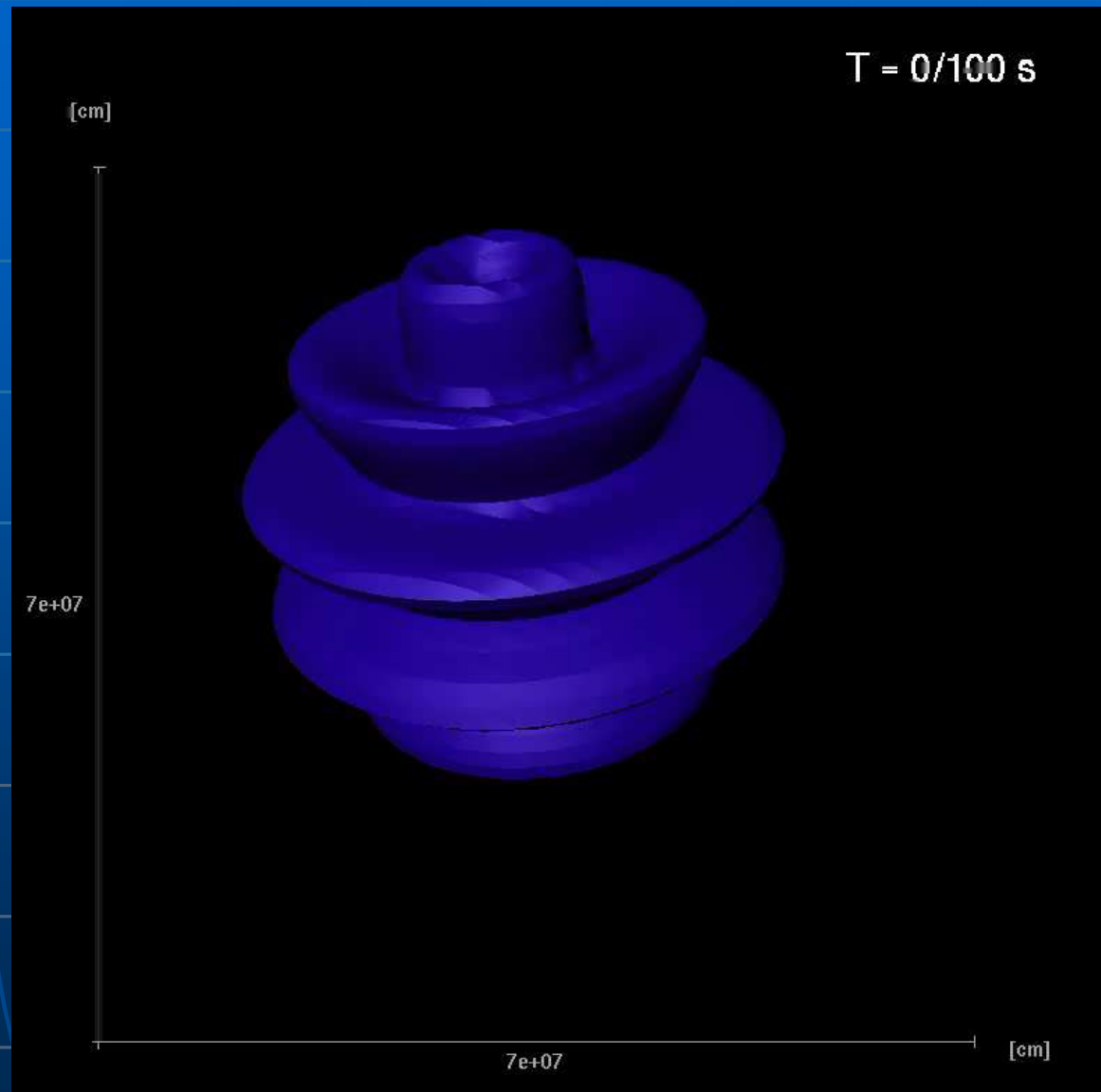
Moderate dependence  
on initial conditions!

(Reinecke et al., 2002)

# Recent modifications of the code:

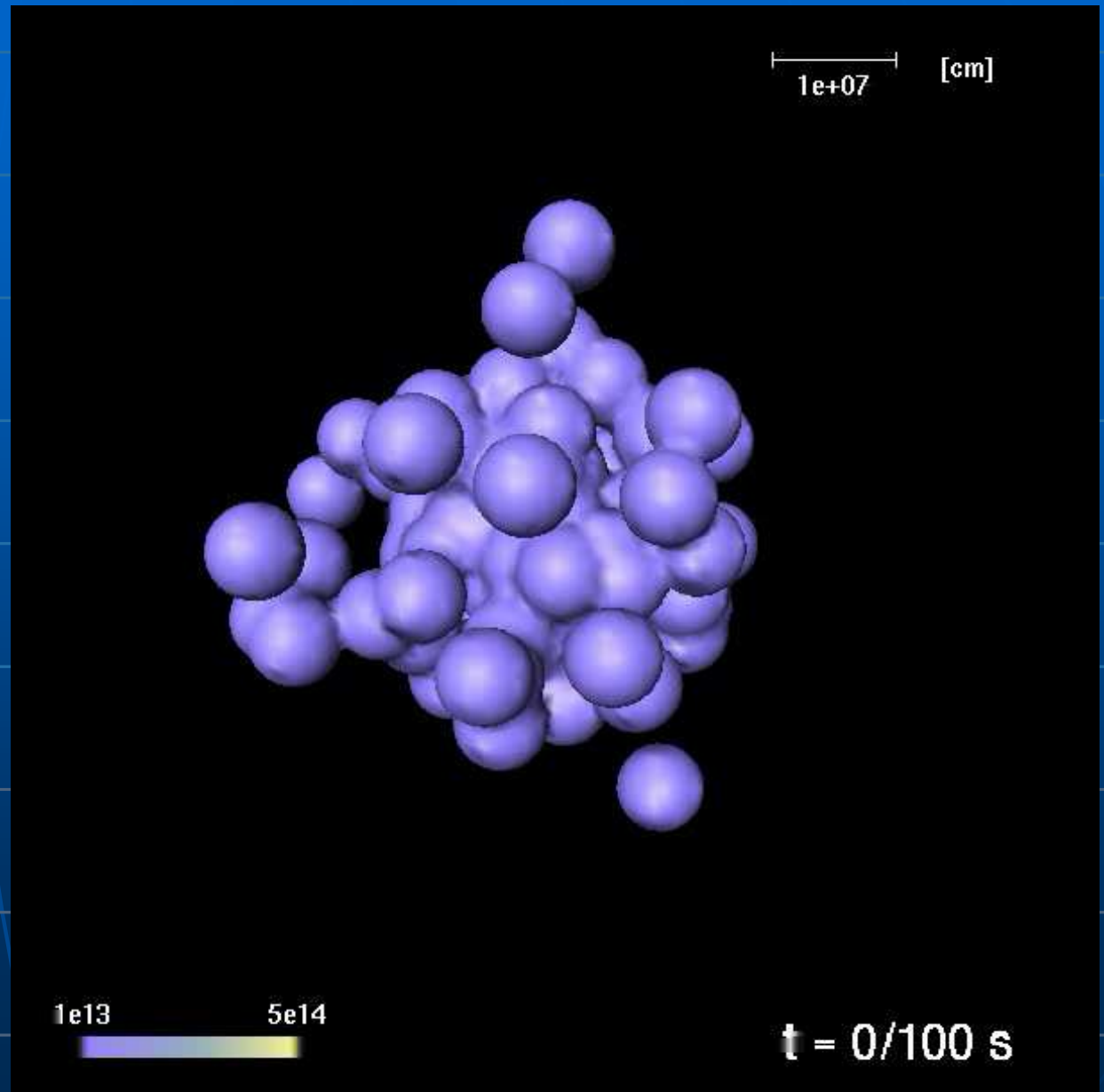
## 1. Moving grid

Röpke (2004)



## 2. Full star (“ $4\pi$ ”)

Röpke & Hillebrandt  
(2004)



# Some open questions and challenges

## q Ignition conditions:

How do WDs reach  $M_{\text{Ch}}$ ? Center/off-center ignition? One/multiple “points”?

## q Combustion modeling:

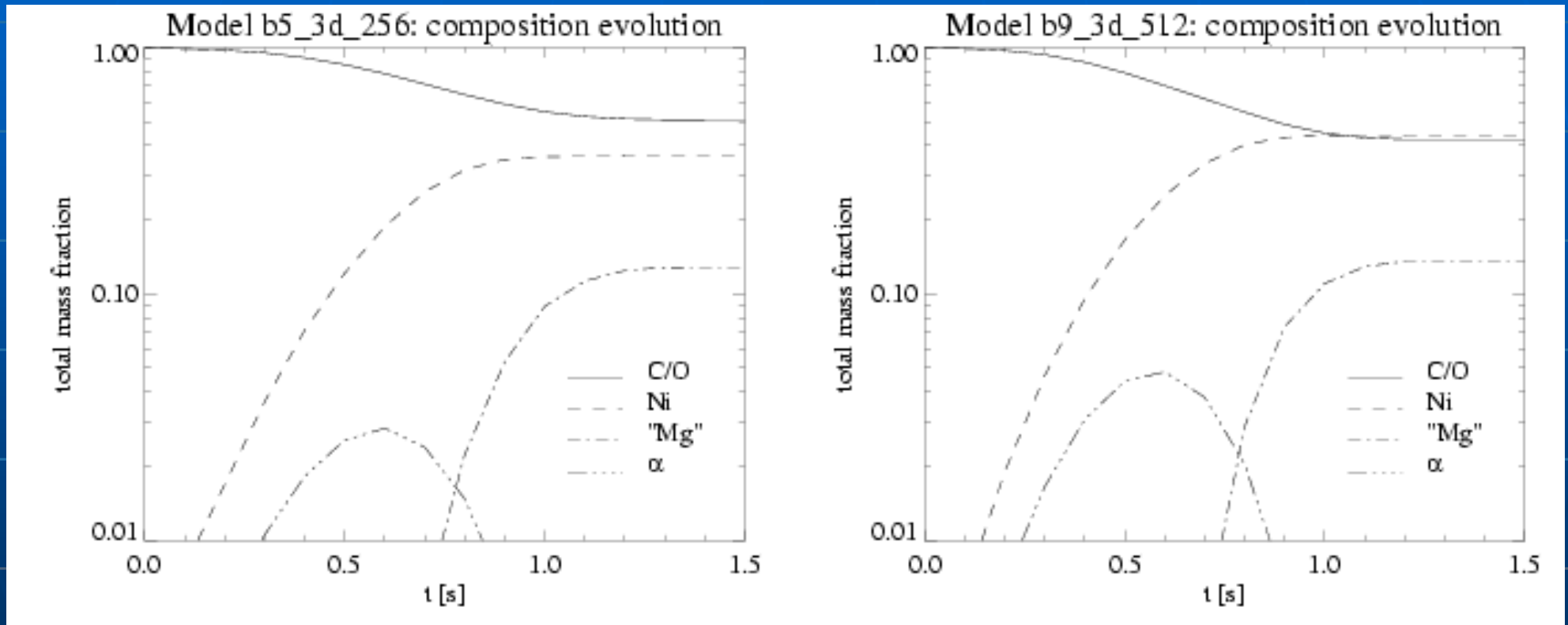
Sub-grid scale models? Interaction of nuclear flames with turbulence; “distributed burning”; “active turbulent combustion”?

Deflagration/detonation transition?

## q ”Full-star” models:

Composition? Rotation? Light curves? Spectra?

# Observable Predictions: Chemical composition?

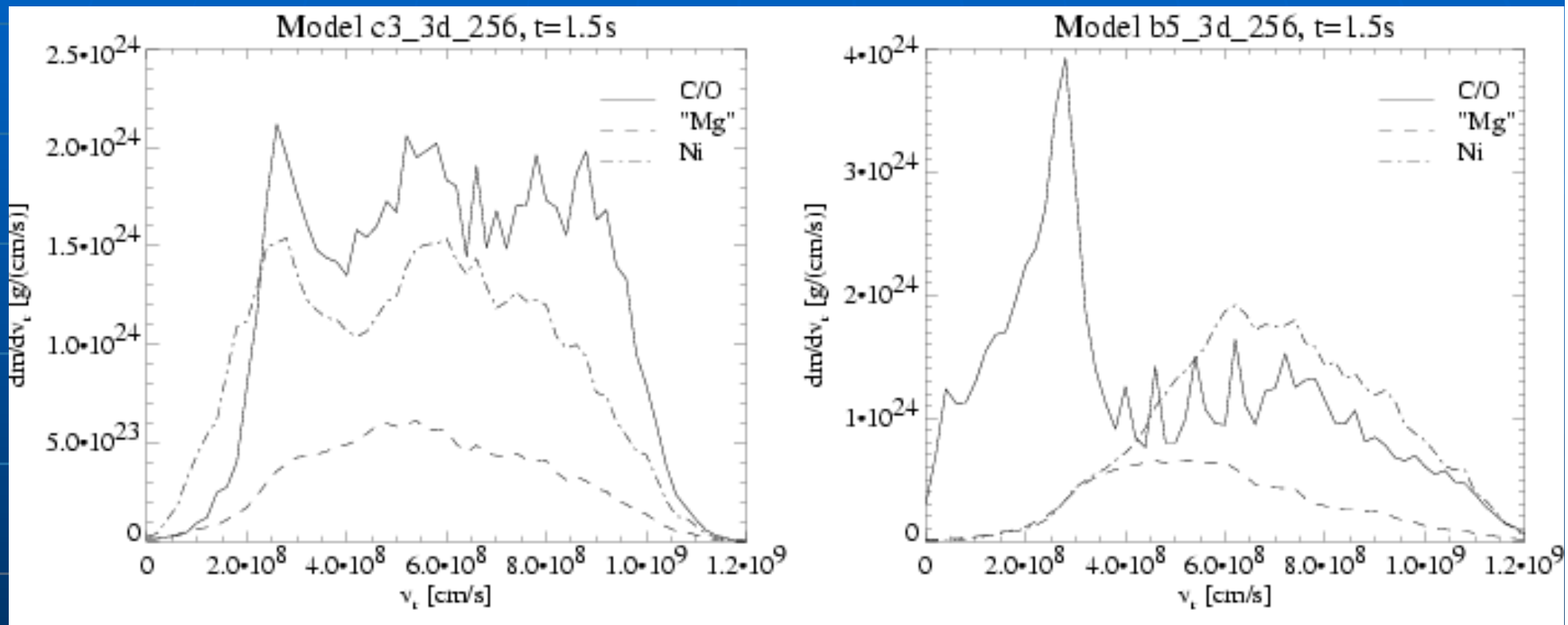


Significant amounts of unburned C and O!

(Reinecke et al., 2002)



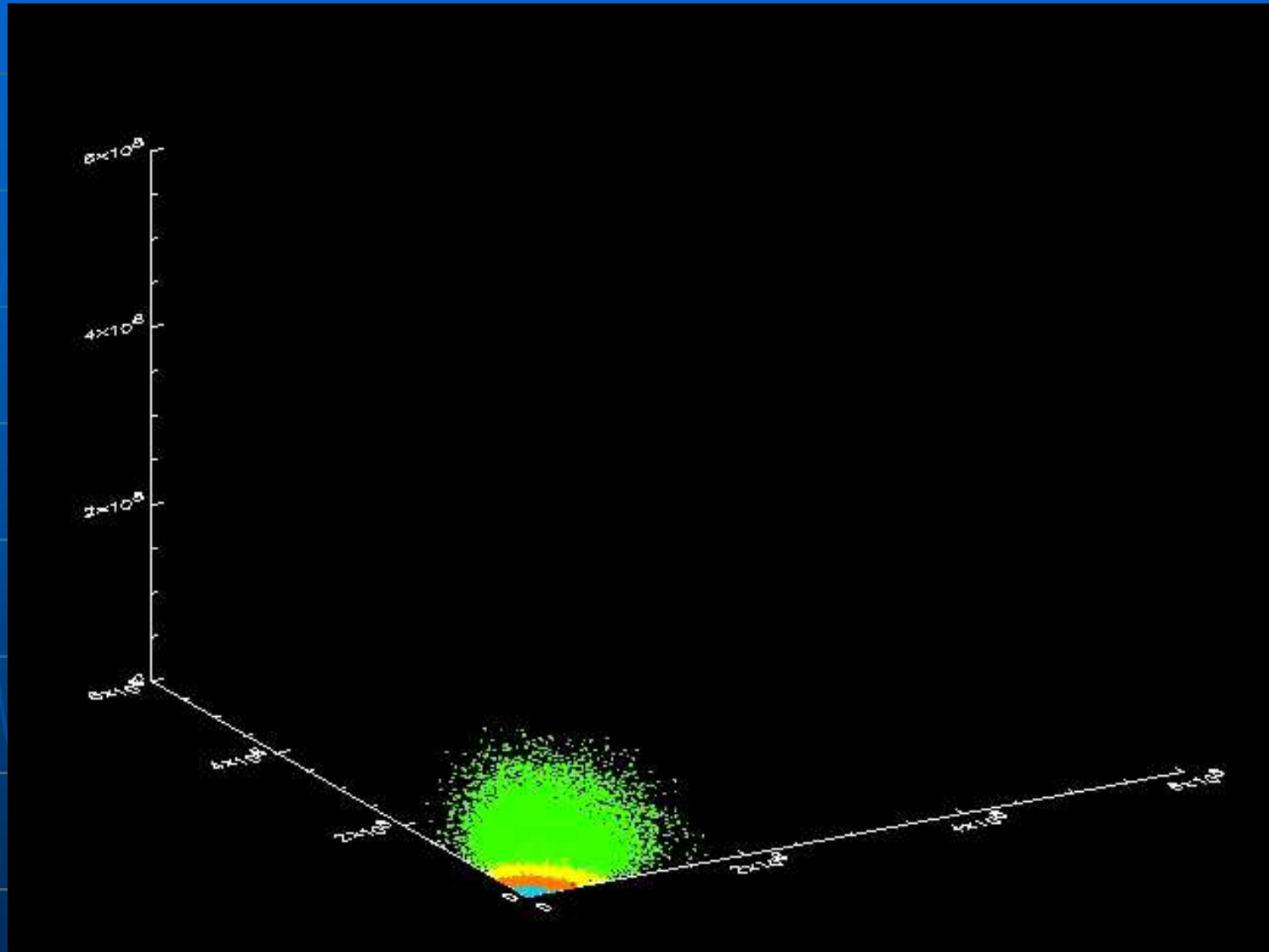
# Observable Predictions: Chemical composition in velocity space?



Velocity distribution sensitive to ignition conditions!

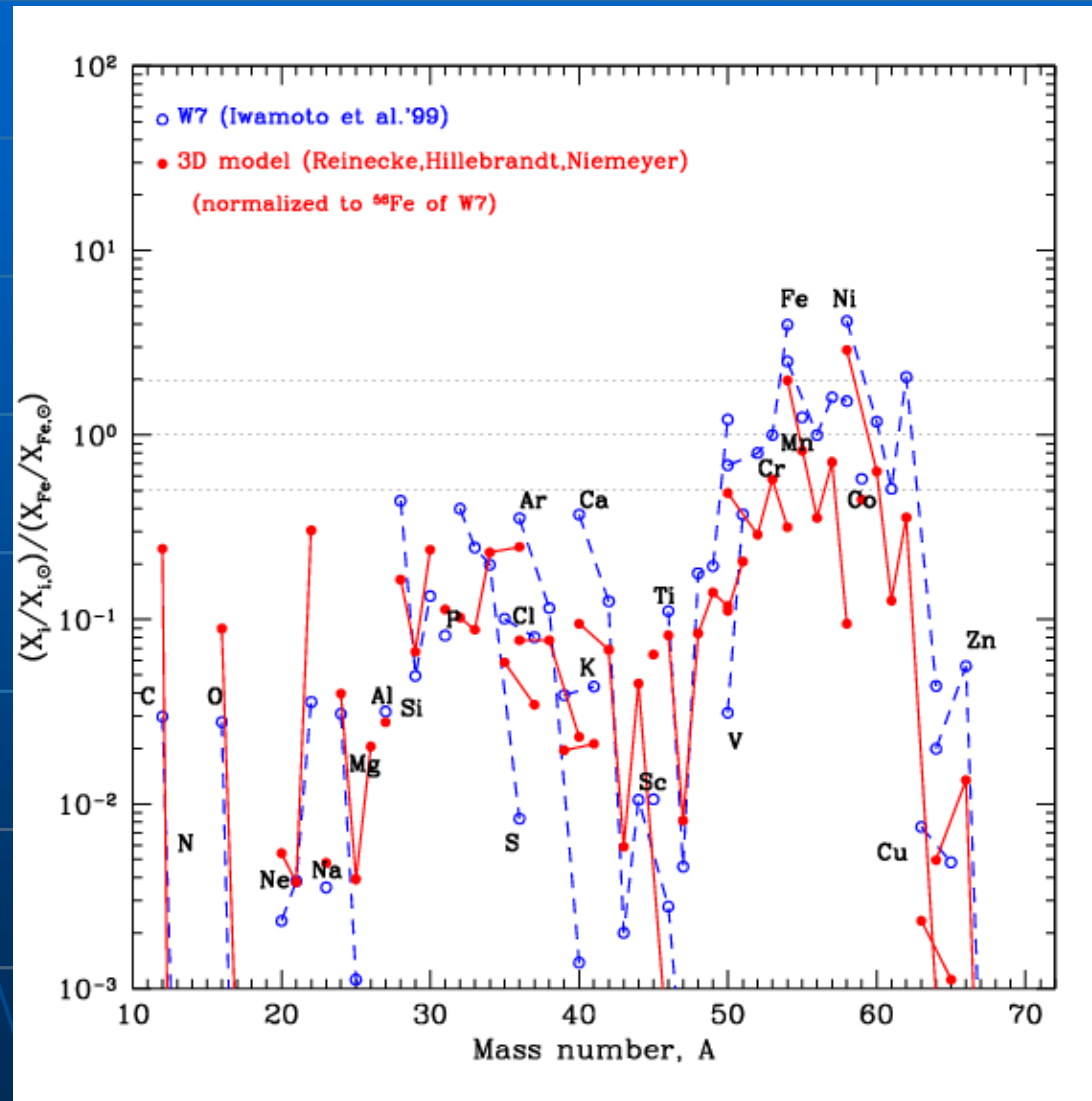
(Reinecke et al., 2002)

# Nucleosynthesis (in ‘post-processing’ mode)



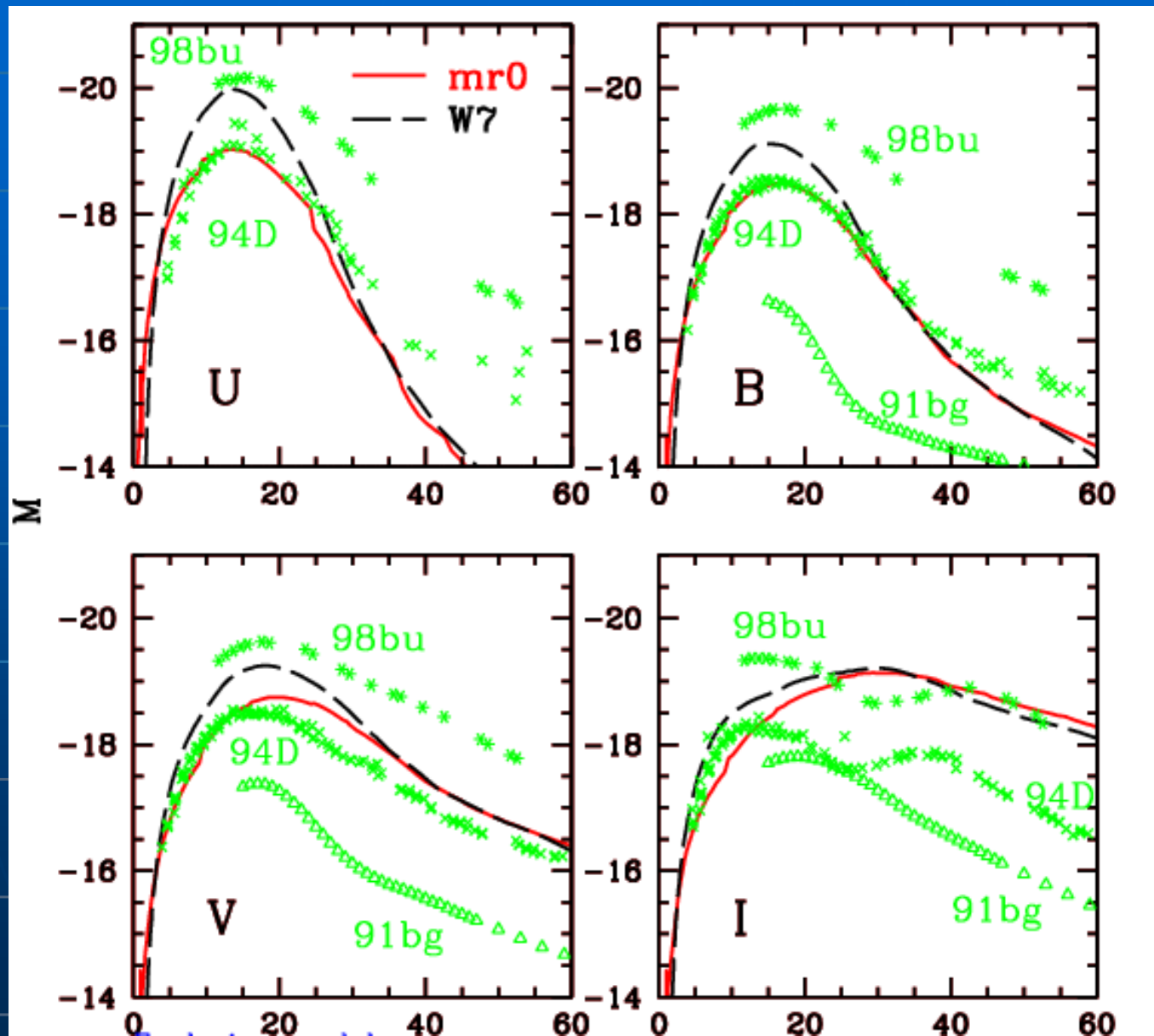
(Travaglio et al., 2004)

# Chemical composition: What is different from W7?



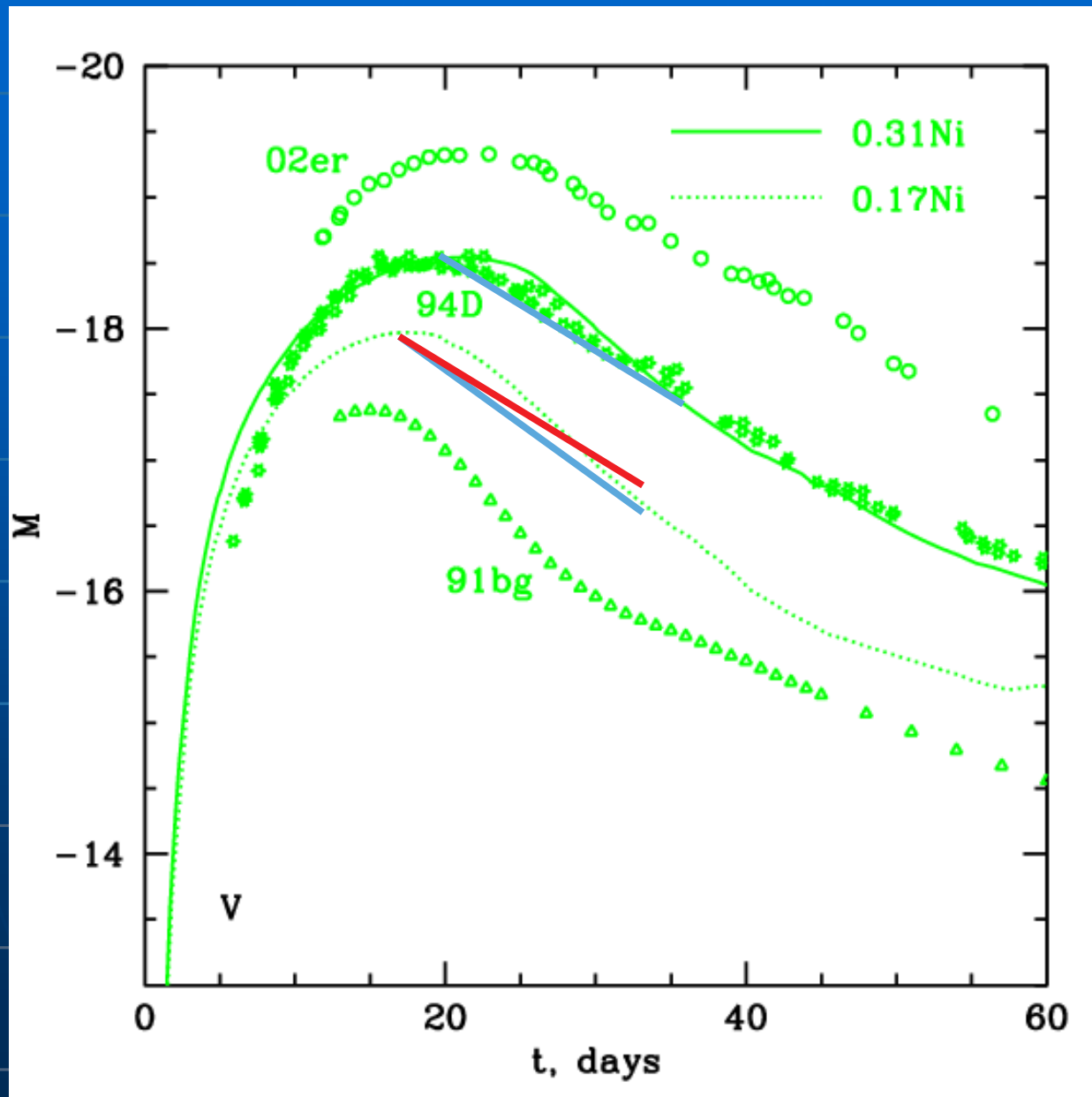
(Off-center ignited 3D model, Travaglio et al., 2003)

## Colour light curves .....



Sorokina &  
Blinnikov  
(2002)

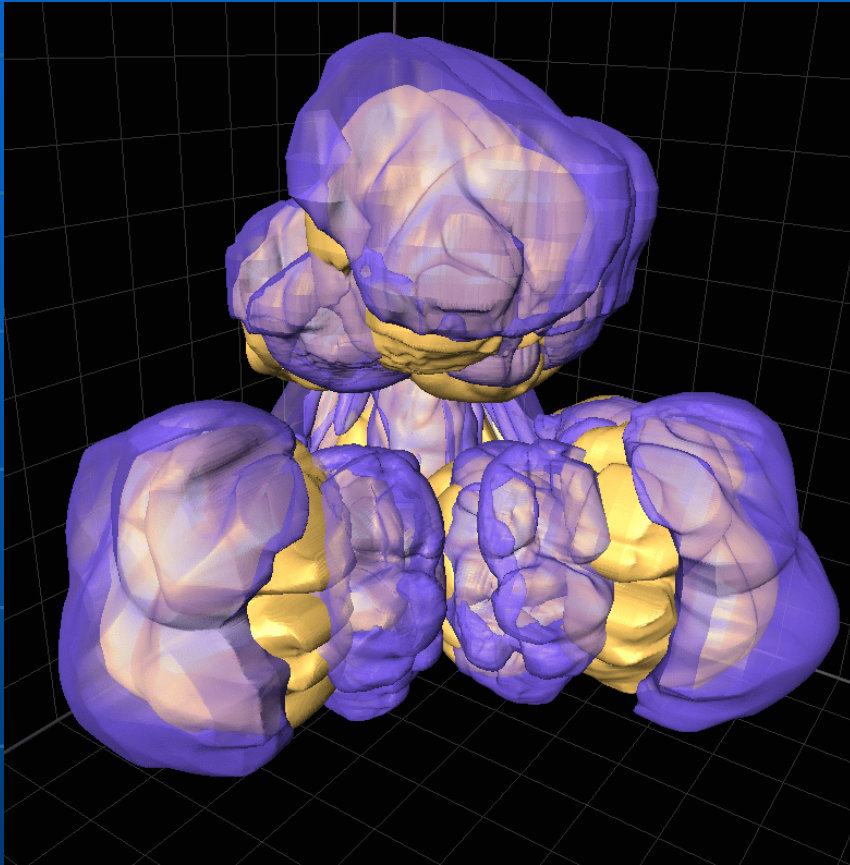
... and model *predictions*.



Prediction from  
Theory :

Light-curve shape  
/ luminosity  
correlation?

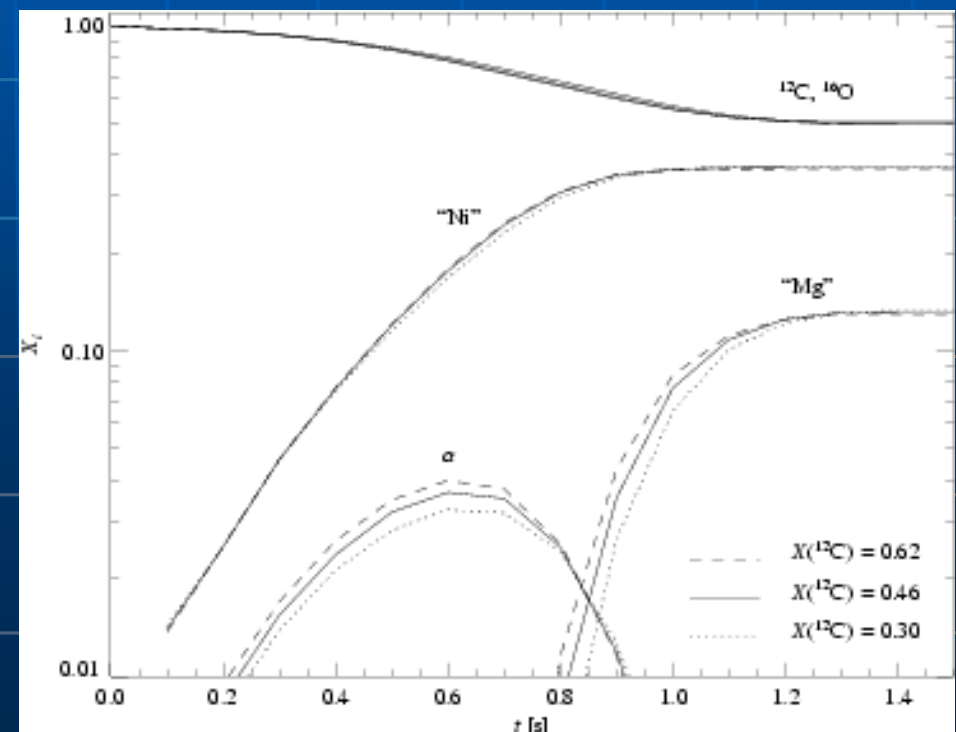
# Dependence on the initial C/O ratio?

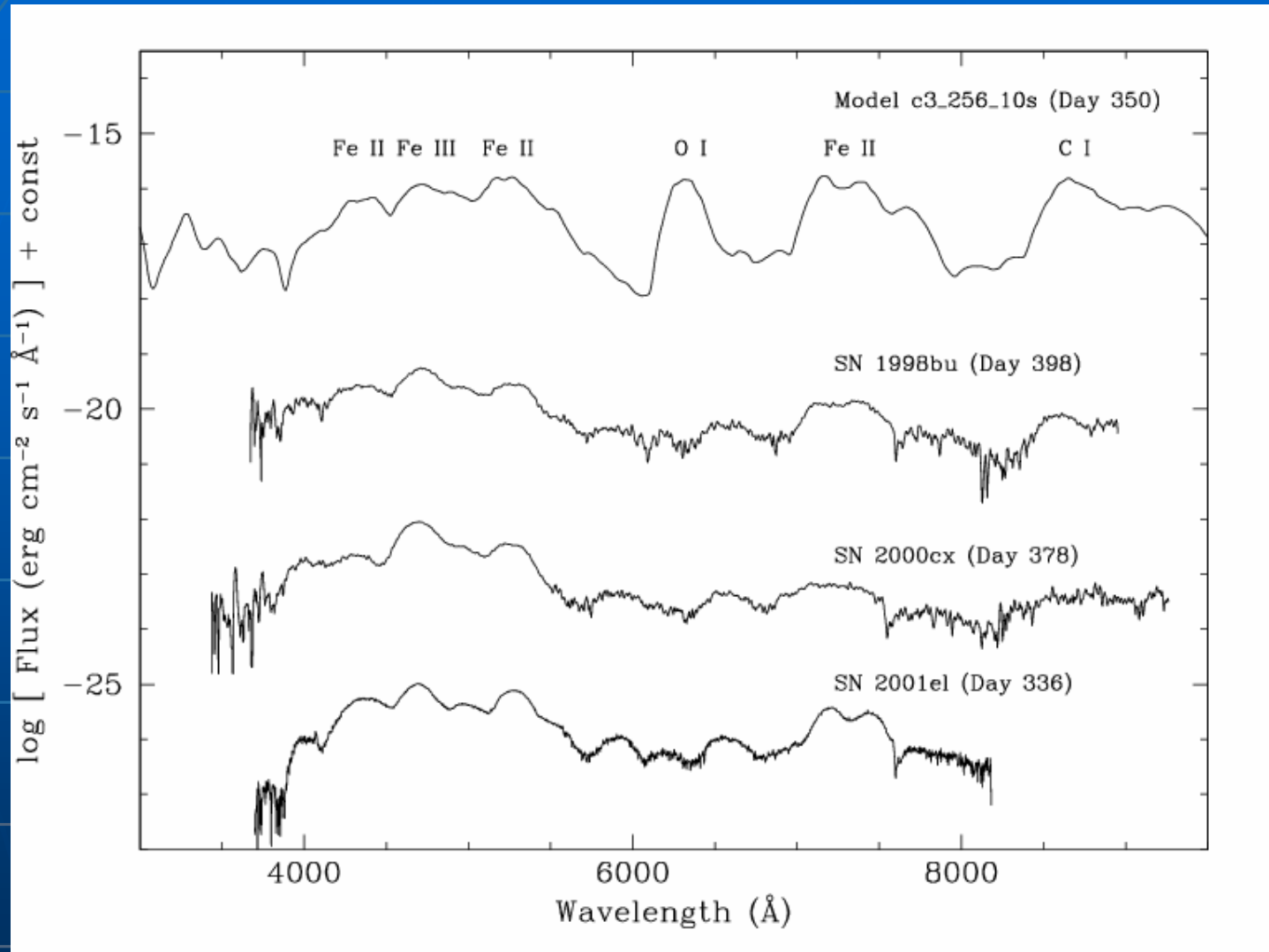


$X(^{12}\text{C})$	$E_{\text{nuc}}$ ( $10^{50}\text{erg}$ )	$M(\text{Ni}) (M_{\odot})$	$M_{\alpha}^{\text{max}}$ ( $M_{\odot}$ )
0.30	8.85	0.5178	0.0458
0.46	9.46	0.5165	0.0518
0.62	9.97	0.5104	0.0564

Ni-mass (luminosity)  
independent of initial C/O!

(Röpke & Hillebrandt, 2004)





*But:*  
*Nebular*  
*spectra!*

Too much  
low-velocity  
oxygen!

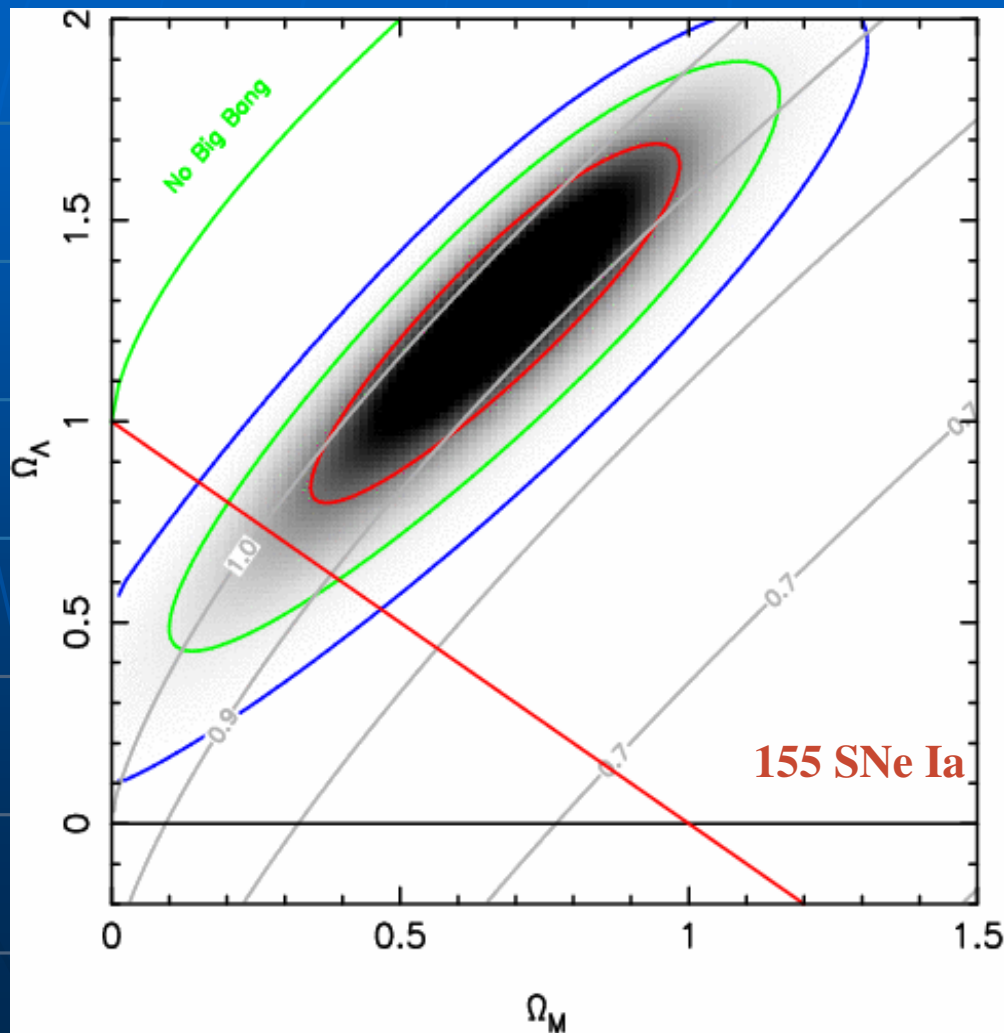
# Summary (Part II)

- n "Parameter-free" thermonuclear models of type Ia supernovae, based on Chandrasekhar-mass C+O white dwarfs explode with about the right energy.
- n They allow to predict light curves and spectra, depending on physical parameters!
- n They can explain (most of ?) the observed properties well.
- n The diversity may be due to randomness in the ignition conditions, (C/O), and metallicity.



# Supernovae and Cosmology: The Quest for Precise Luminosity Distances

(In part “borrowed” from a lecture by Bruno Leibundgut)



(Tonry et al. 2003)

# Distances in the local universe

- Assume a linear expansion (“Hubble law”)

$$v = cz = H_0 \cdot D$$

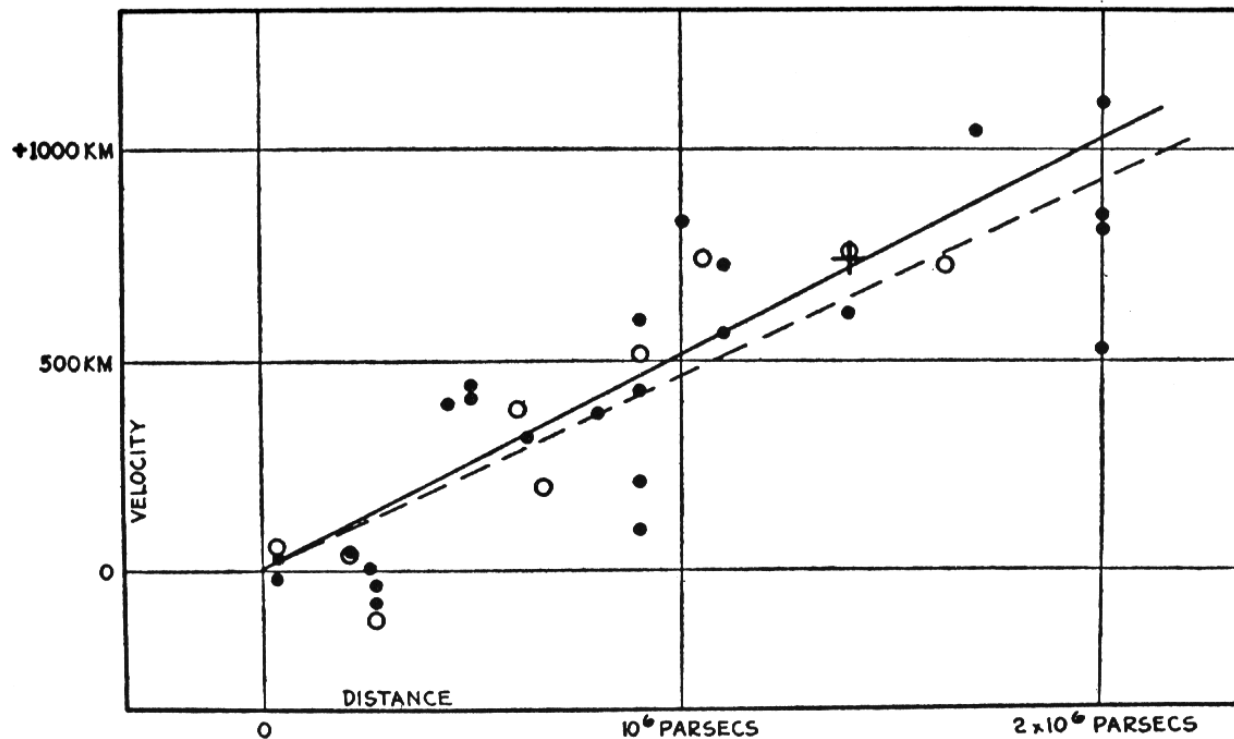
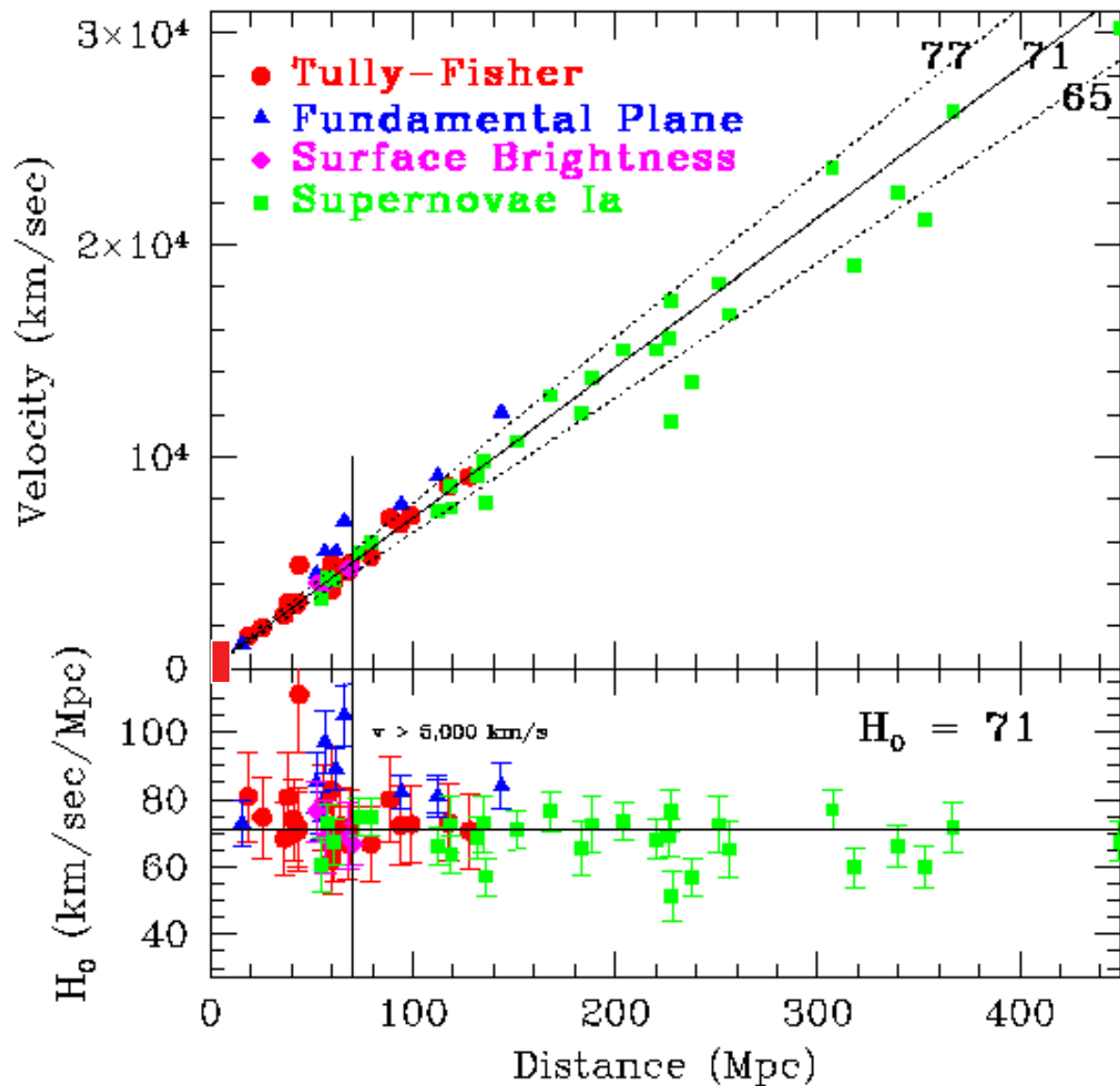
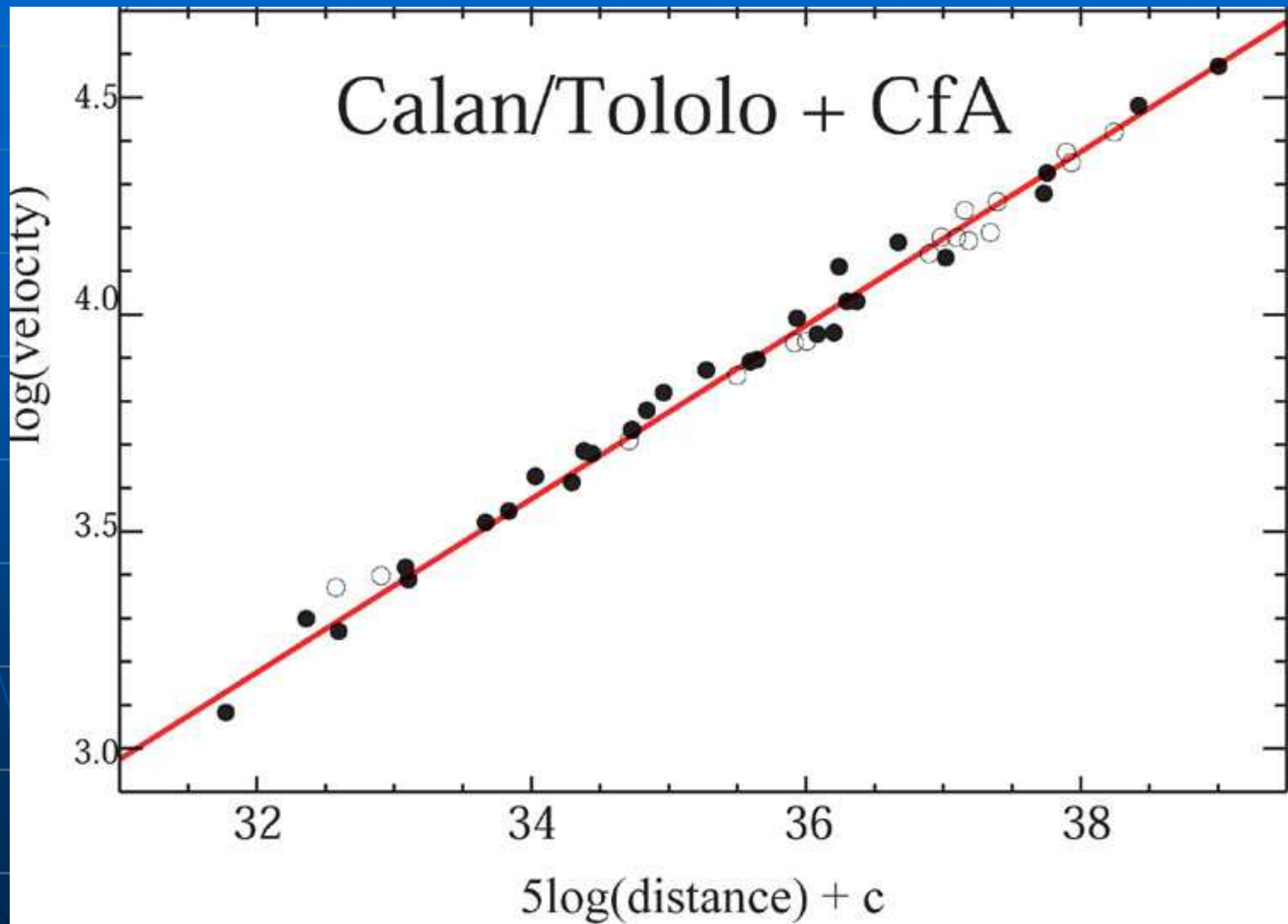


FIG. 9. *The Formulation of the Velocity-Distance Relation.*

# A “modern” Hubble diagram



# Universal expansion



## Distances in the local universe

- n Assume a linear expansion (Hubble law):

$$v = cz = H_0 \cdot D$$

- n Use the distance modulus

$$m - M = 5 \log(D/10 \text{ pc}) - 5$$

- n Distances of a 'standard candle' ( $M = \text{const.}$ )

$$m = 5 \log(z) + b$$

$$b = M + 25 + 5 \log(c) - 5 \log(H_0)$$

# The Hubble constant

- n Sets the absolute scale of cosmology
  - replaces these annoying  $h$ 's in all the theorists talks
- n Measure redshifts and distances in the nearby universe
  - Supernovae can do this in two ways:
    - n Expanding photosphere method of core-collapse SNe
    - n accurate (relative) distances from SN Ia

# Expanding Photosphere Method

n Baade (1926), Schmidt et al. (1993), Eastman et al. (1996), Hamuy et al. (2001)

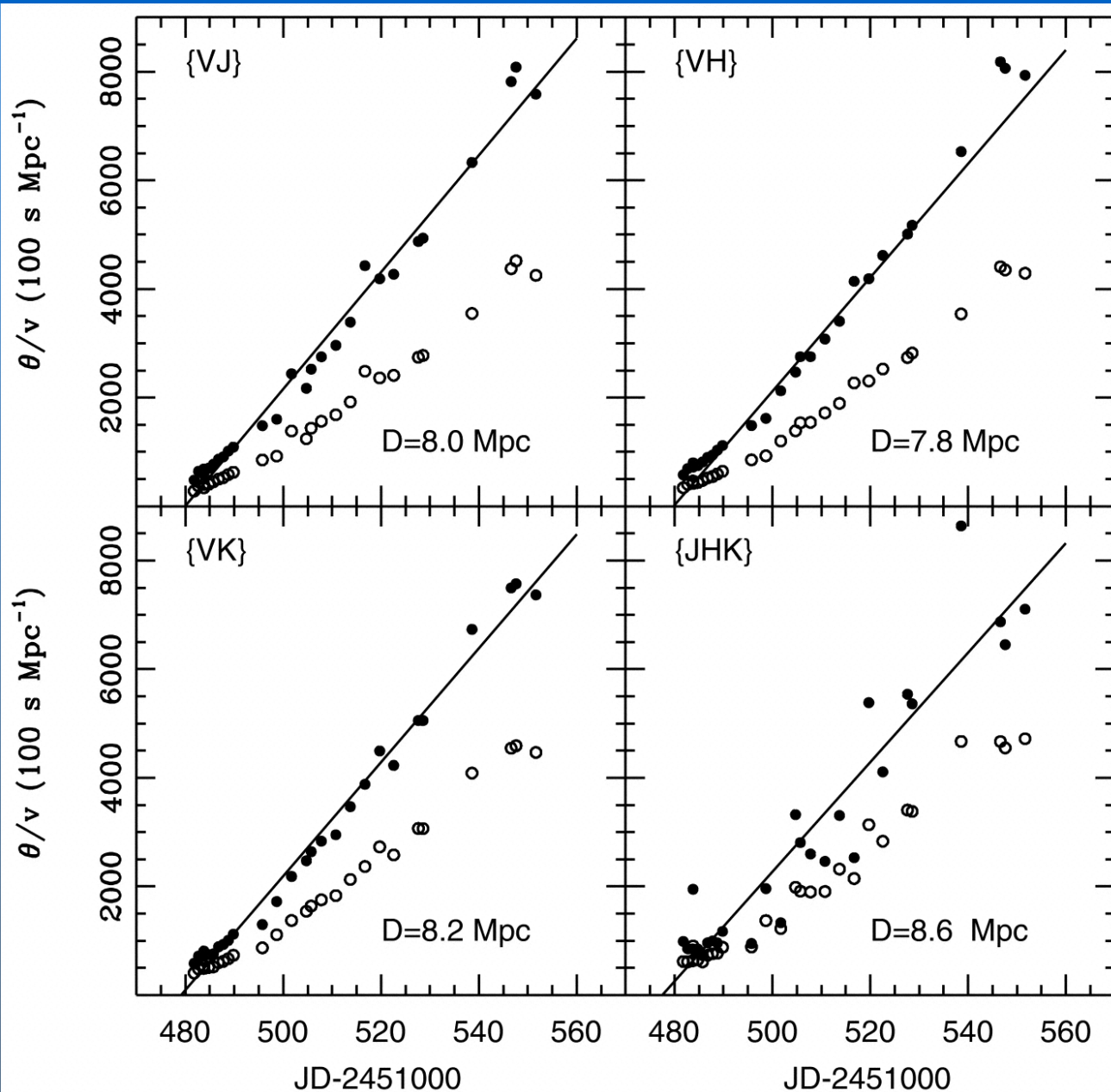
∅ Assume homologous expansion:  $R(t) = R_0 + v(t - t_0)$

∅ Photometric angular diameter

$$\Theta = \frac{R}{D} = \sqrt{\frac{f_\lambda}{\zeta_\lambda^2 \pi B_\lambda(T) 10^{-0.4A(\lambda)}}$$

# Distances from EPM

(SN 1999em, Hamuy et al. 2001)



$$\frac{\Theta_i}{v_i} \approx \frac{t_i - t_0}{D}$$

**Slope** gives the distance

**Intercept** the size of the progenitor and/or time of explosion



# Distances from EPM

- n Note that this distance measurement is completely **independent** of any other astronomical object!
  - no distance ladder
- n Assumption:
  - massive envelope that creates a photosphere
  - spherical symmetry
    - ⌘ not true for many core collapse supernovae
  - correction factors for deviation from black body spectrum
    - ⌘ model dependent

# EPM so far

## <sup>n</sup> Limitations

- needs large and extensive data sets
- difficulties to get into the Hubble flow
- distances only to galaxies with supernovae
  - <sup>n</sup> difficult to build large sample

## <sup>n</sup> Promise

- completely independent distance measurements
  - <sup>n</sup> checks on the Cepheid distance scale

## Distances with Type Ia Supernovae

n Use the Hubble diagram ( $m-M$  vs.  $\log z$ )

$$\emptyset m-M=5\log(z)+25+5\log(c)-5\log(H_0)$$

n Note that the slope is given here.

n Hubble constant can be derived when the absolute luminosity  $M$  is known

$$\emptyset \log H_0 = \log(z) + 5 + \log(c) - 0.2(m-M)$$

# Hubble constant from SNe Ia

## n Calibrate the absolute luminosity

- through Cepheids

- n 'classical distance ladder'

- depends on the accuracy of the previous rungs on the ladder
    - LMC distance,  $P - I_C$  relation, metallicities

- n HST program (Sandage, Tammann)

- n HST Key Programme (Freedman, Kennicutt, .....

- through models

- n extremely difficult

# Absolute Magnitudes of SNe Ia

SN	Galaxy	m-M	$M_B$	$M_V$	$M_I$	$\Delta m_{15}$
1937C	IC 4182	28.36 (12)	-19.56 (15)	-19.54 (17)	-	0.87 (10)
1960F	NGC 4496	31.03 (10)	-19.56 (18)	-19.62 (22)	-	1.06 (12)
1972E	NGC 5253	28.00 (07)	-19.64 (16)	-19.61 (17)	-19.27 (20)	0.87 (10)
1974G	NGC 4414	31.46 (17)	-19.67 (34)	-19.69 (27)	-	1.11 (06)
1981B	NGC 4536	31.10 (12)	-19.50 (18)	-19.50 (16)	-	1.10 (07)
1989B	NGC 3627	30.22 (12)	-19.47 (18)	-19.42 (16)	-19.21 (14)	1.31 (07)
1990N	NGC 4639	32.03 (22)	-19.39 (26)	-19.41 (24)	-19.14 (23)	1.05 (05)
1998bu	NGC 3368	30.37 (16)	-19.76 (31)	-19.69 (26)	-19.43 (21)	1.08 (05)
1998aq	NGC 3982	31.72 (14)	-19.56 (21)	-19.48 (20)	-	1.12 (03)
Straight mean			-19.57 (04)	-19.55 (04)	-19.26 (0 6)	
Weighted mean			-19.56 (07)	-19.53 (06)	-19.25 (0 9)	

(Saha et al. 1999)

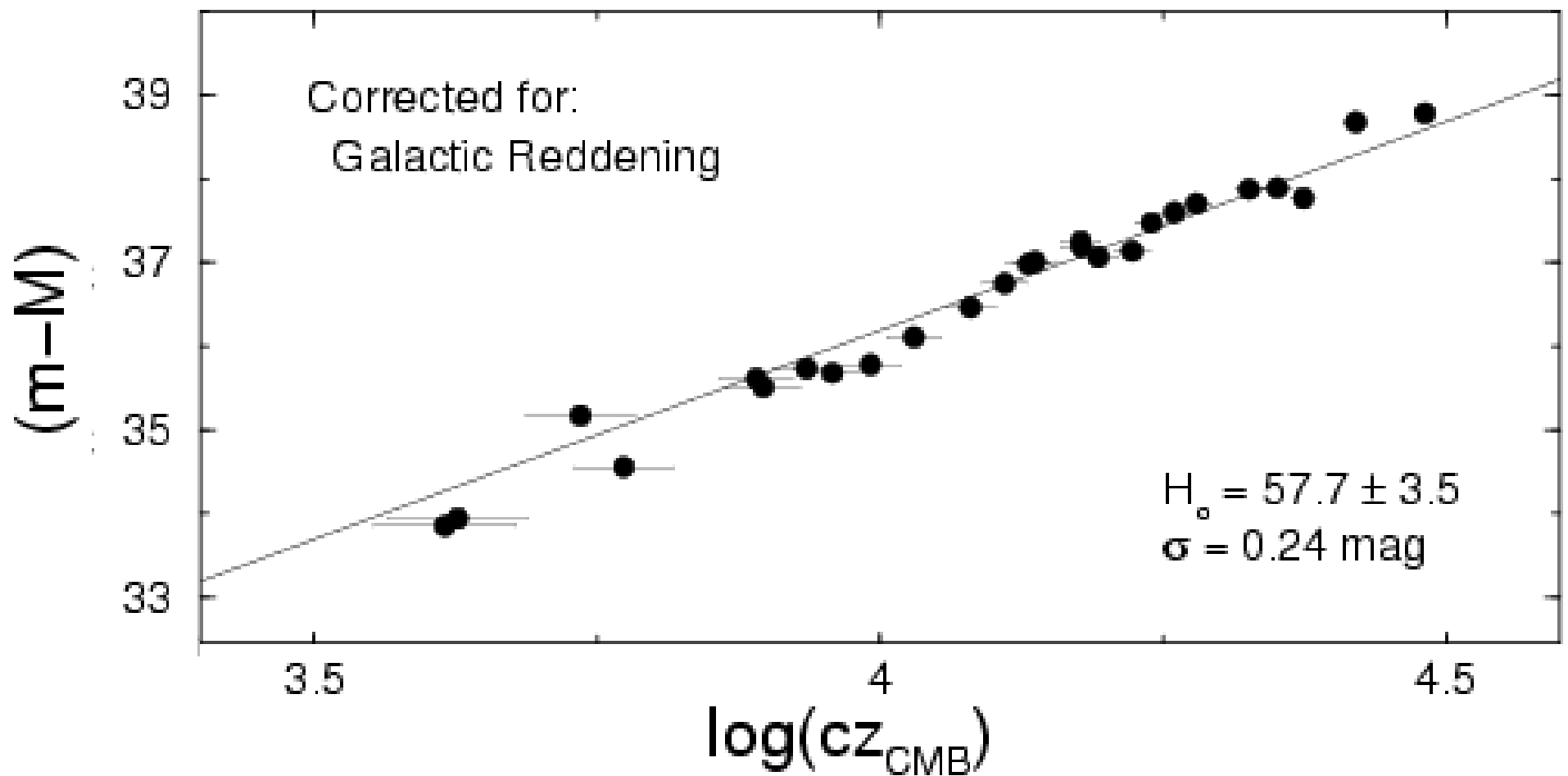
# Testing the SNe Ia as distance indicators

- n Hubble diagram of SNe Ia in the local, linear expansion, Hubble flow
- n Calibration through “primary” distance indicators
- n Theoretical models

# Nearby SNe Ia

Phillips et al. (1999)

## Calan/Tololo "Low Extinction" Sample



# Light curve shape – luminosity

## n $\Delta m_{15}$ relation

Phillips (1993), Hamuy et al. (1996), Phillips et al. (1999)

## n MLCS

Riess et al. (1996, 1998), Jha et al. (2003)

## n stretch

Perlmutter et al. (1997, 1999), Goldhaber et al. (2001)

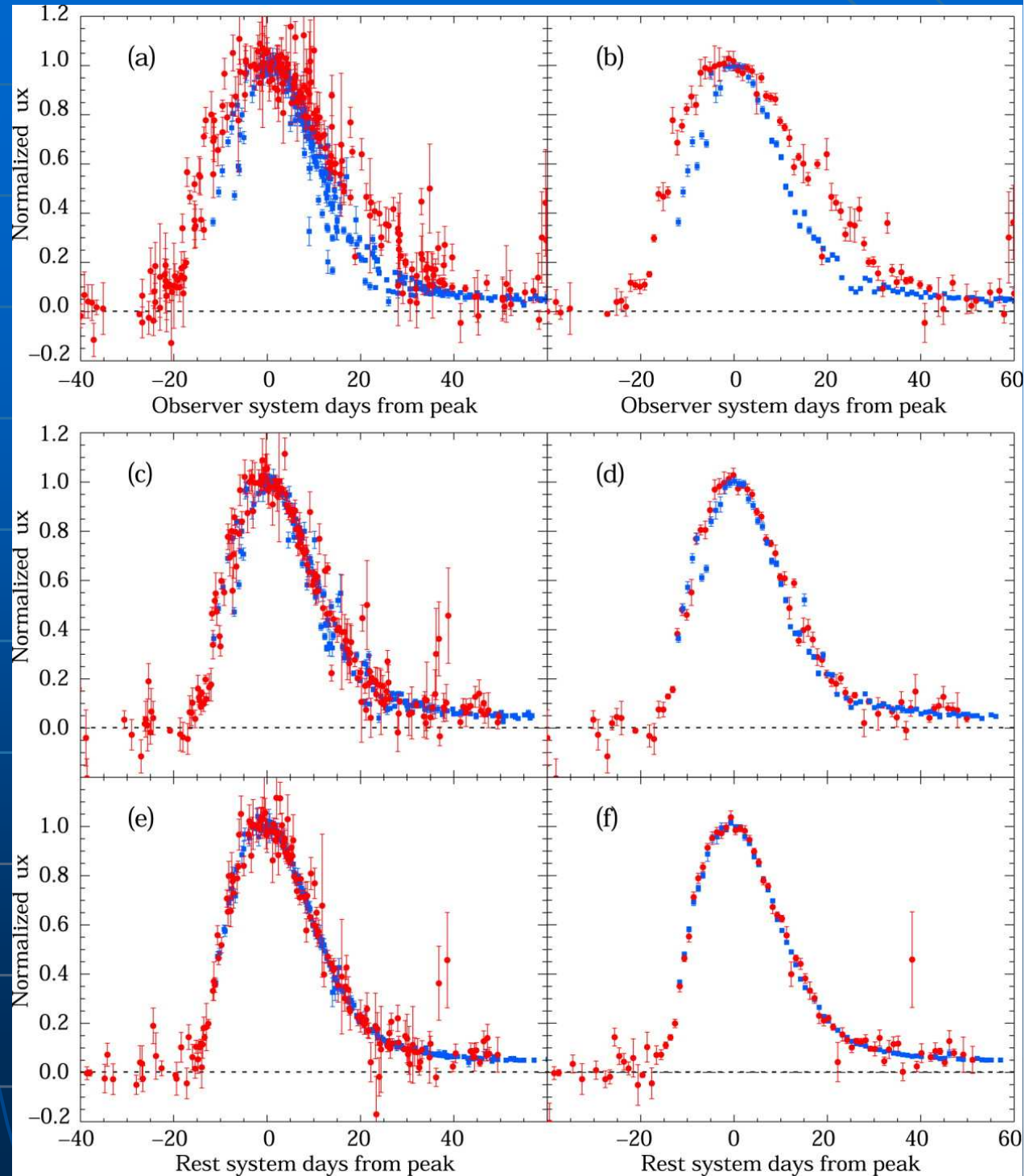
## n MAGIC

Wang et al. (2003)



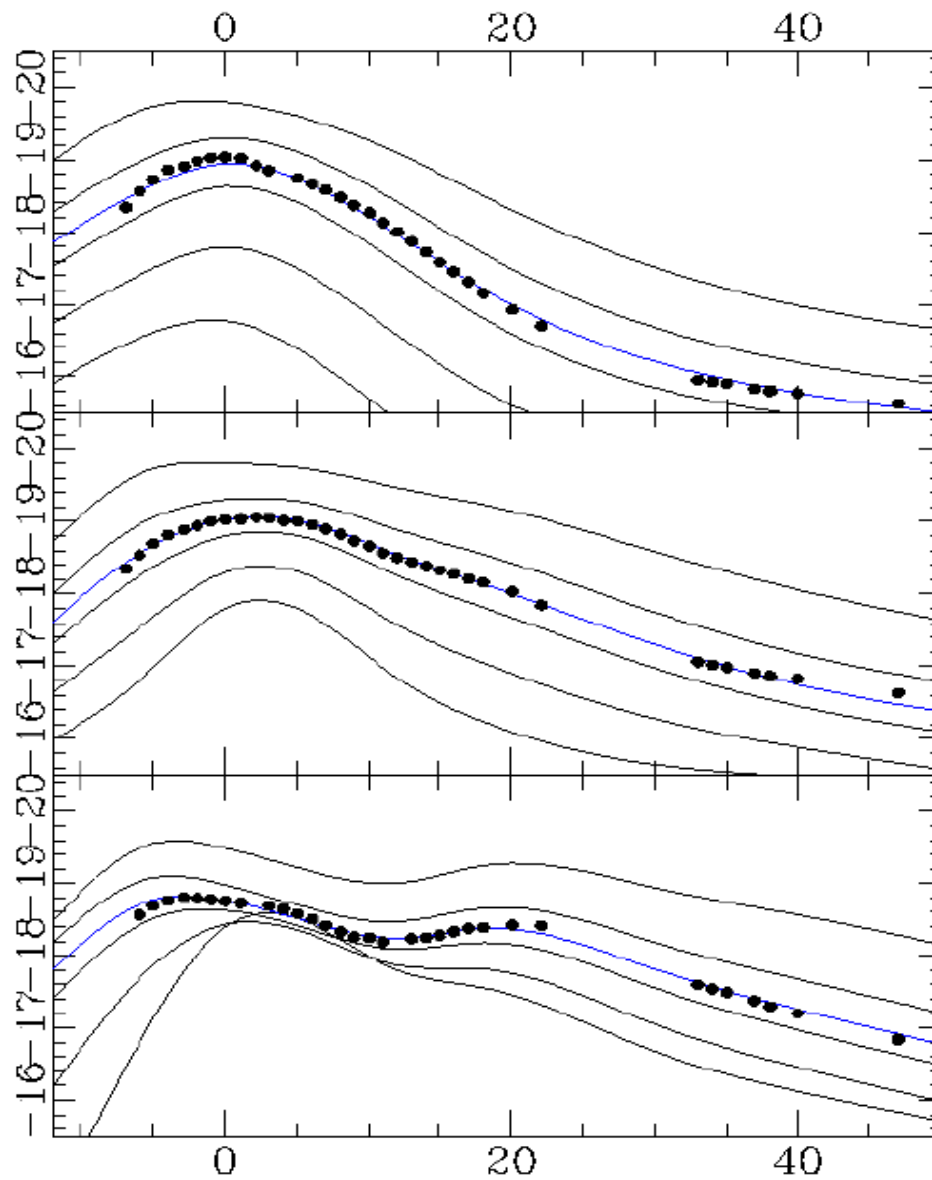
# The principles of the calibration

(Goldhaber et al. 2001)



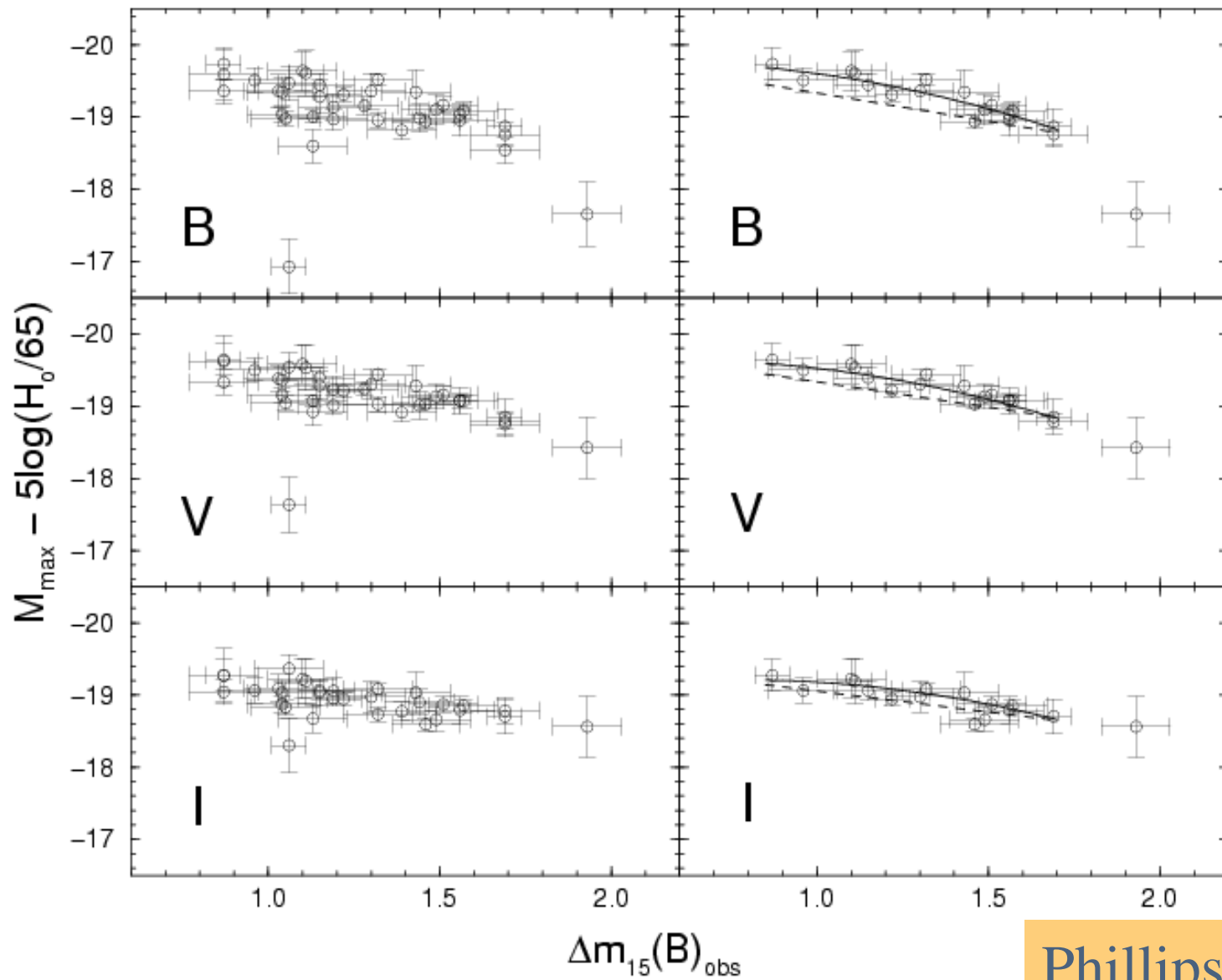
The SN Ia luminosity  
can be normalised:

Bright = slow  
Dim = fast



(Riess et al. 1996)

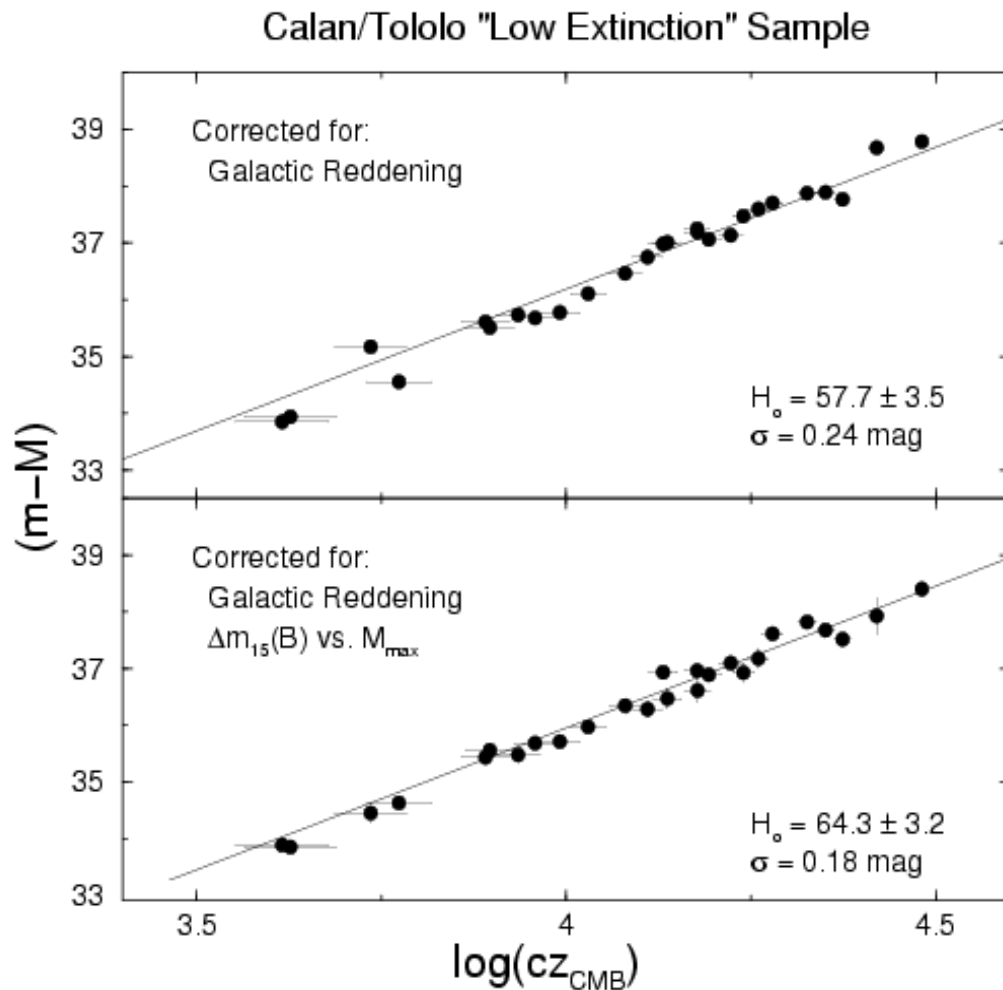
# Correlations



Phillips et al. 1999

# Normalisation of the peak luminosity

Phillips et al. 1999



Using the luminosity-decline rate relation one can normalise the peak luminosity of SNe Ia



Reduces the scatter!

# SN Ia Correlations

## n Luminosity vs. decline rate

- Phillips 1993, Hamuy et al. 1996, Riess et al. 1996, 1998, Perlmutter et al. 1997, Goldhaber et al. 2001

## n Luminosity vs. rise time

- Riess et al. 1999

## n Luminosity vs. color at maximum

- Riess et al. 1996, Tripp 1998, Phillips et al. 1999

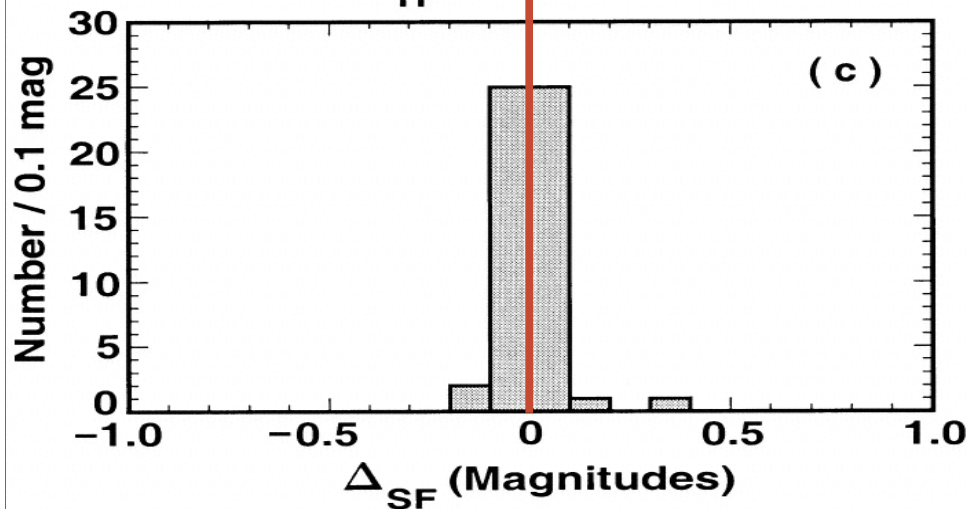
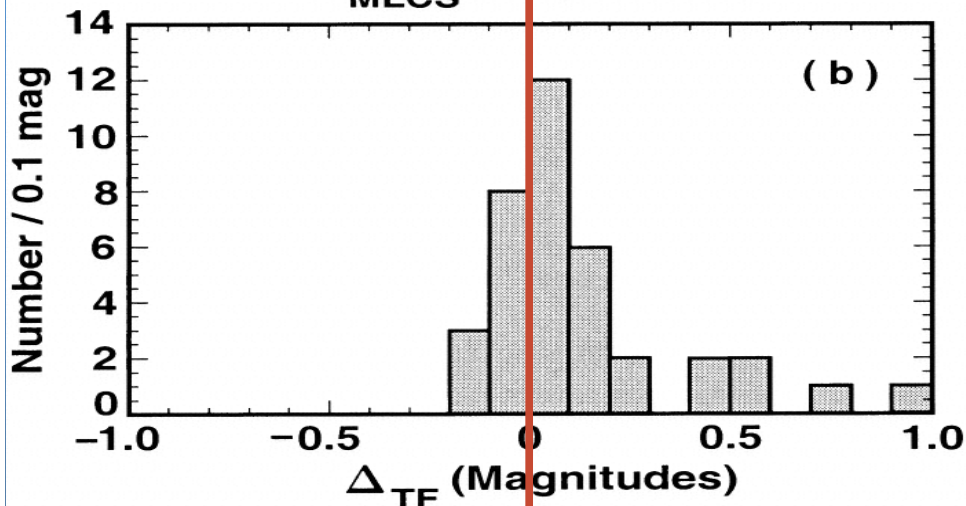
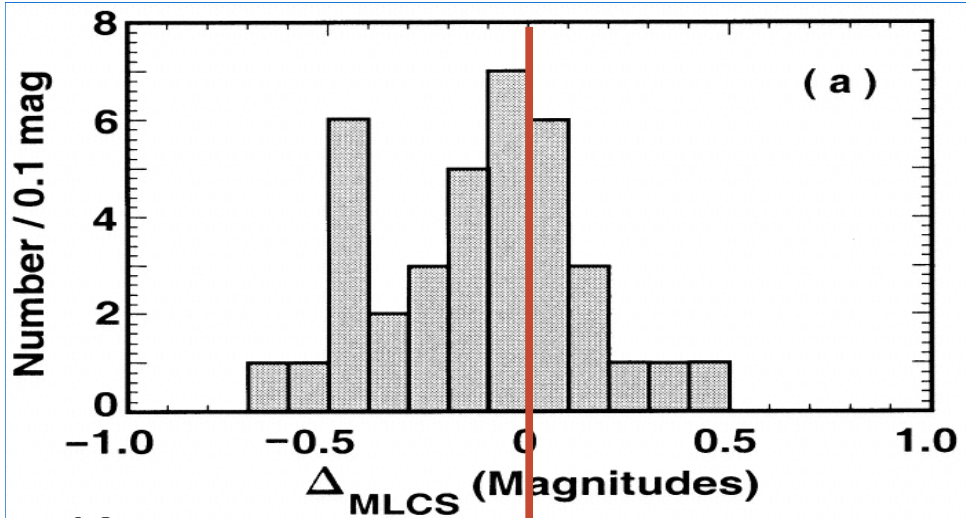
## n Luminosity vs. line strengths and line widths

- Nugent et al. 1995, Riess et al. 1998, Mazzali et al. 1998

## n Luminosity vs. host galaxy morphology

- Filippenko 1989, Hamuy et al. 1995, 1996, Schmidt et al. 1998, Branch et al. 1996

# SN Ia Correlations



Riess et al. 1998



Phillips et al. 1999

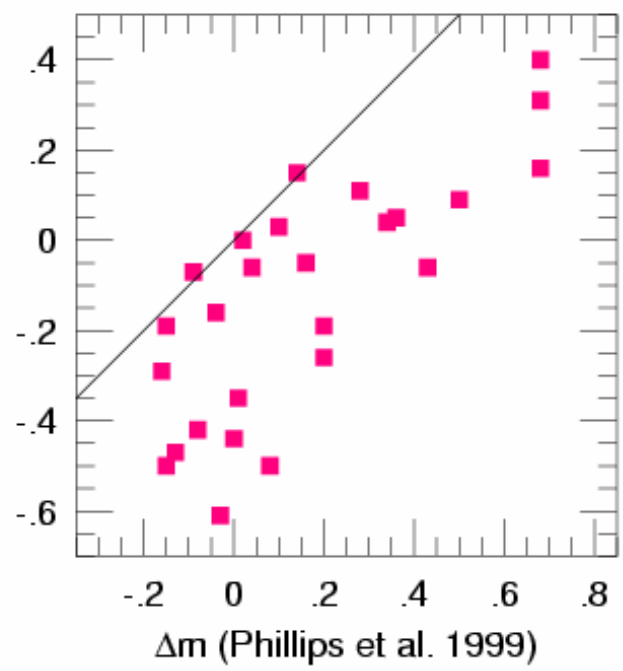
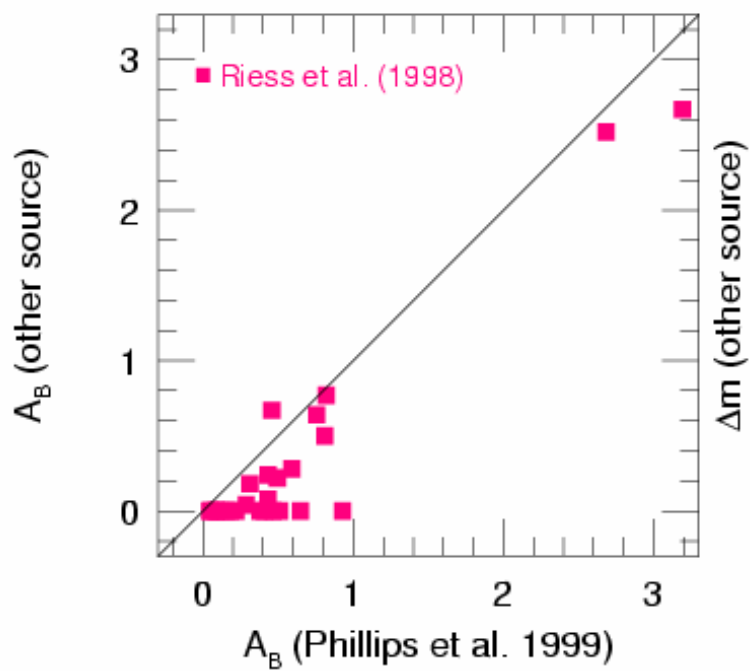
Perlmutter et al. 1997



(Drell et al. 2000)

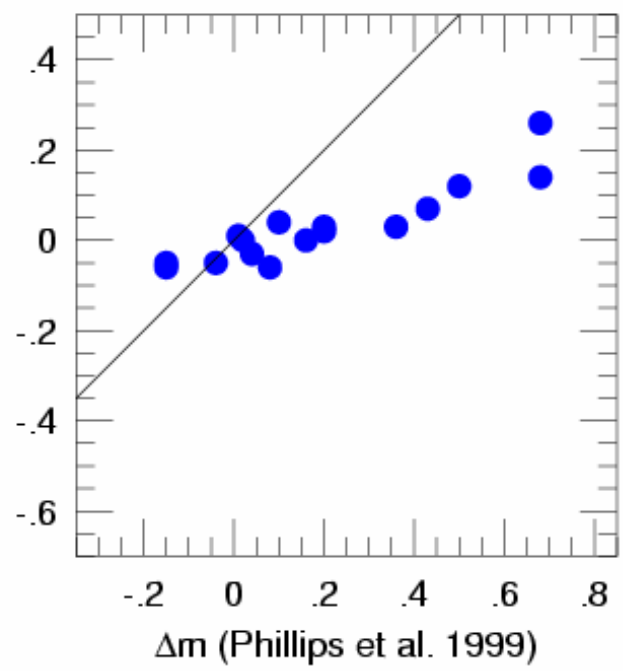
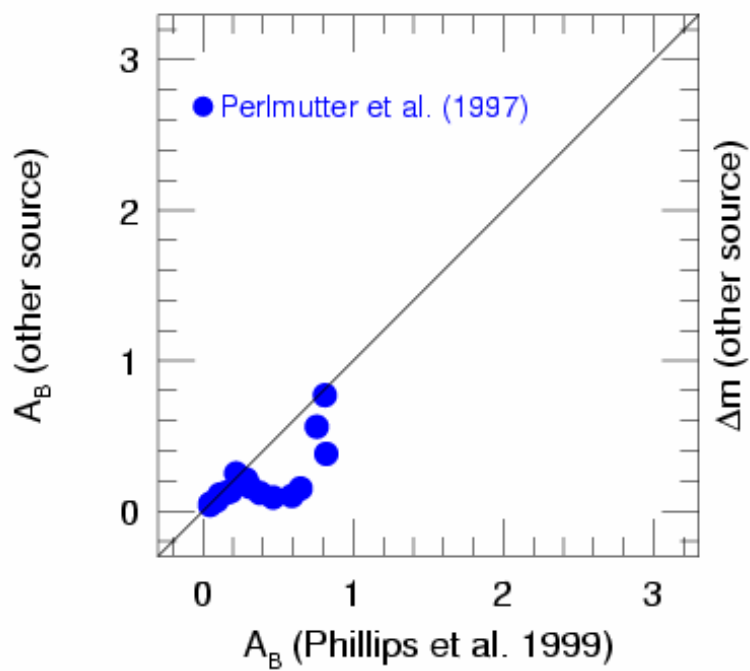
# SN Ia Correlations

Leibundgut 2000



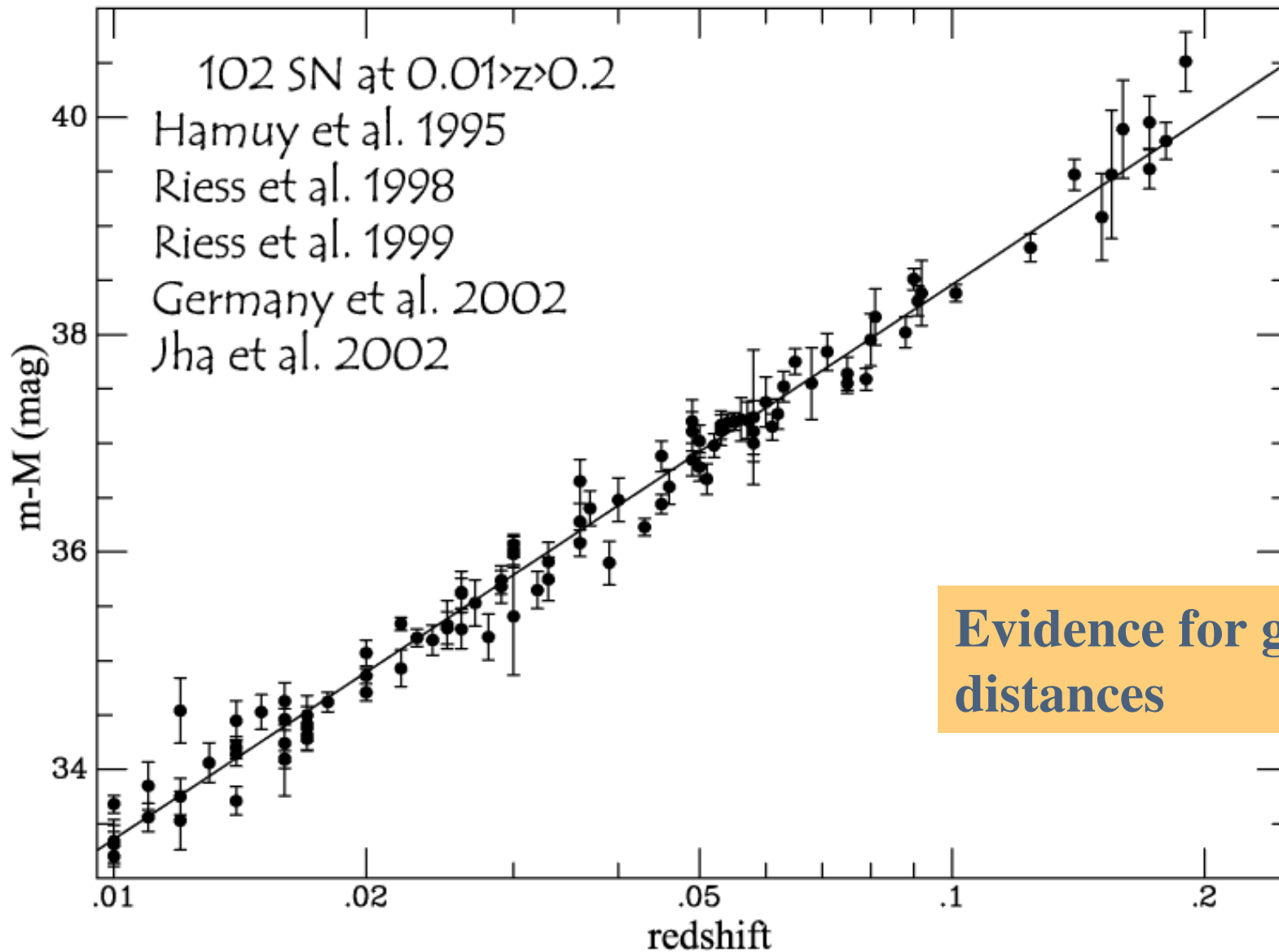
# SN Ia Correlations

Leibundgut 2000





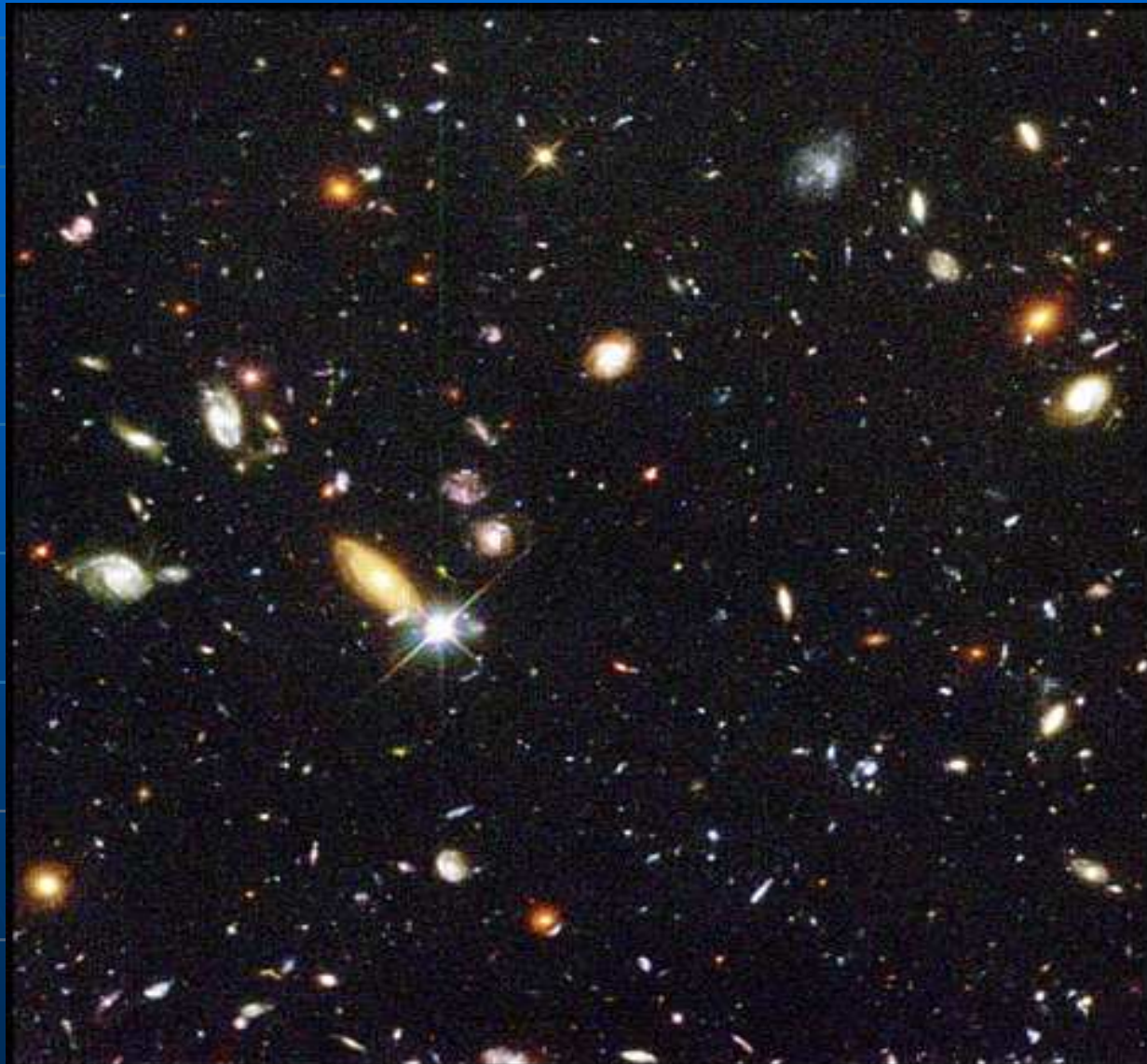
# The nearby SN Ia sample



# Hubble constant from SNe Ia

- n Extremely good (relative) distance indicators
  - distance accuracy around 10%
- n Uncertainty in  $H_0$  mostly from the LMC and the Cepheid P-L relation

# Very distant supernovae



Hubble Deep Field

HST · WFPC2

PRC96-01a · ST ScI OPO · January 15, 1996 · R. Williams (ST ScI), NASA

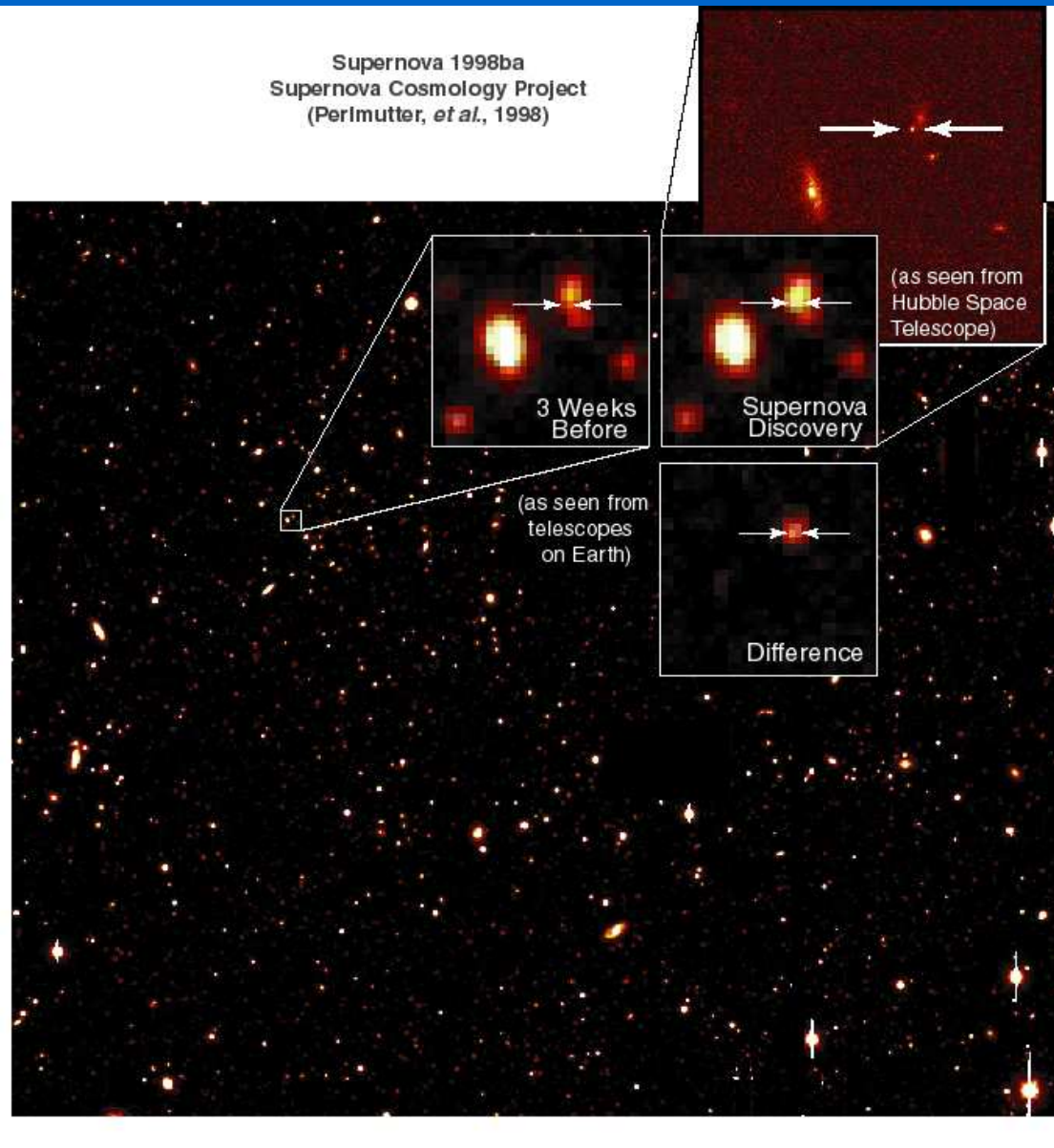
Supernovae are very rare,  $\sim 1$  SN per 100 years and galaxy.

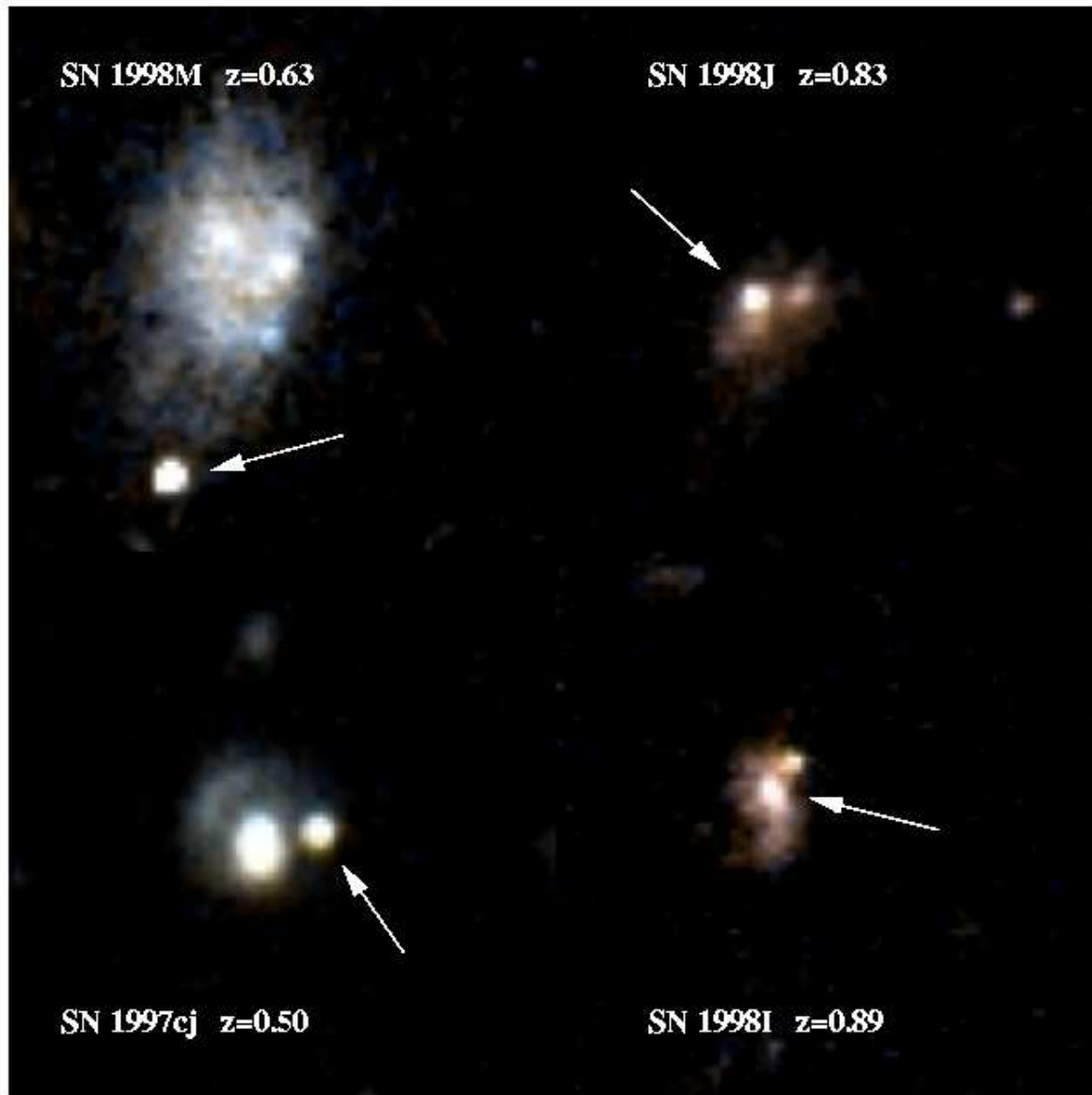


One has to observe very many galaxies!

## Search strategy:

1. Repeated scanning of a certain field.
2. Electronic readout of the data.
3. Follow-up observations, e.g., HST, VLT, ...

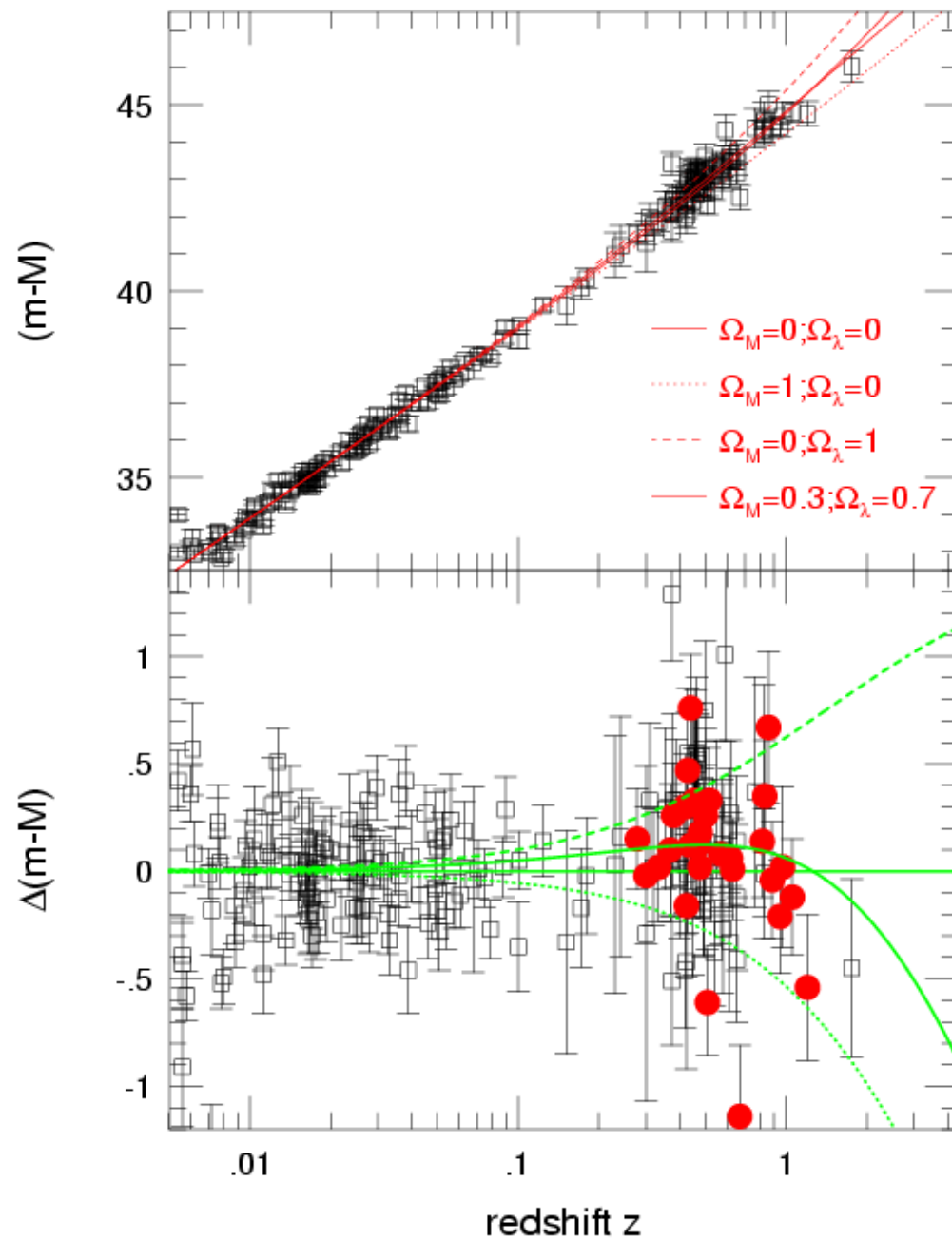




Supernovae are routinely detected at redshifts  $Z > 0.4$ :

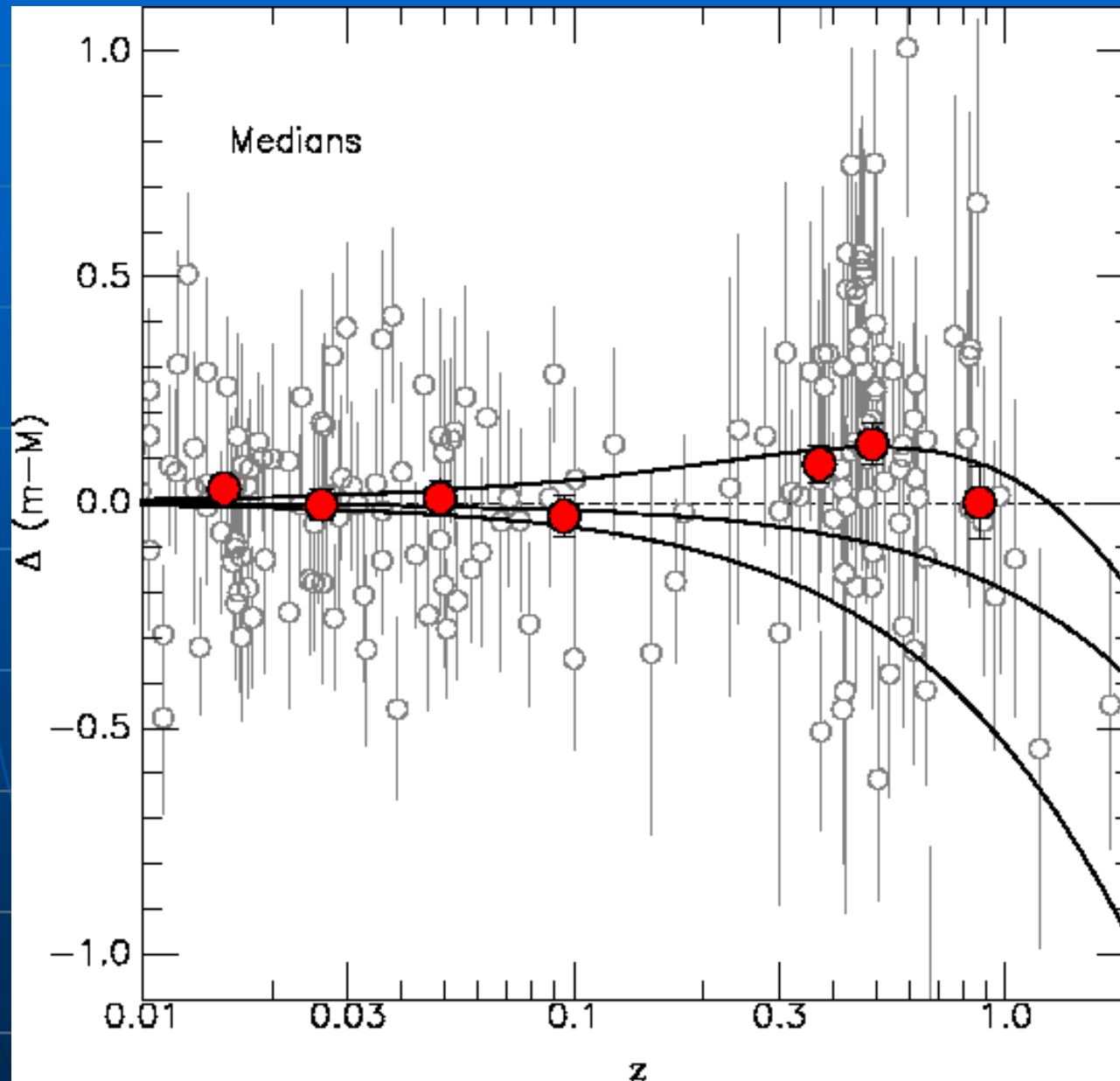
- What is the intrinsic scatter in luminosities?
- Are they different from the local sample?
- Do we understand the differences?

# Supernovae at high redshifts



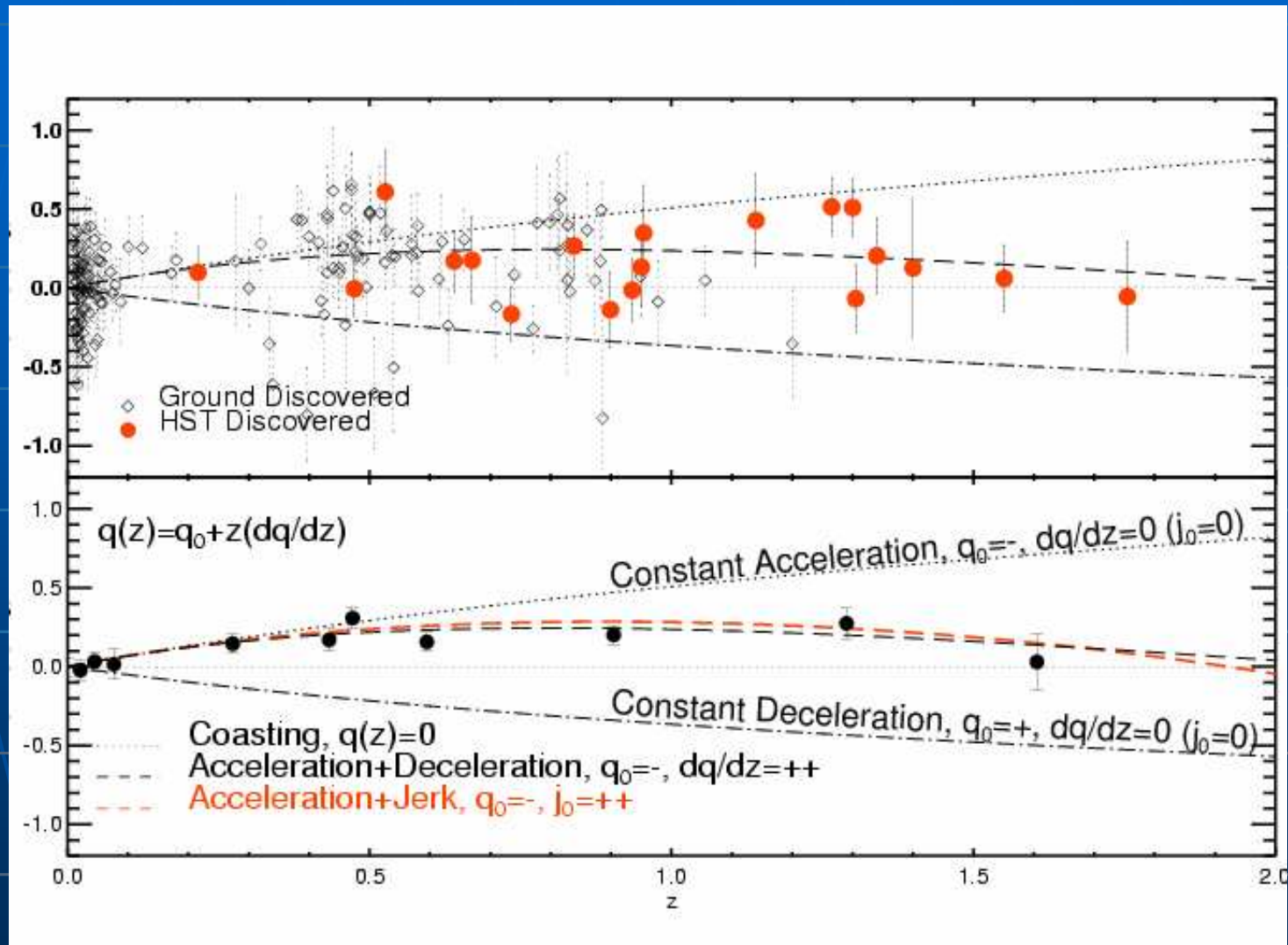
Tonry et al. 2003

# 209 SNe Ia and medians



Tonry et al. 2003

# Very high redshift SNe Ia





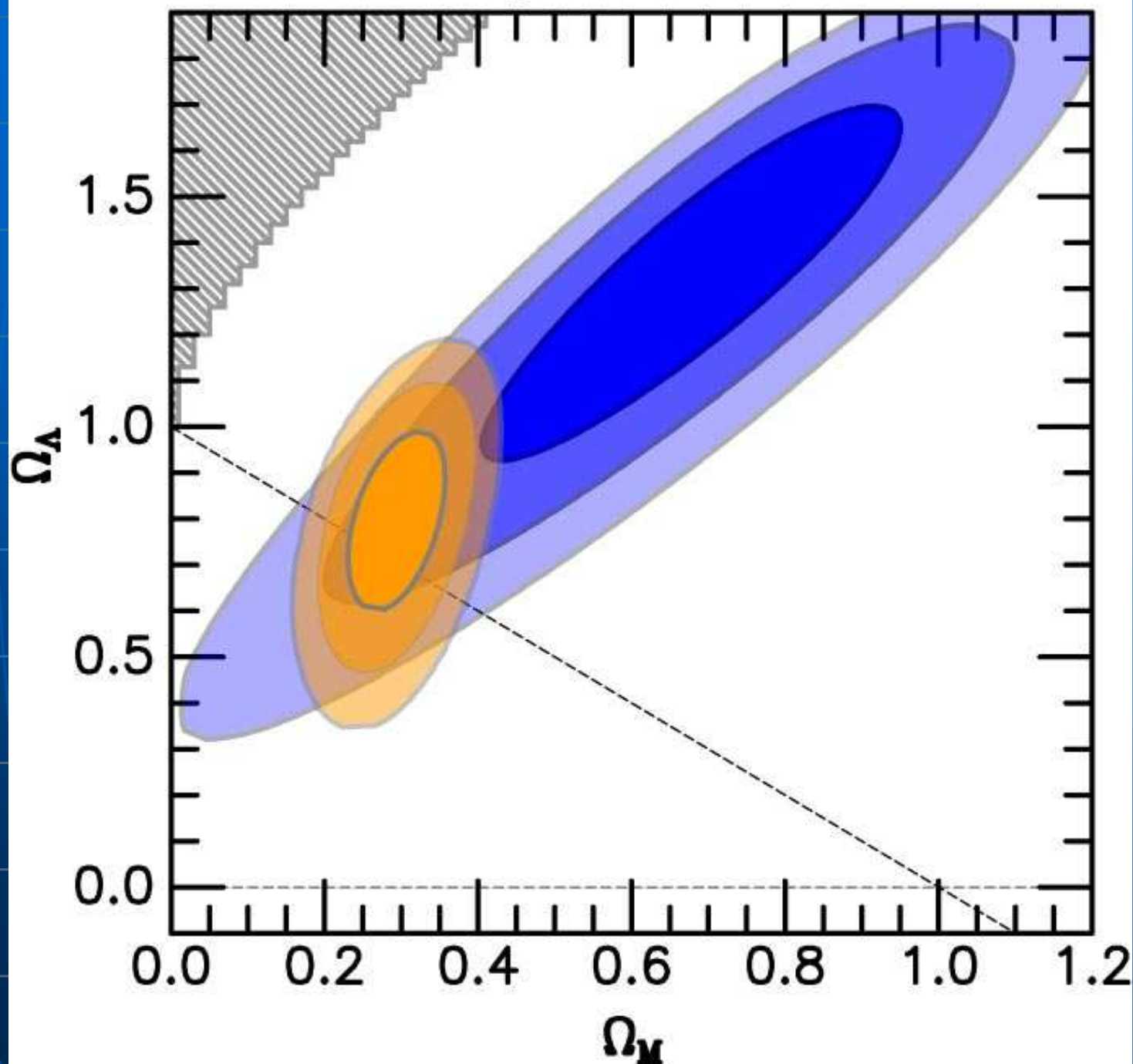
# Entire High-Z SN Ia Data Set

*2dF:*

$$\Omega_M = 0.2 \pm 0.03$$

*KP:*

$$h = 0.72 \pm 0.08$$



## General luminosity distance

$$D_L = \frac{(1+z)c}{H_0 \sqrt{|\Omega_k|}} S \left\{ \sqrt{|\Omega_k|} \int_0^z \left[ \Omega_k (1+z')^2 + \sum_i \Omega_i (1+z')^{3(1+\omega_i)} \right]^{-1/2} dz' \right\}$$

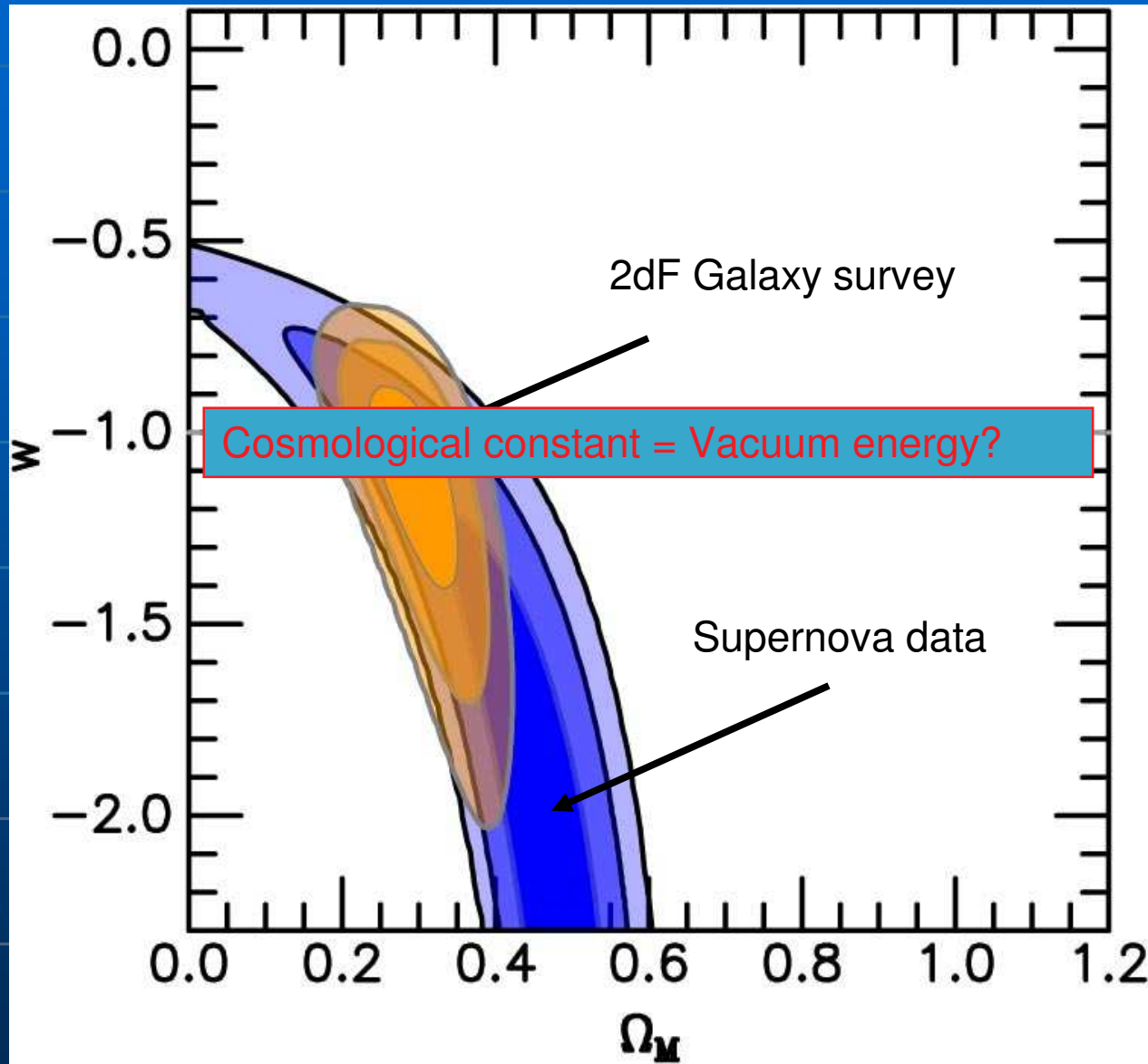
• with  $\Omega_k = 1 - \sum_i \Omega_i$  and  $\omega_i = \frac{p_i}{\rho_i c^2}$

$\omega_M = 0$  (matter)

$\omega_R = 1/3$  (radiation)

$\omega_\Lambda = -1$  (cosmological constant)

$(w \equiv \omega !)$



## Cosmology and Typ Ia supernovae

The “equation of state” of the Universe:

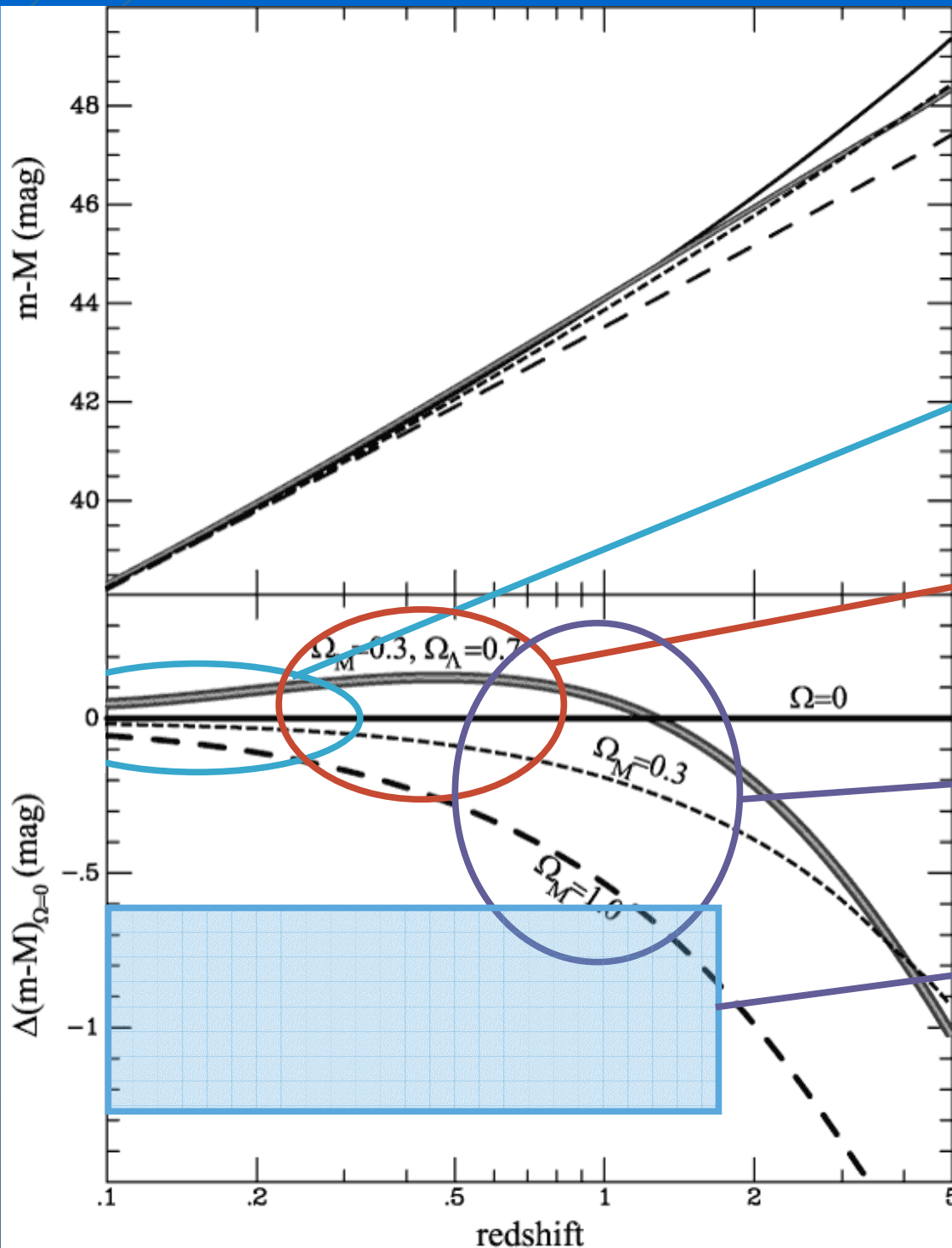
$$p = wp$$

$$\ddot{a} \sim (\rho + 3p)$$

$$w < -1/3 :$$

Acceleration!

# SN Projects

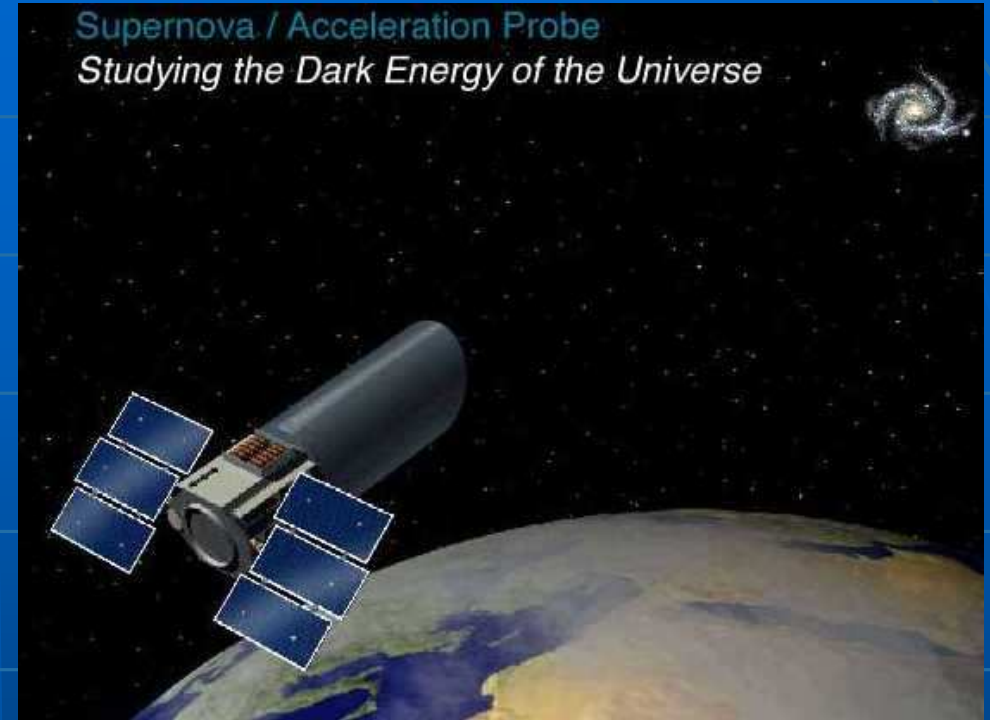
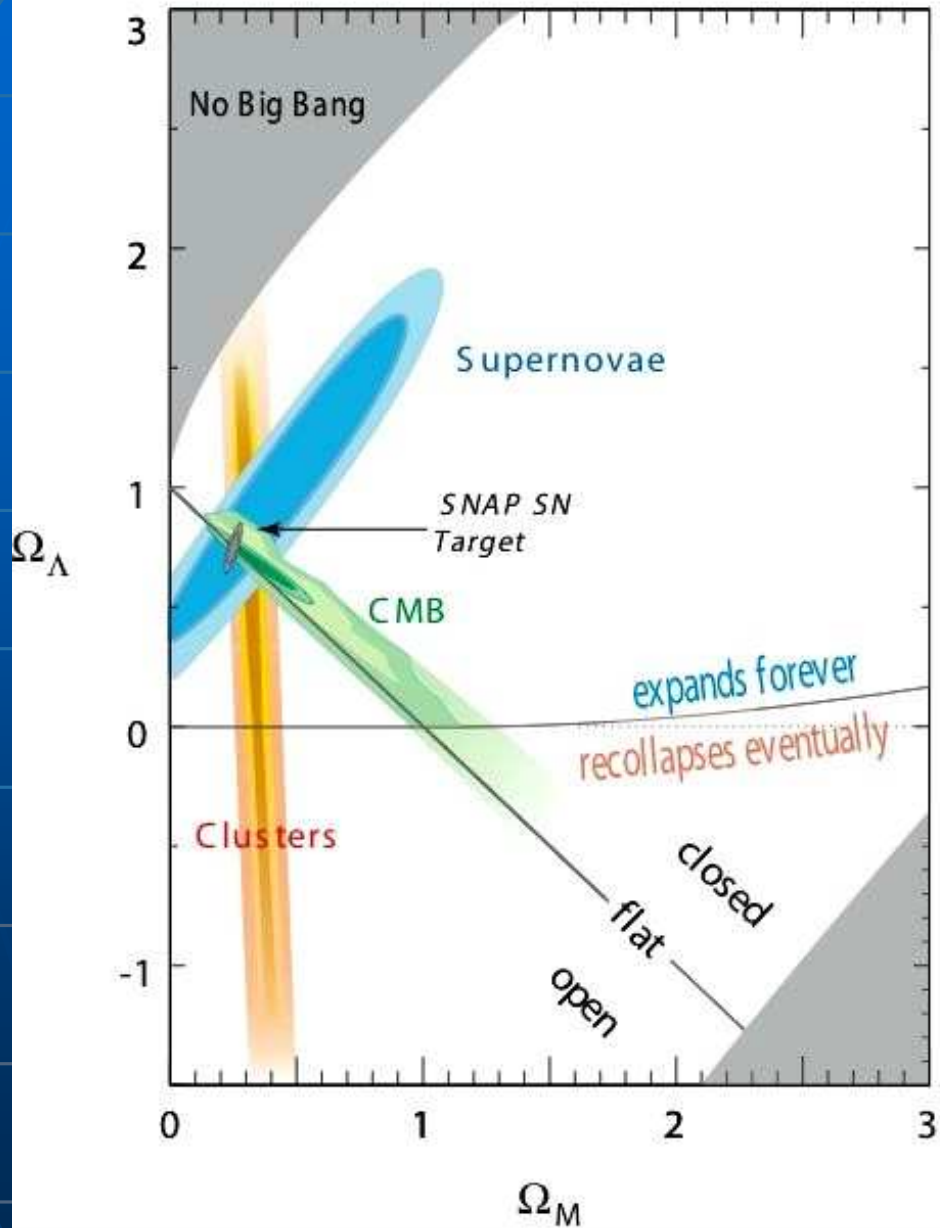


SN Factory  
Carnegie SN Project

ESSENCE  
CFHT Legacy Survey

High-z SN Search  
(GOODS)

SNAP  
(Supernova  
acceleration  
Probe)

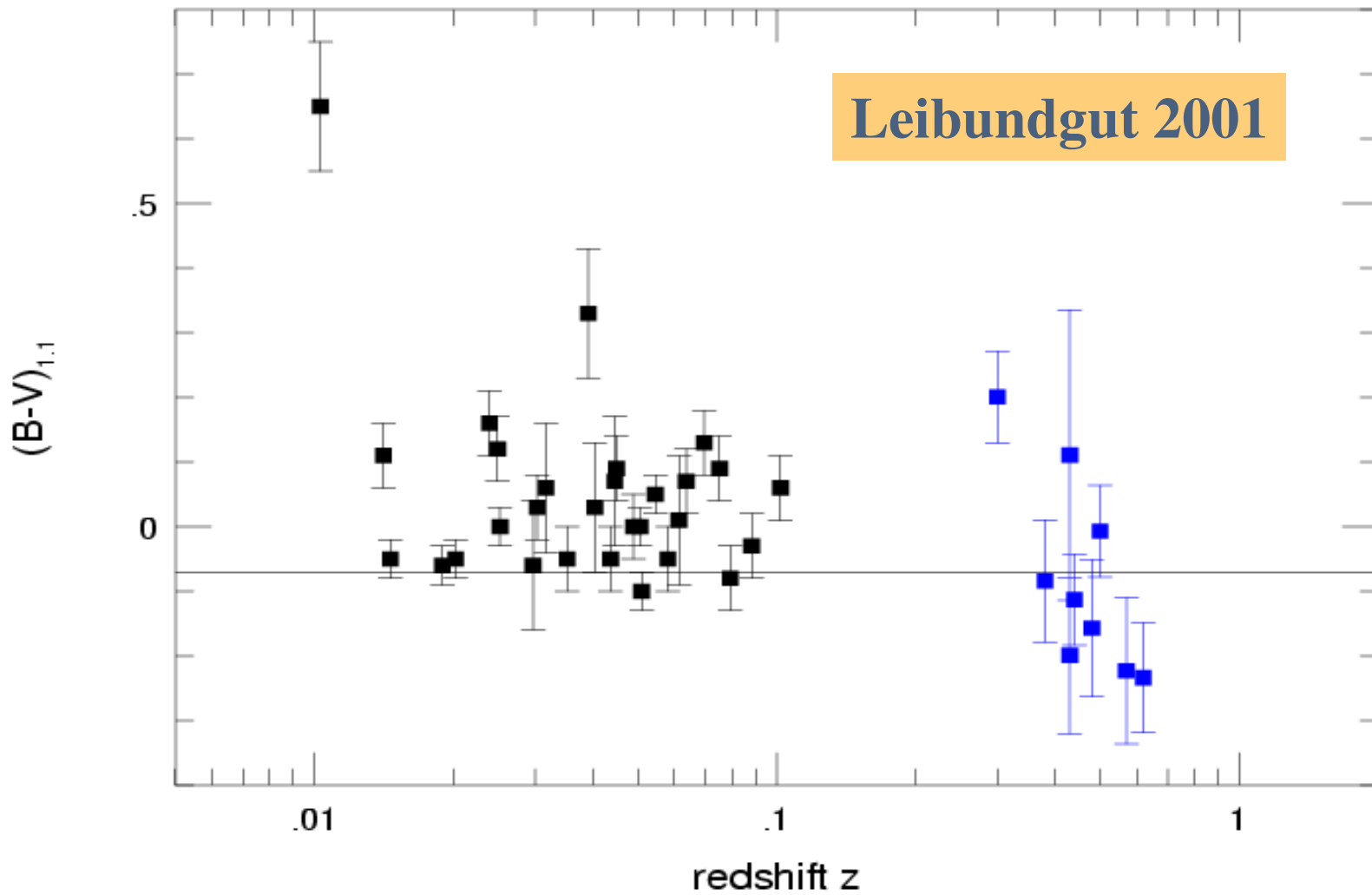


SNAP:  
“Supernova/Acceleration Probe”

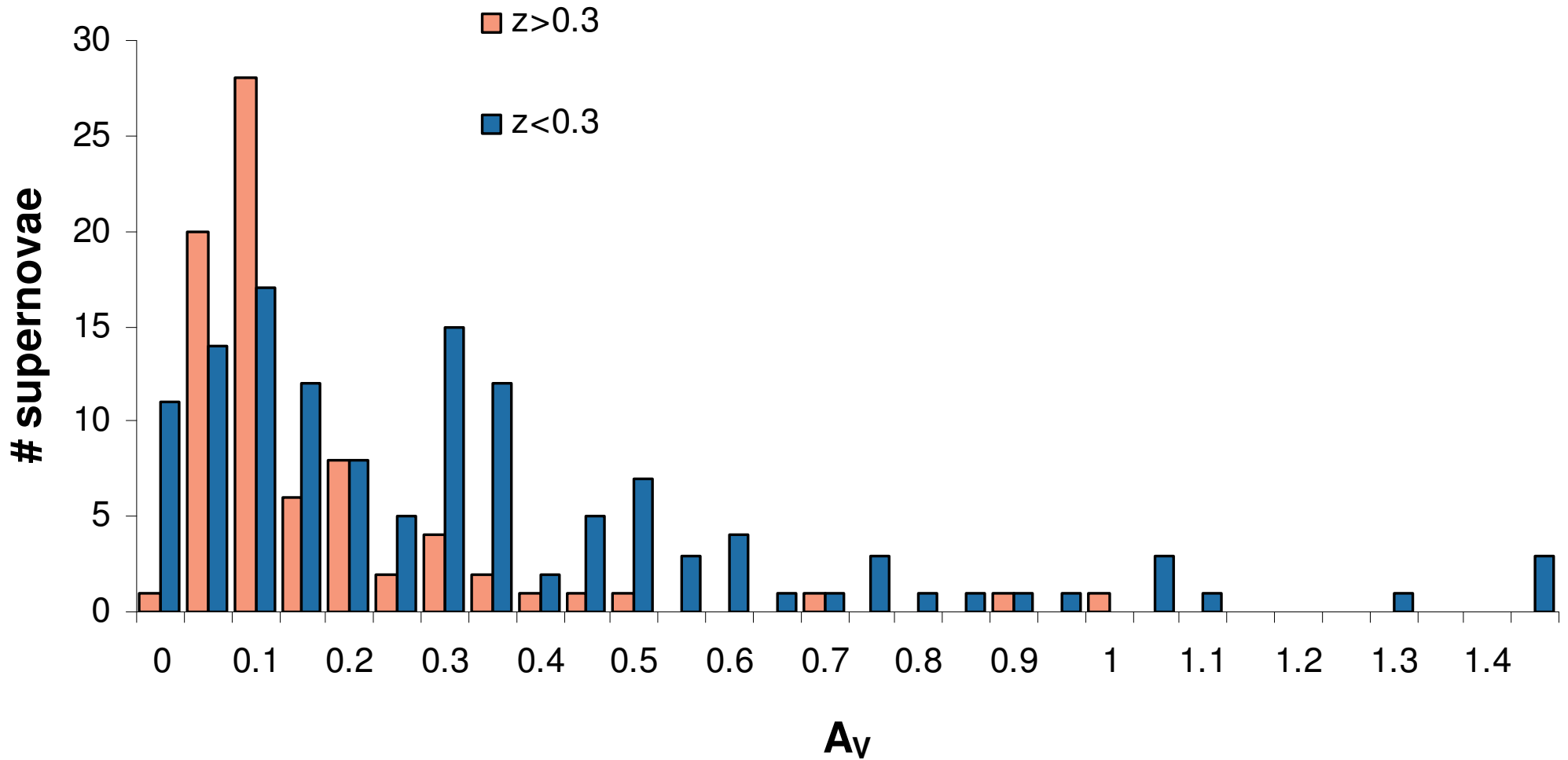
# What can still be wrong???

- q Systematic errors?
- q Pollution of high-Z samples?

# Is evolution a problem?

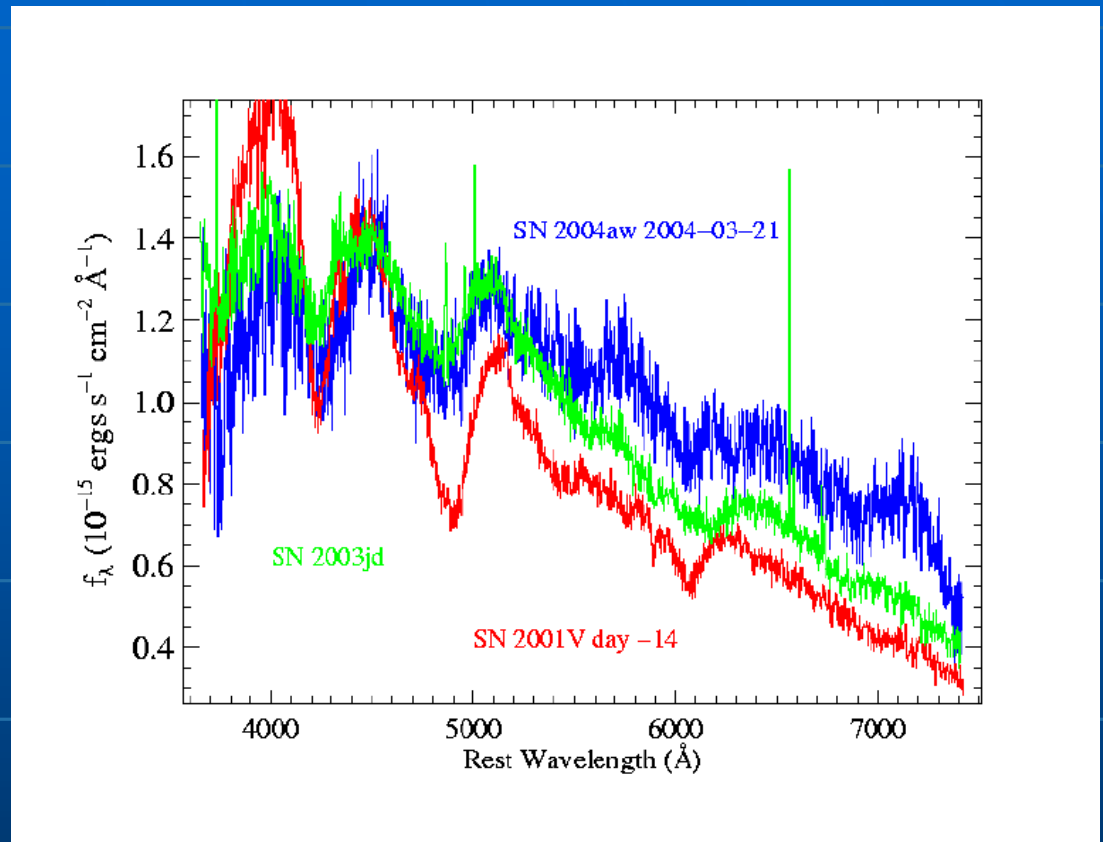


# Absorption distributions





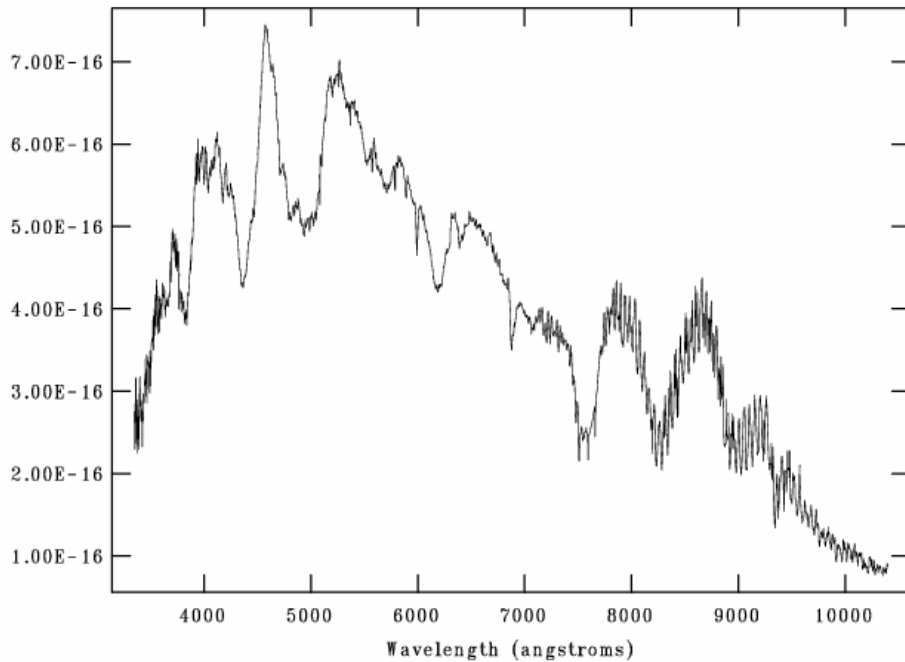
# Pollution of the samples: SN 2004aw?



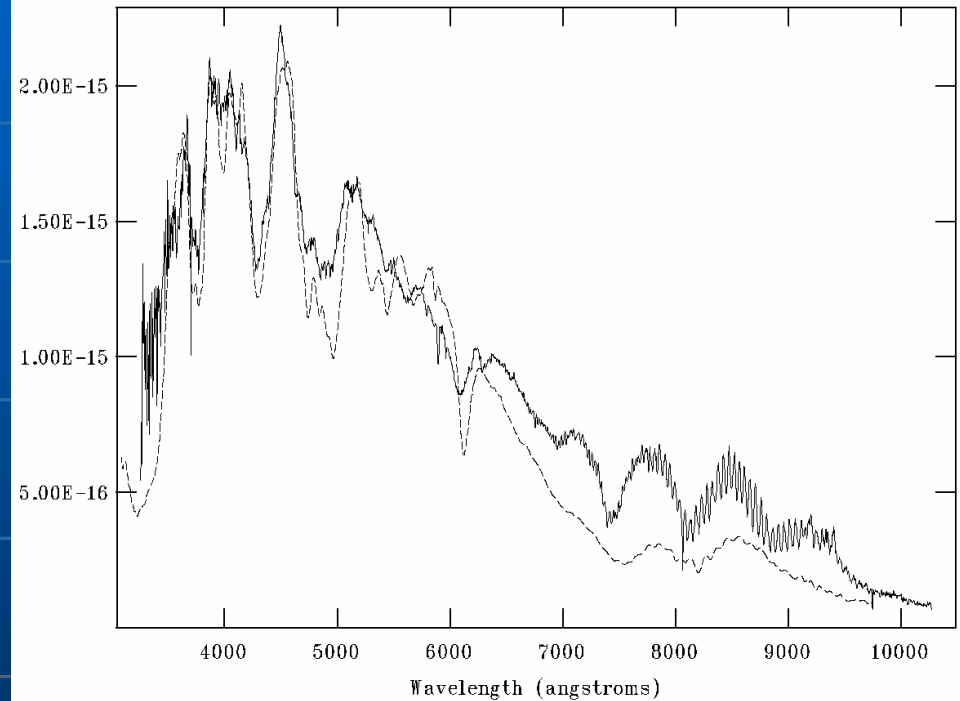
- Discovery: *March 19, 2004*
- Host galaxy: *NGC 3997;  $V = 4771 \text{ km/s}$*
- B-Maximum: *~ April 5, 2004*

# First classification

NOAO/IRAF V2.12.2-EXPORT tauben@ncf-11 Fri 16:04:42 30-Apr-2004  
[spec]: 1200. ap:1 beam:1



NOAO/IRAF V2.12.1-EXPORT sbenetti@graspa.pd.astro.it Fri 09:00:58 26-Ma  
[2004aw\_20040324\_z0\_der]: 1200. ap:1 beam:1



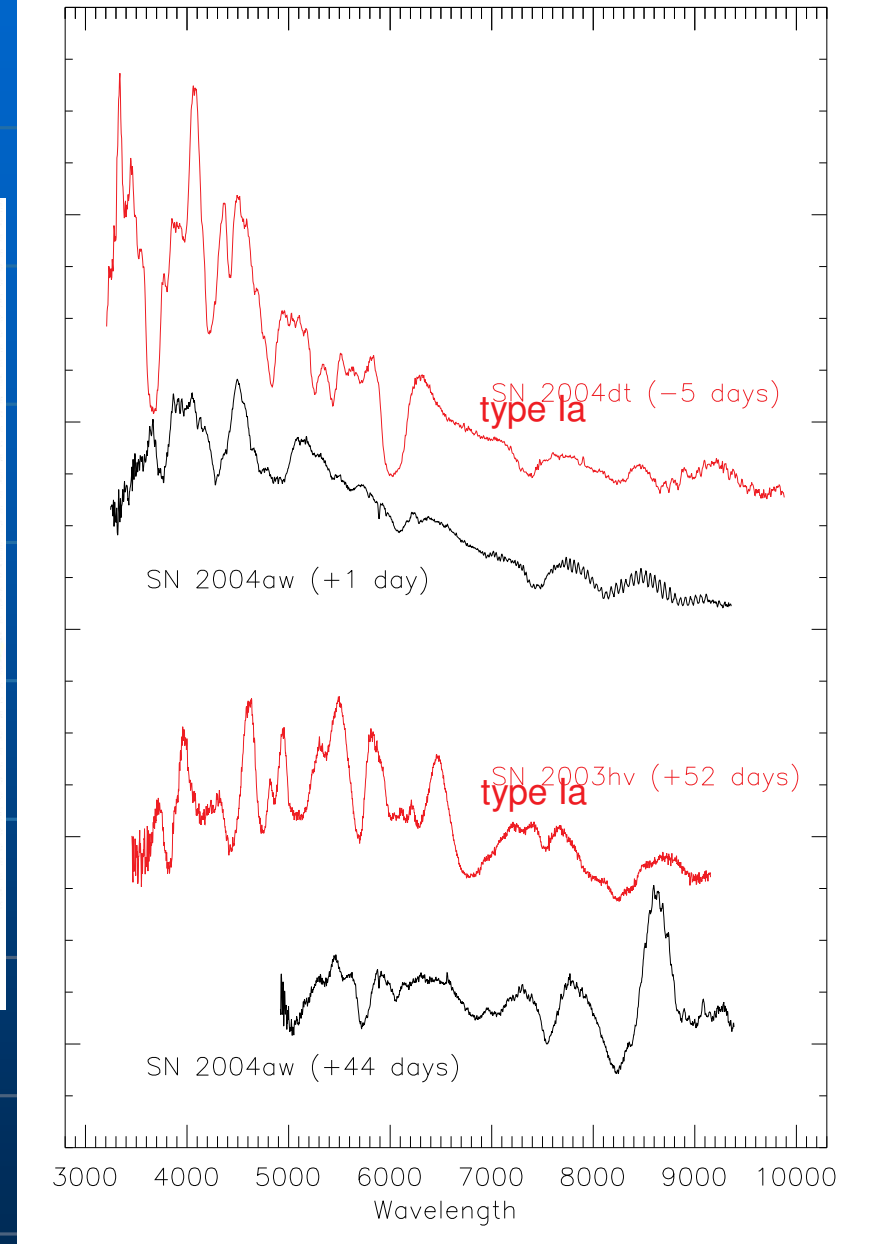
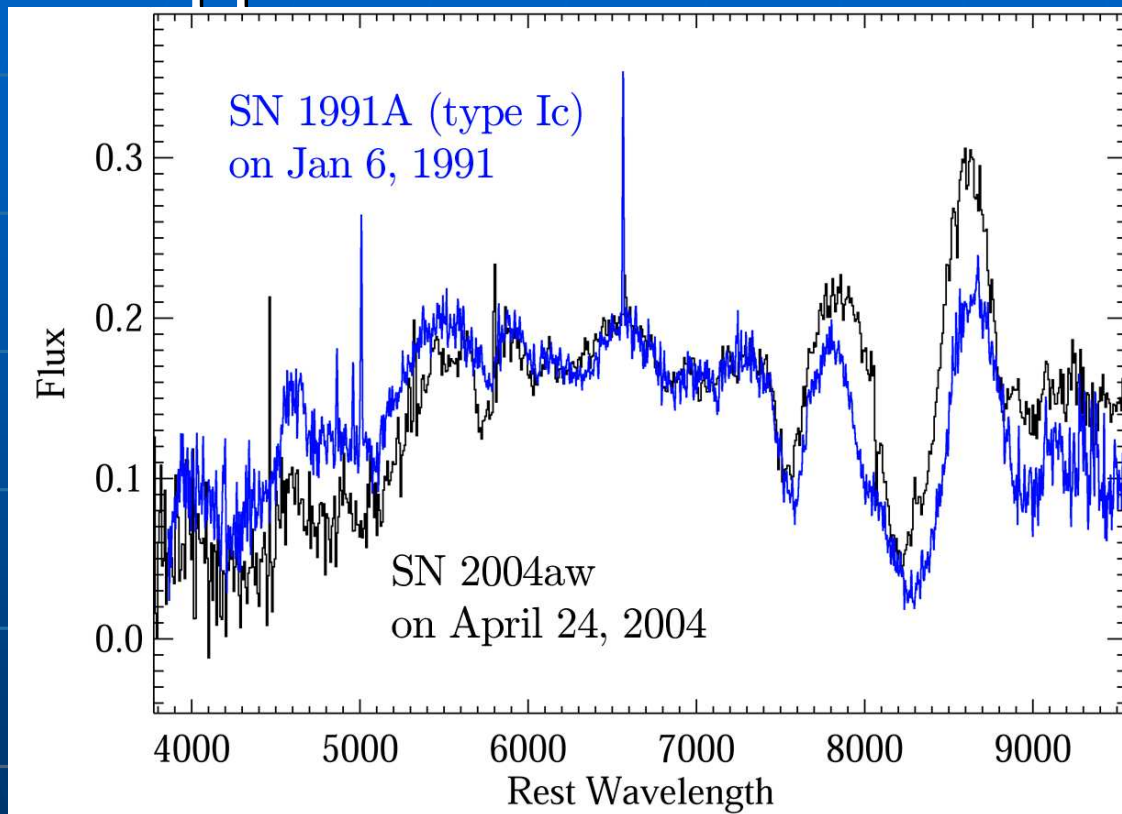
*Early spectrum of SN 2004aw*

(S. Benetti)

*... and SN 1991T*

n After one month of observations:

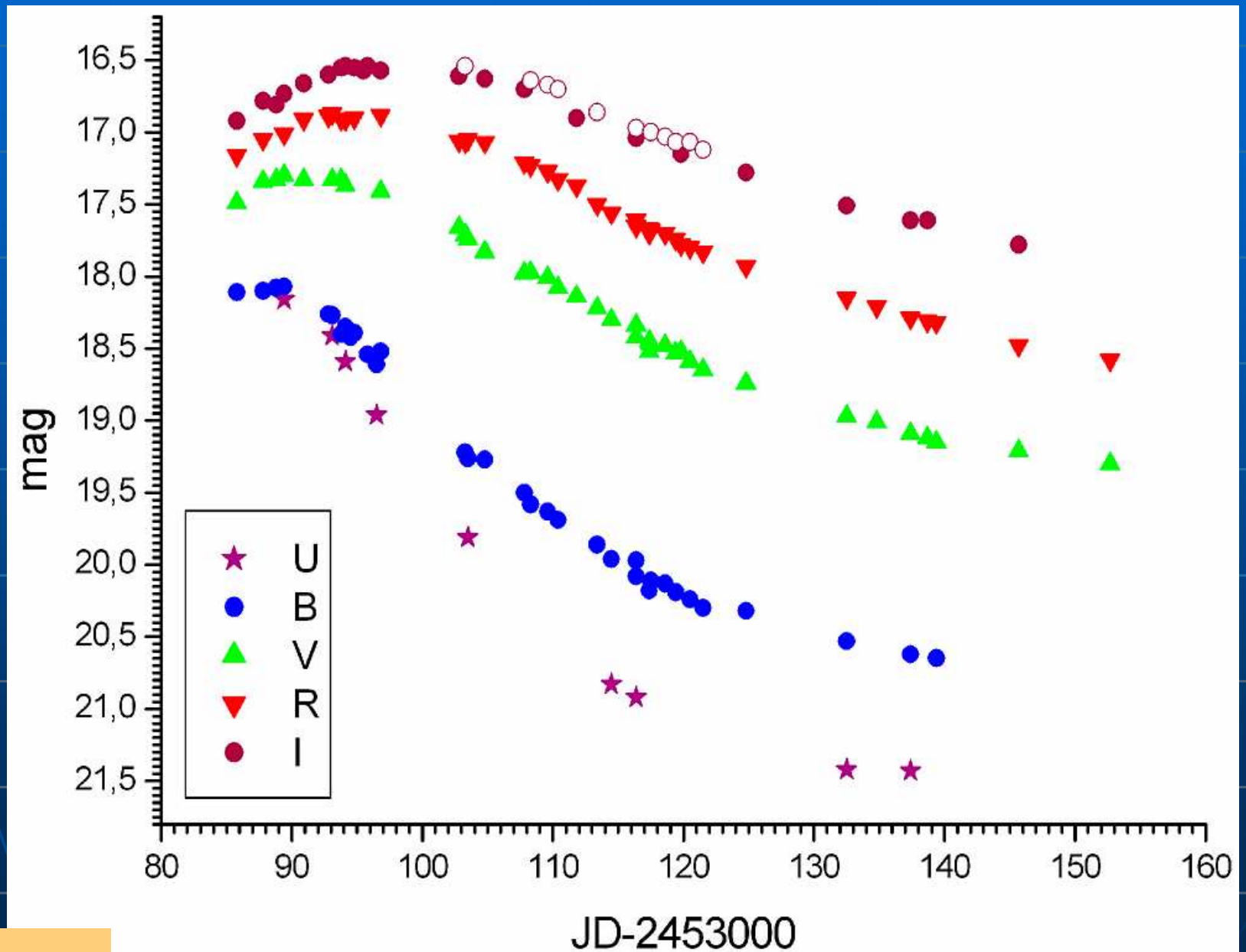
n Reclassification by Alex Filippenko



*It's a Ic !!!*

S. Taubenberger

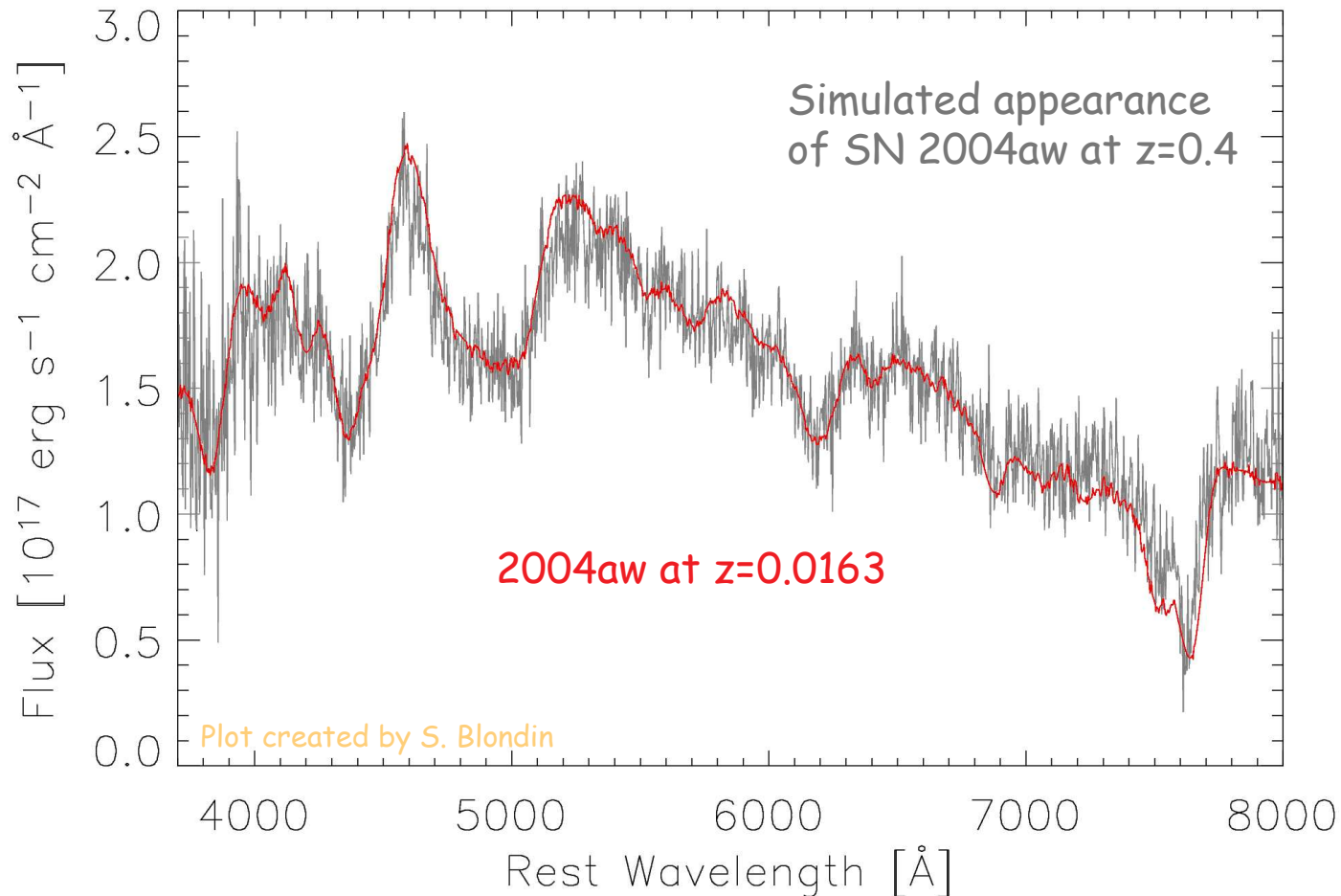
# Light curves of SN 2004aw



# Absolute magnitudes

- n For 2004aw extinction and distance highly uncertain:
  - $A(B) = 1.80$  mag and  $A(V) = 1.36$  mag from EW measurements
  - $\mu = 34.23$  from host galaxy recession velocity
  
- n Results for maximum brightness:
- n  $B = -17.95 \pm 0.47$  mag ,  $V = -18.26 \pm 0.39$  mag, ...  
(Errors almost arbitrary !)
  
- n For comparison:
  - peak luminosities of normal type Ia SNe  
 $B = -19.4$  mag and  $V = -19.4$  mag with scatter ( $\pm 0.3$  mag)
  - For type Ic SNe:  
 $B = -16.2 \dots -19.4$  mag and  $V = -16.7 \dots -19.8$  mag

# High-z sample contamination ?



+1.5 days  
spectrum

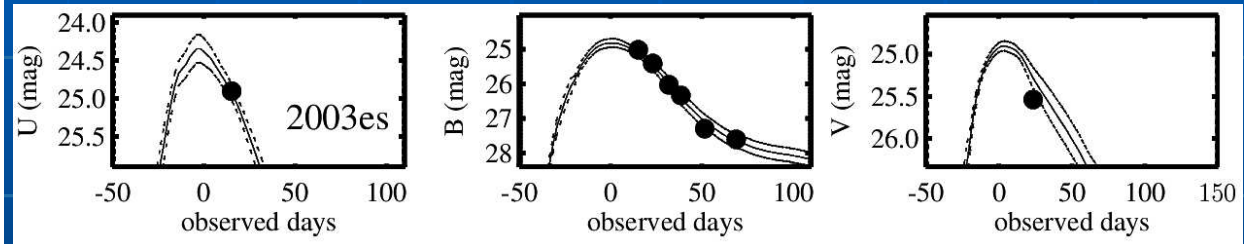
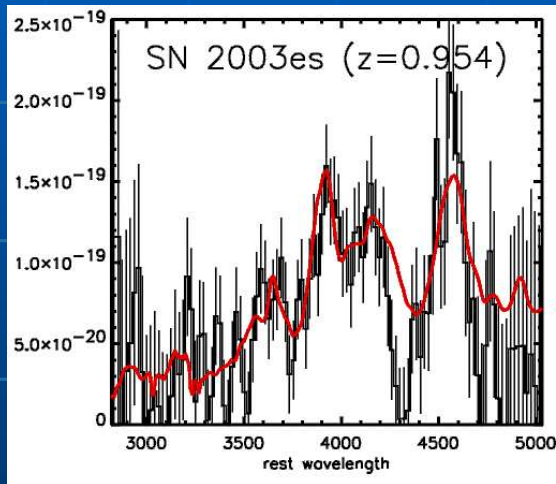
(S. Taubenberger)

n Result of a classification code of S. Blondin (for the  $z = 0.4$  case):

n best match: 1991T (Ia pec) @ +17.4d  
second best: 1992A (Ia) @ +9.0d  
third best: 1995D (Ia) @ +8.1d

# What does this mean?

- n Assume a hypothetical 2004aw at  $z = 0.4$  and UNREDDENED (otherwise too faint)
- n Typical dataset obtained for such SNe:  
one spectrum + sparse photometry in 2 or 3 filters



Figures from Ries et al. 2004

- n 2004aw would be classified as Ia (pec) according to the spectrum
- n B-V color determined, result: 0.28 mag (instead of -0.05 mag for a typical type Ia)

- n Mis-interpreted as extinction, correction for  $E(B-V) = 0.33$  applied
- n This brings 2004aw to absolute magnitudes of **-19.3** in B and V
- n Similar to type Ia SNe, aligns rather well in the Hubble diagram  
**But: Only by chance !**
- n Of course the procedure is much more complex and sophisticated in reality.
- n Nevertheless: the danger of contamination remains!



# Summary (Part III)

- n Type II supernovae are good distance indicators out to a few Mpc.
- n They measure absolute distances without any calibration!
- n Type Ia supernovae are very good distance indicators in the local Universe .
- n They allow to measure relative distances very accurately (after calibration).
- n They provide the best distance indicators for cosmological distances if systematic errors can be controlled.