

WMAP 5-Year Observations: Cosmological Interpretation

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CITA, March 11, 2008

WMAP 5-Year Papers

- **Hinshaw et al.**, “*Data Processing, Sky Maps, and Basic Results*” [0803.0732](#)
- **Hill et al.**, “*Beam Maps and Window Functions*” [0803.0570](#)
- **Gold et al.**, “*Galactic Foreground Emission*” [0803.0715](#)
- **Wright et al.**, “*Source Catalogue*” [0803.0577](#)
- **Nolta et al.**, “*Angular Power Spectra*” [0803.0593](#)
- **Dunkley et al.**, “*Likelihoods and Parameters from the WMAP data*” [0803.0586](#)
- **Komatsu et al.**, “*Cosmological Interpretation*” [0803.0547](#)

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Special
Thanks to
WMAP
Graduates!

- C. Barnes
- R. Bean
- O. Dore
- H.V. Peiris
- L. Verde

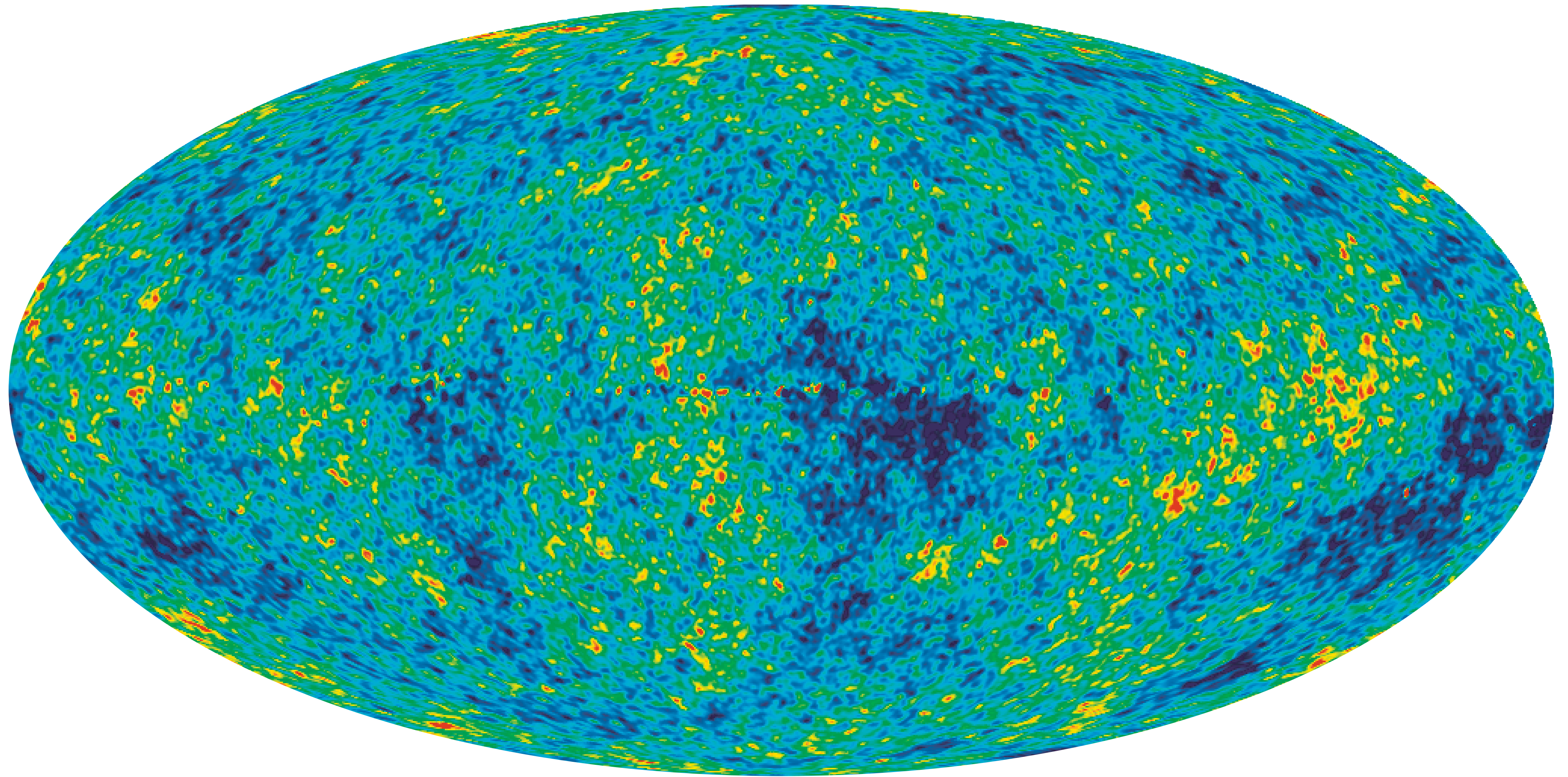
WMAP 5-Year Press Release

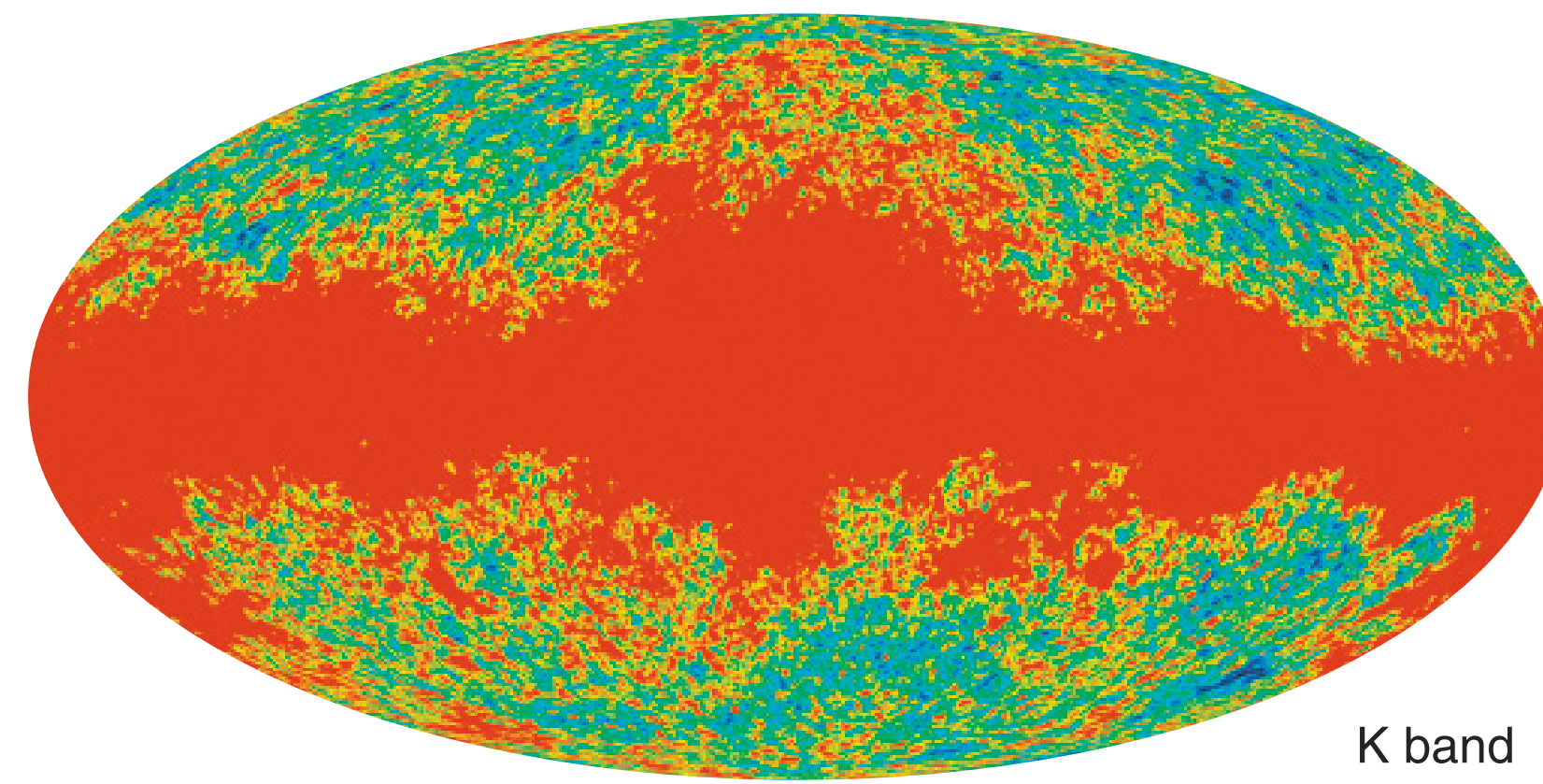
On March 7, 2008

- Evidence for the cosmic neutrino background from the WMAP data alone
- Instantaneous reionization at $z_{\text{reion}}=6$ is excluded at the 3.5 sigma level
- The tightest constraints on inflation models to date

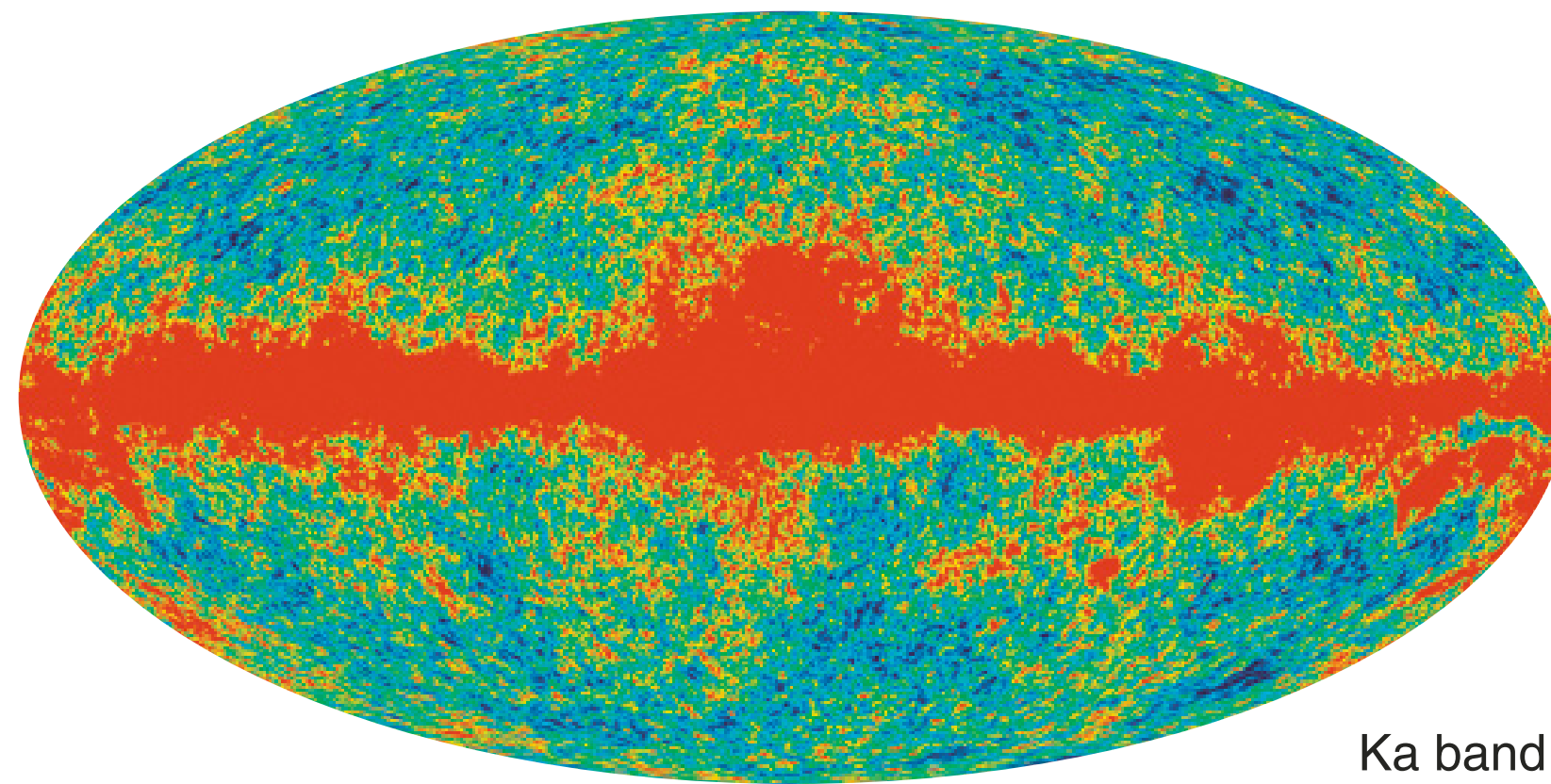
WMAP 5-Year Data

Hinshaw et al.

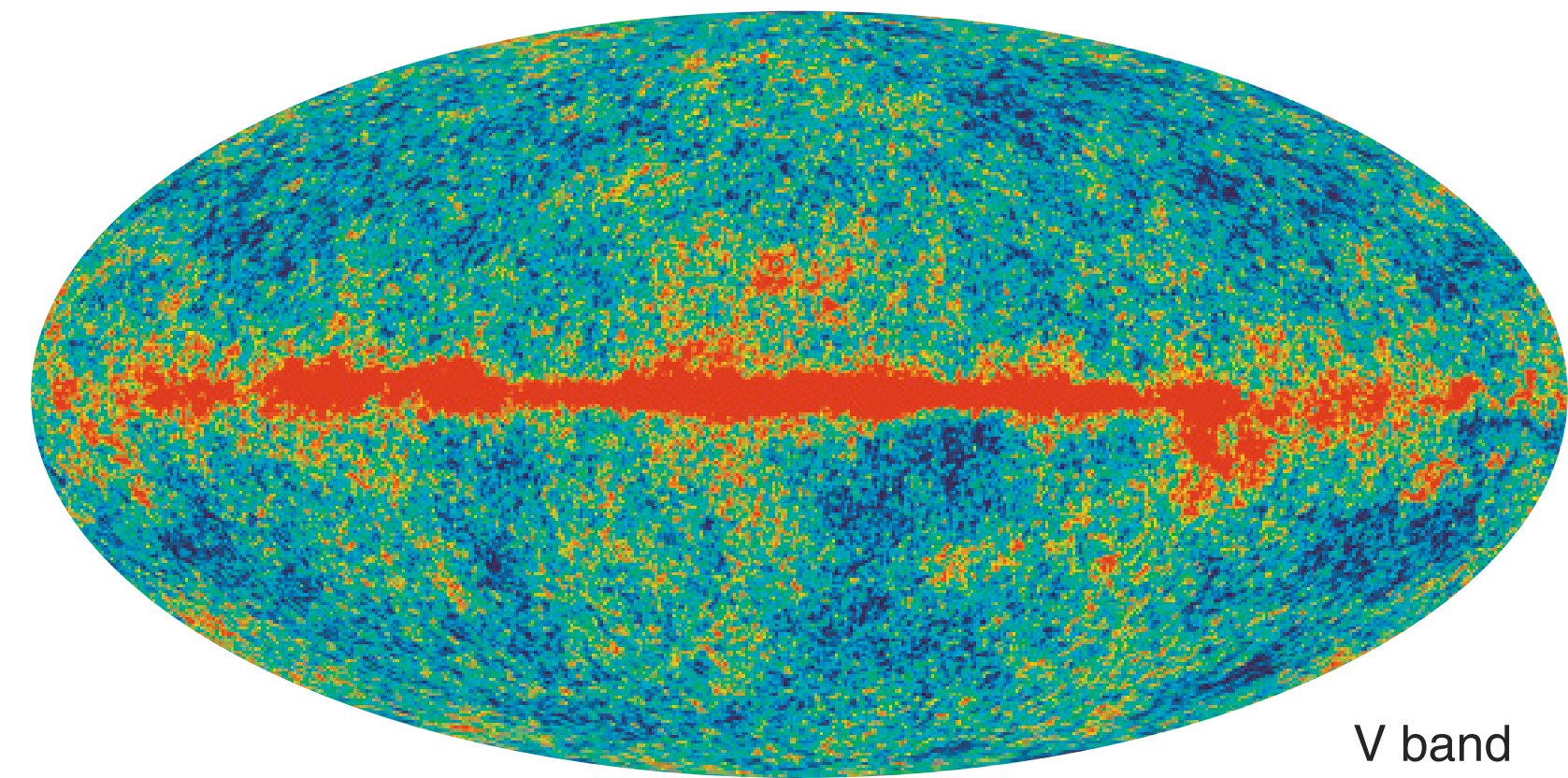




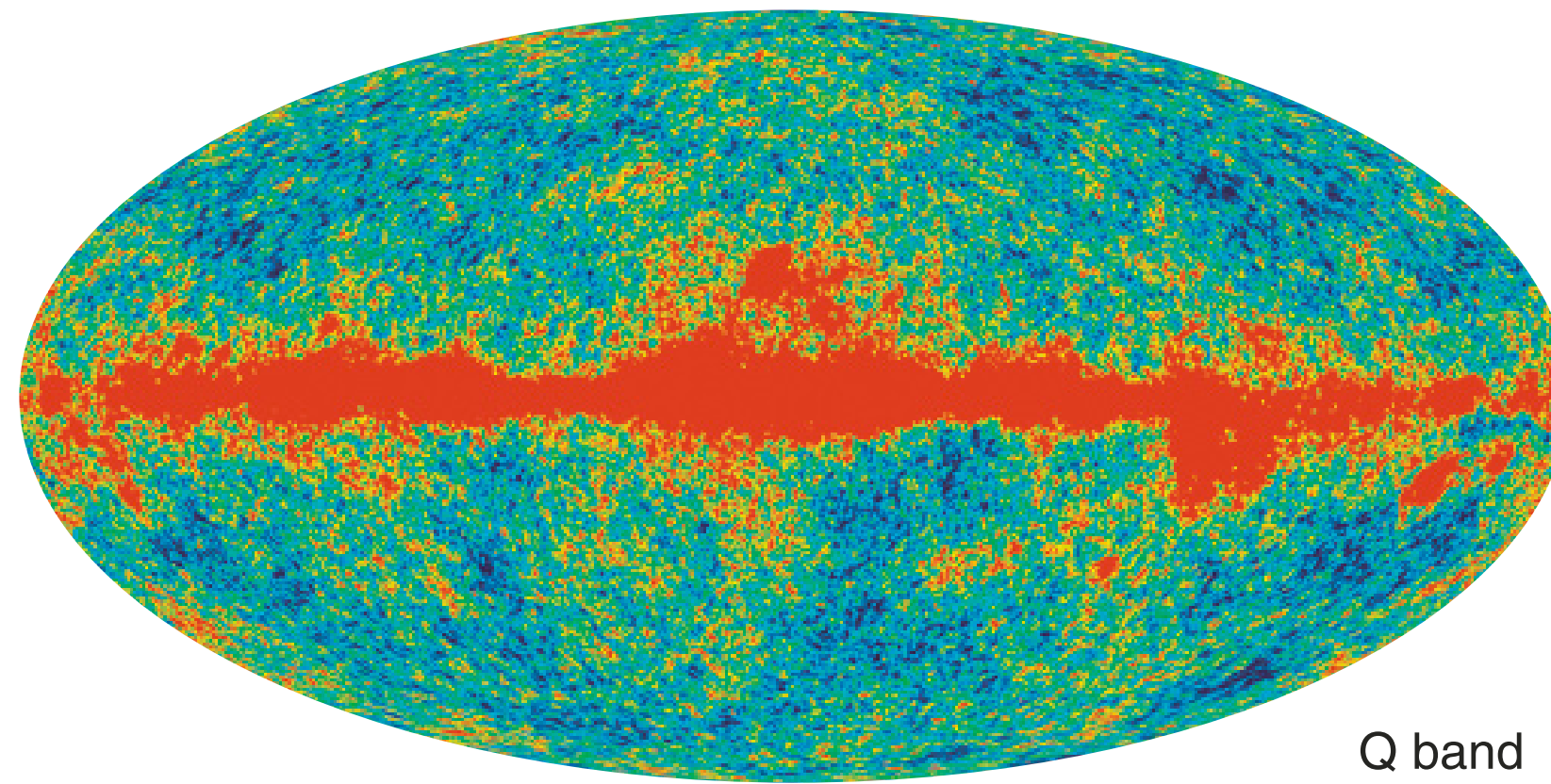
K band



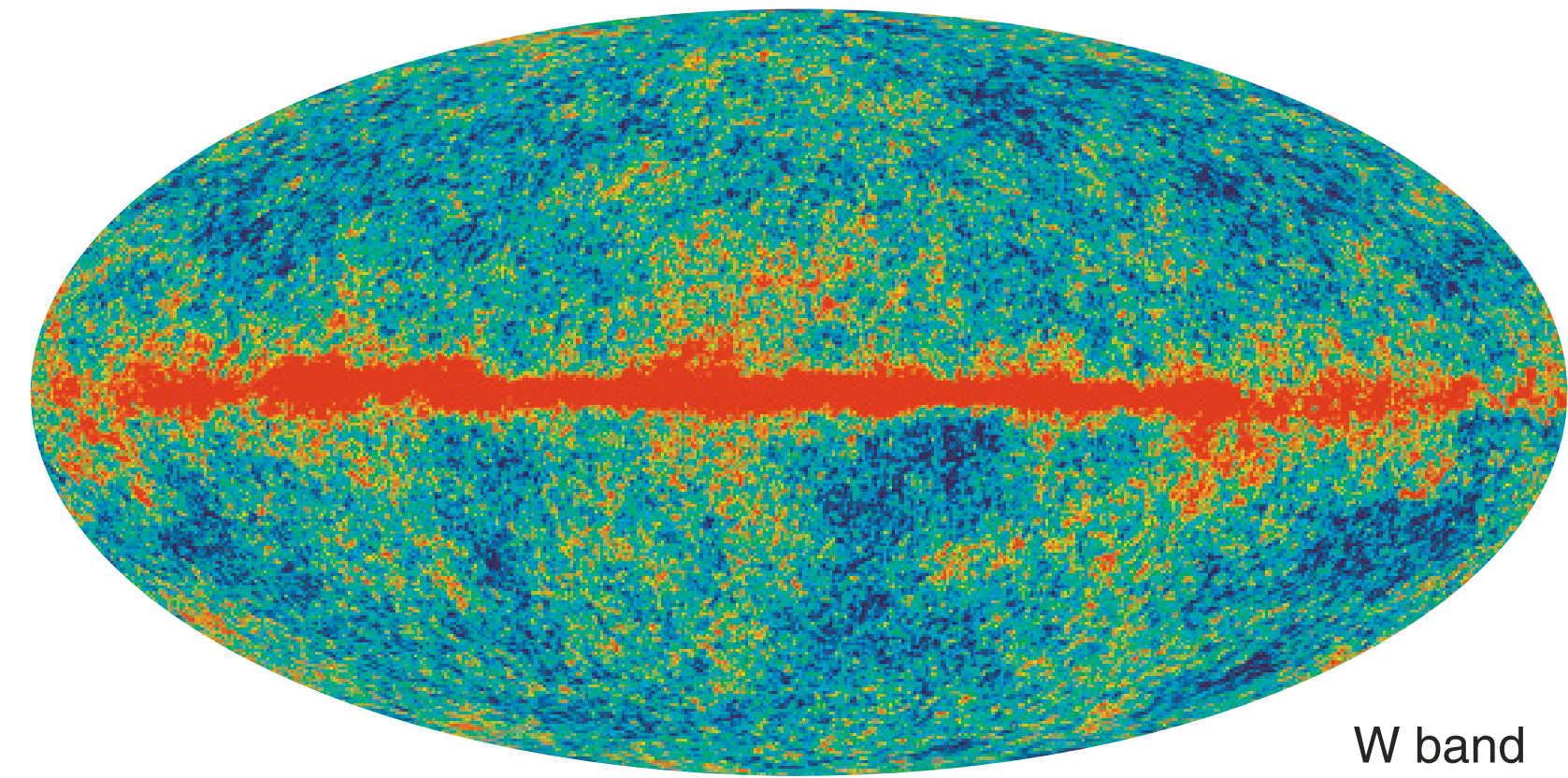
Ka band



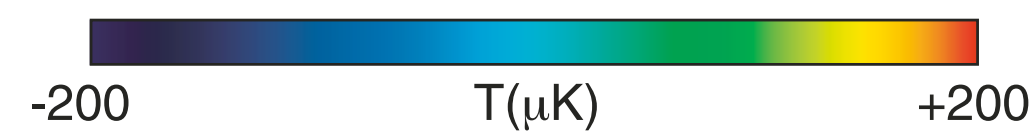
V band



Q band



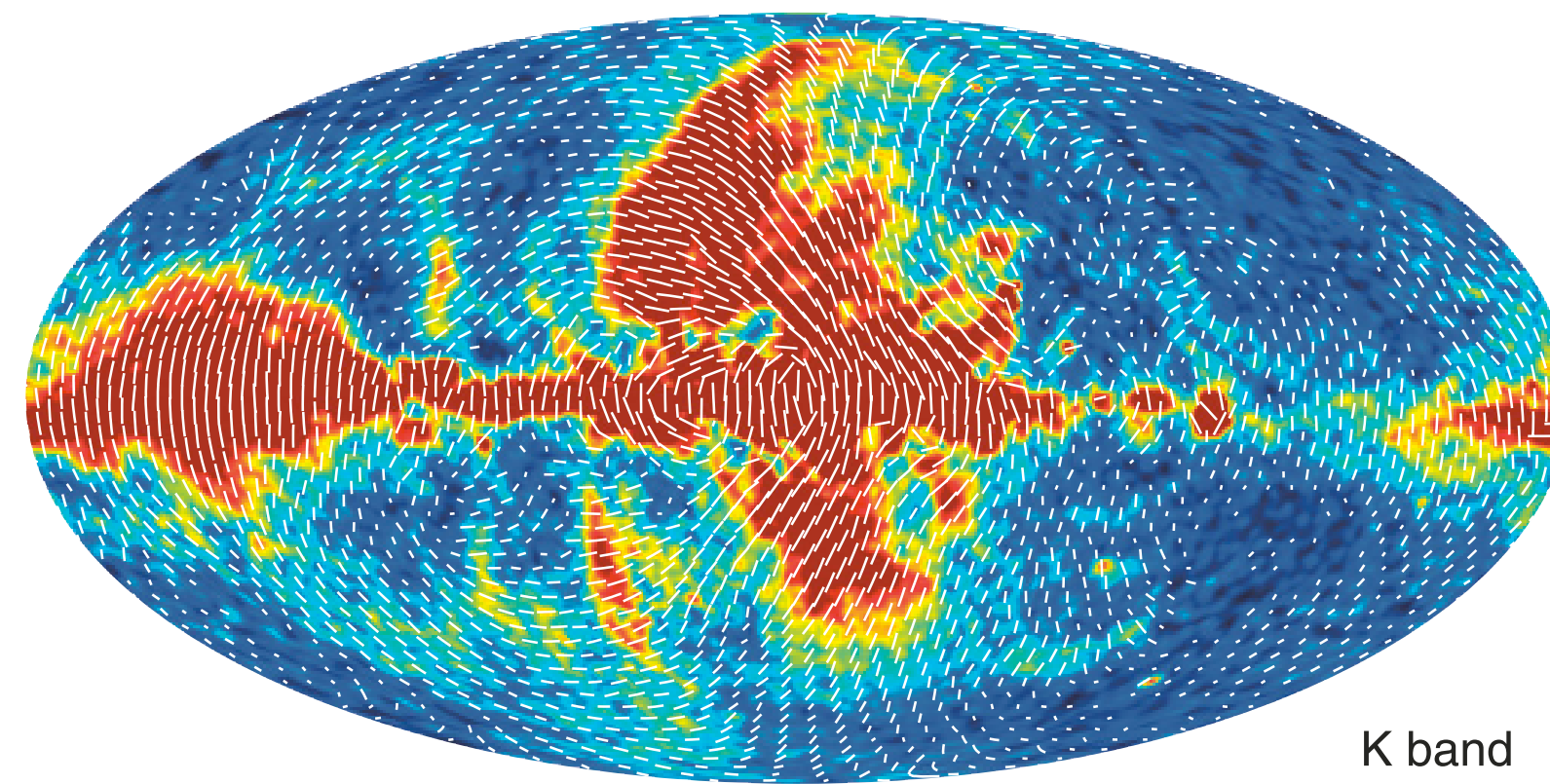
W band



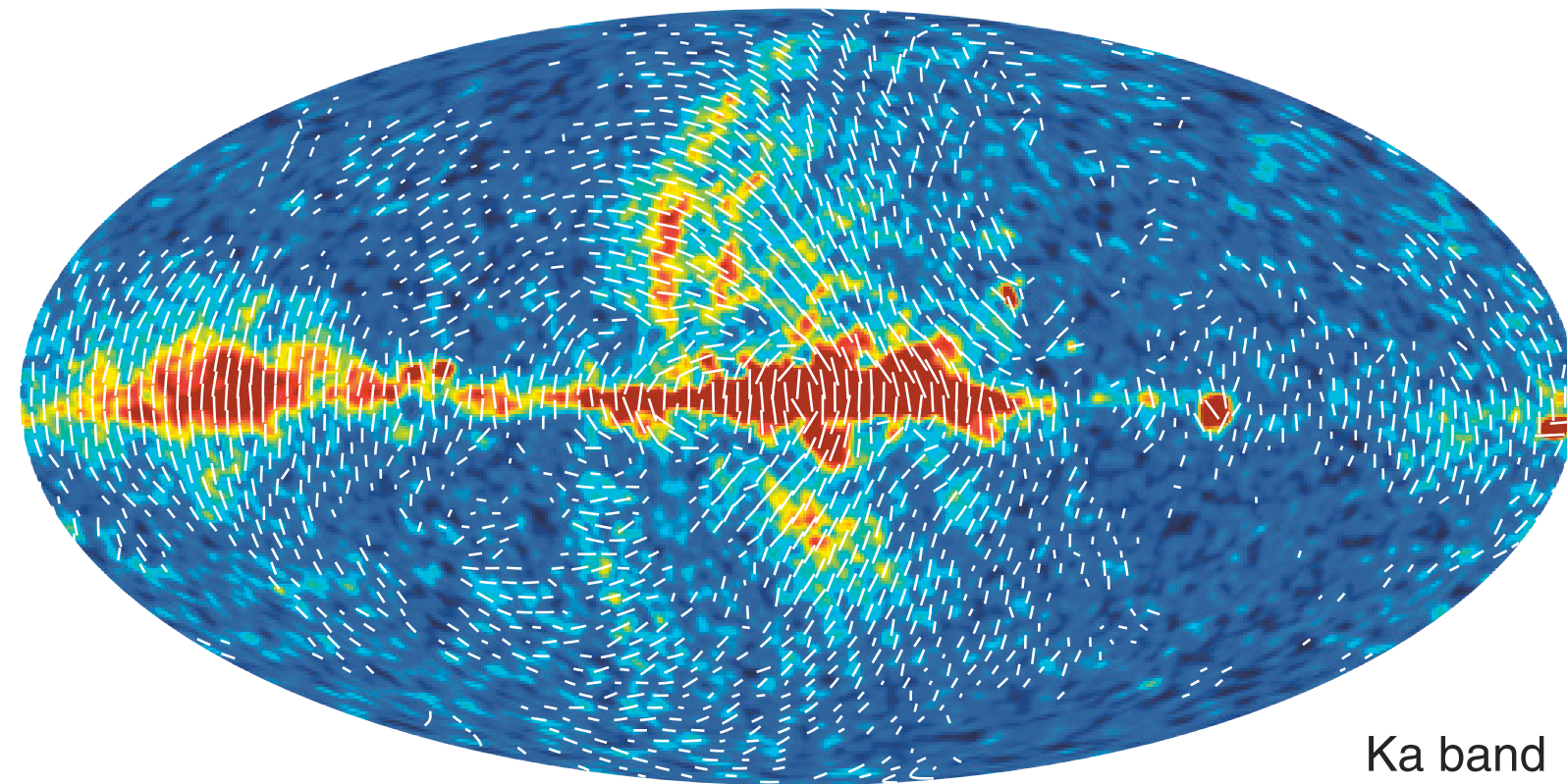
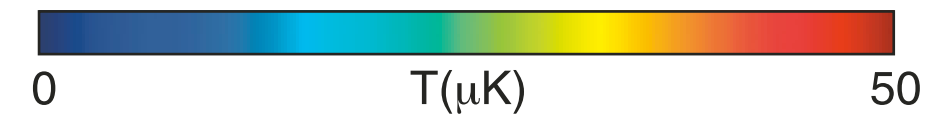
-200

$T(\mu\text{K})$

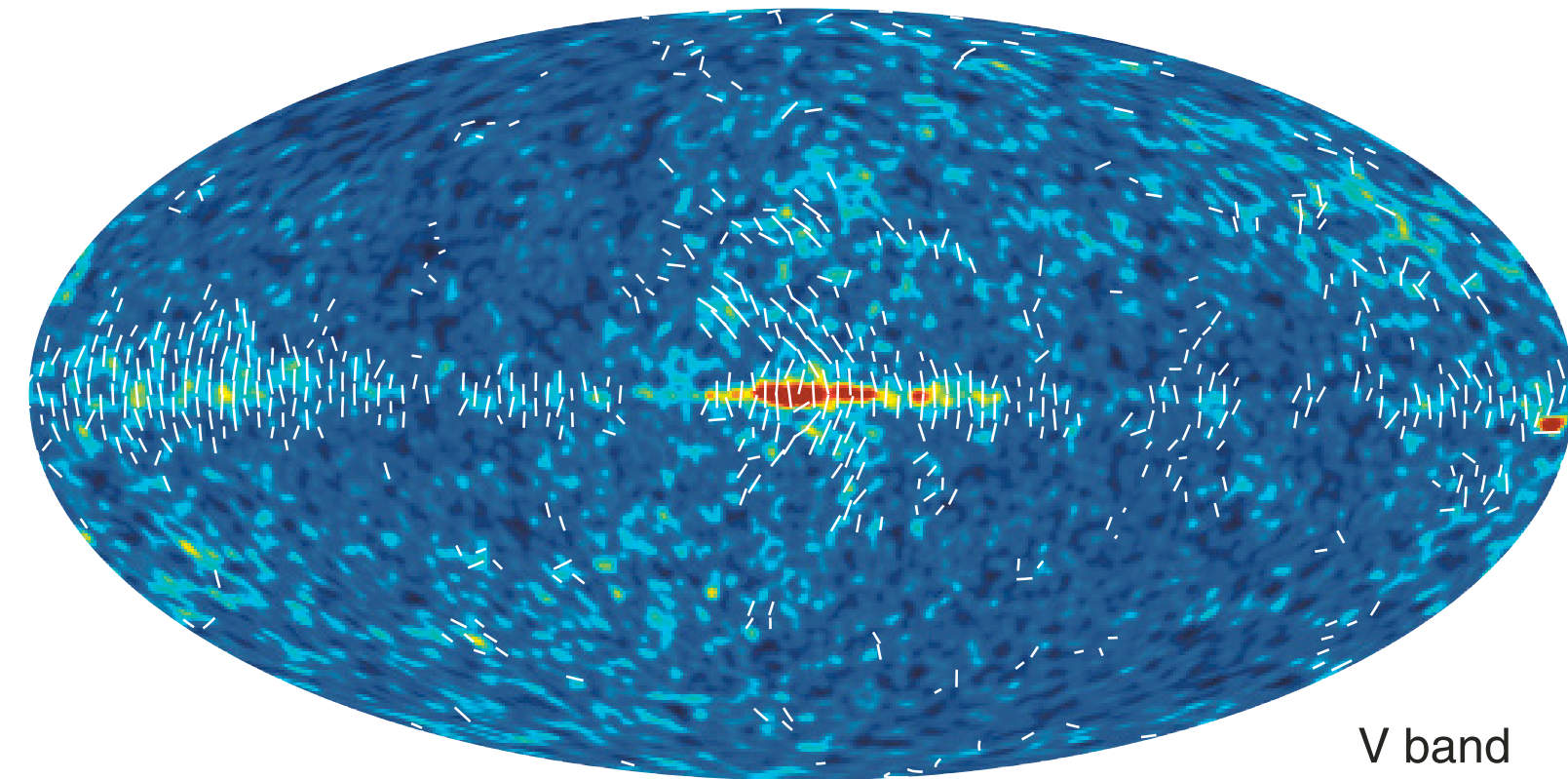
+200



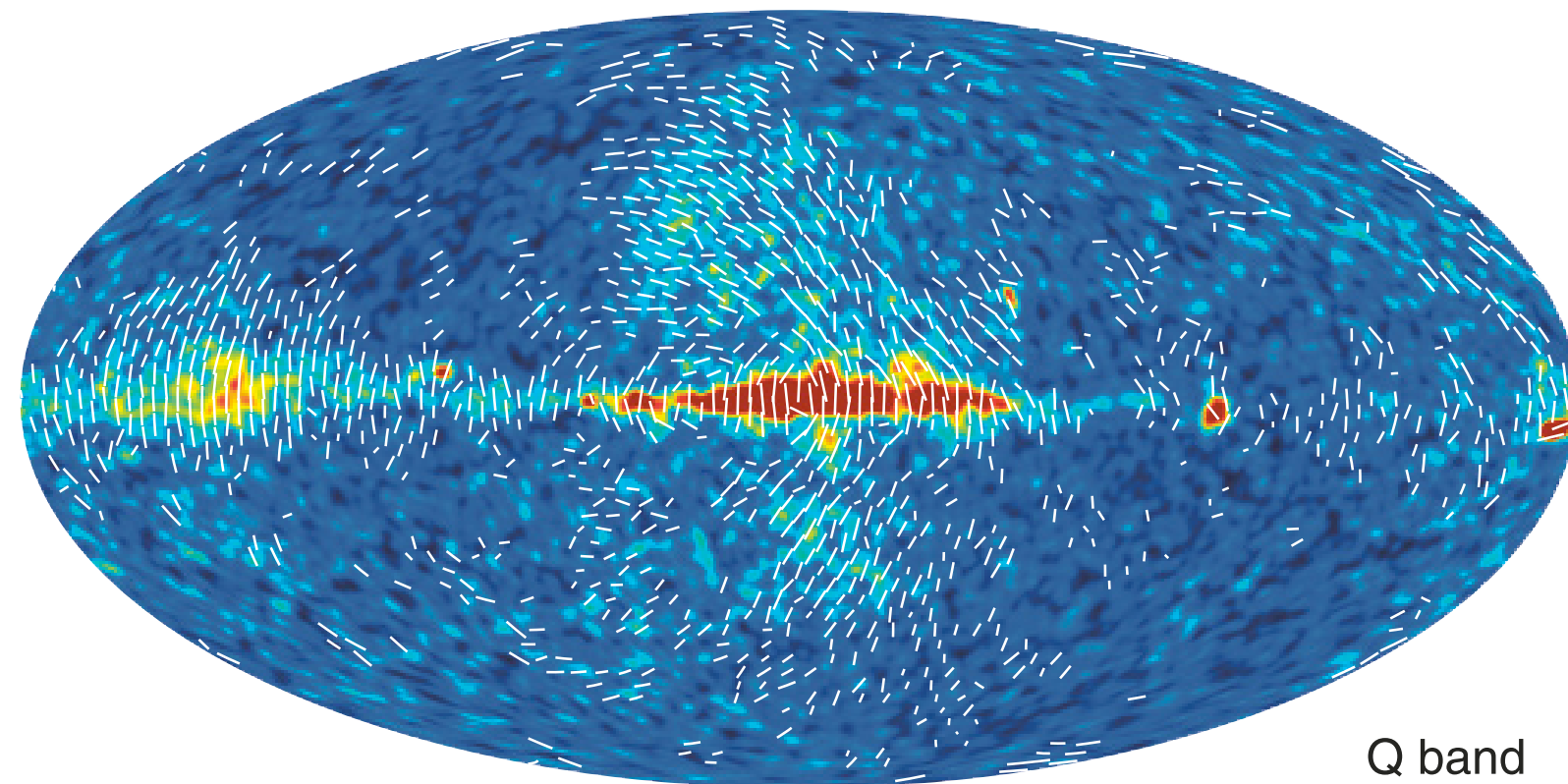
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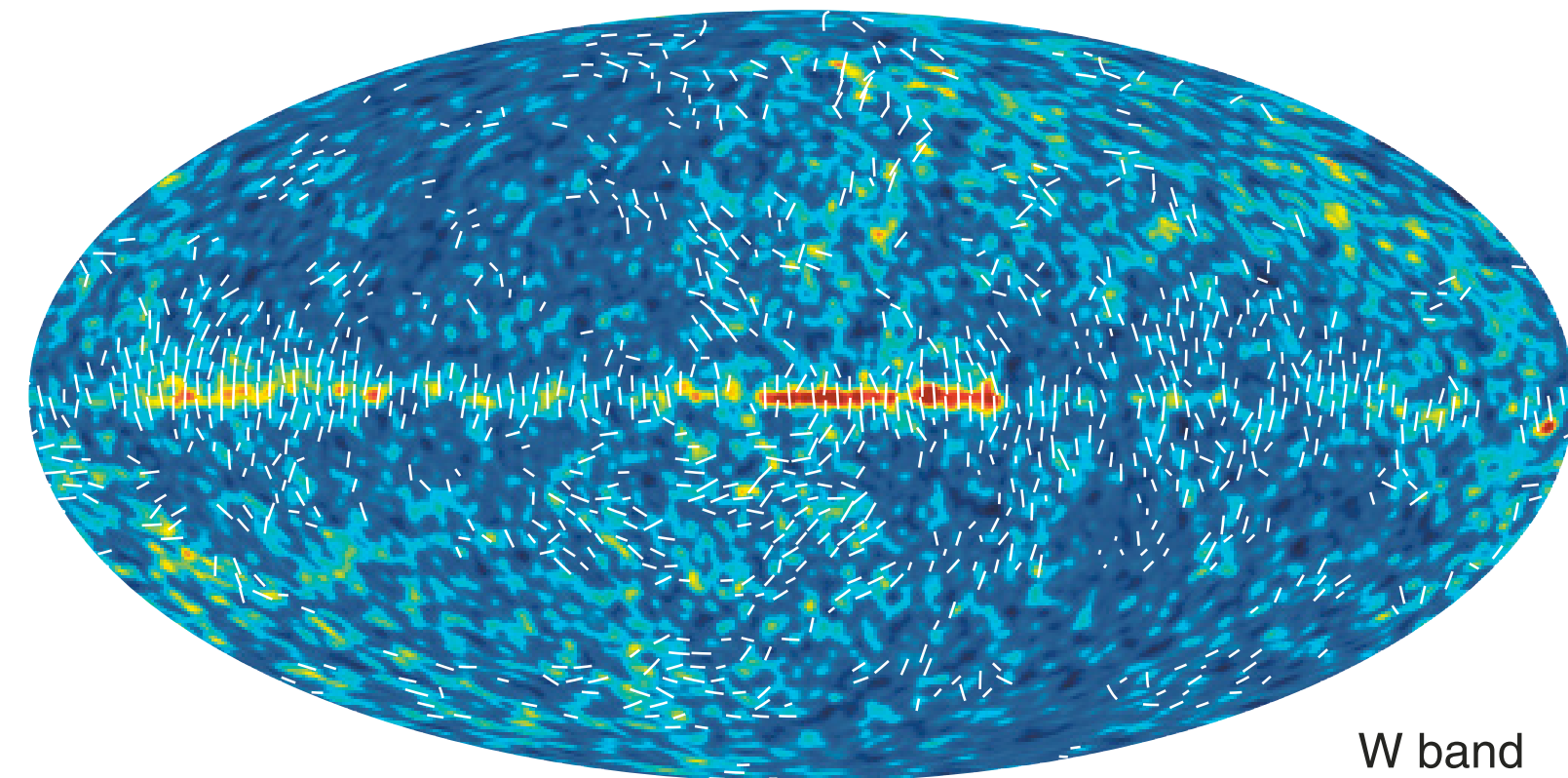
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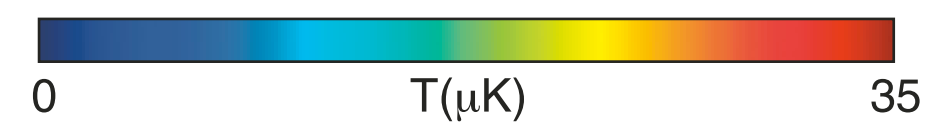
V band



Q band



W band

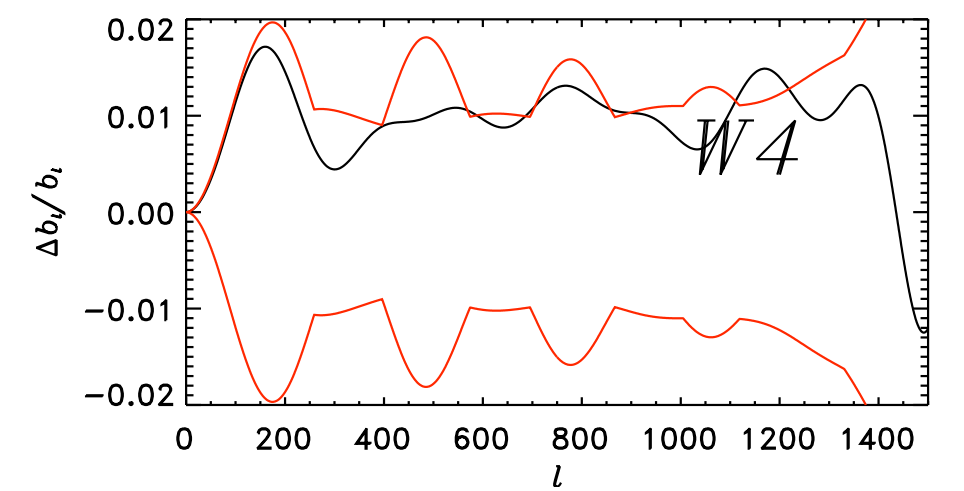
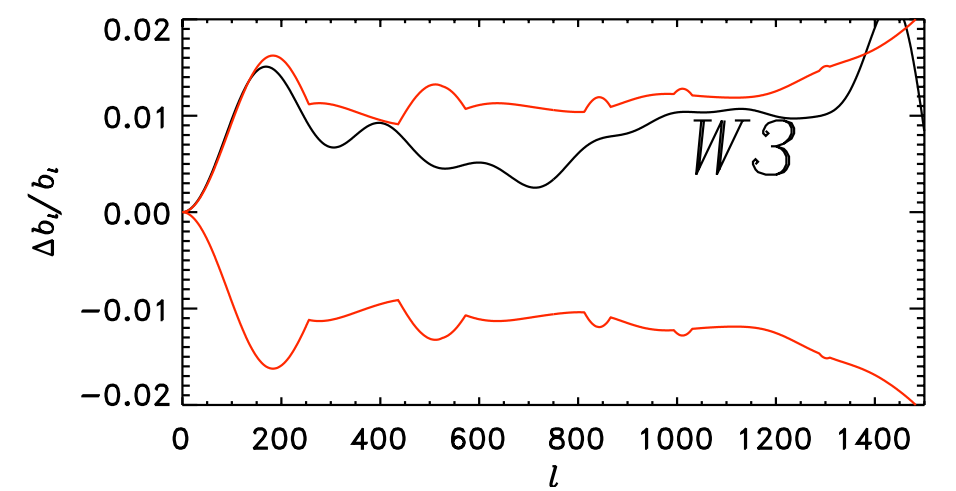
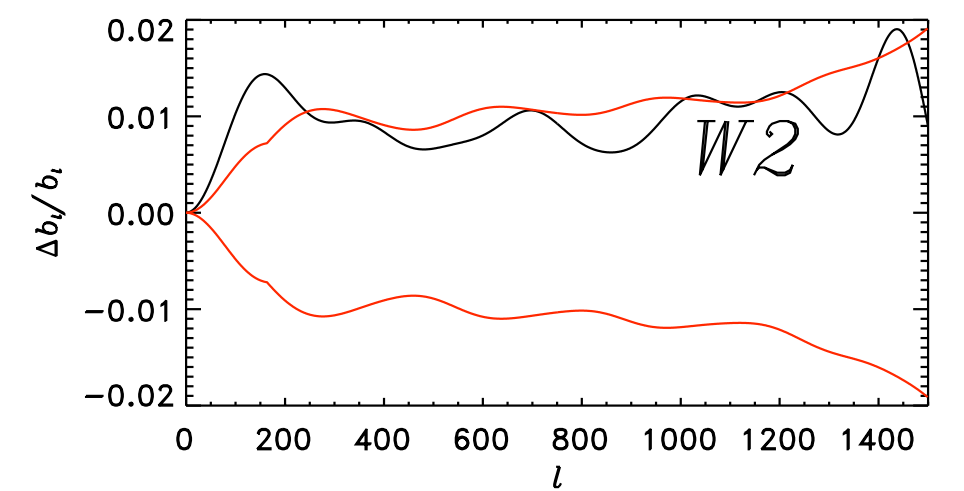
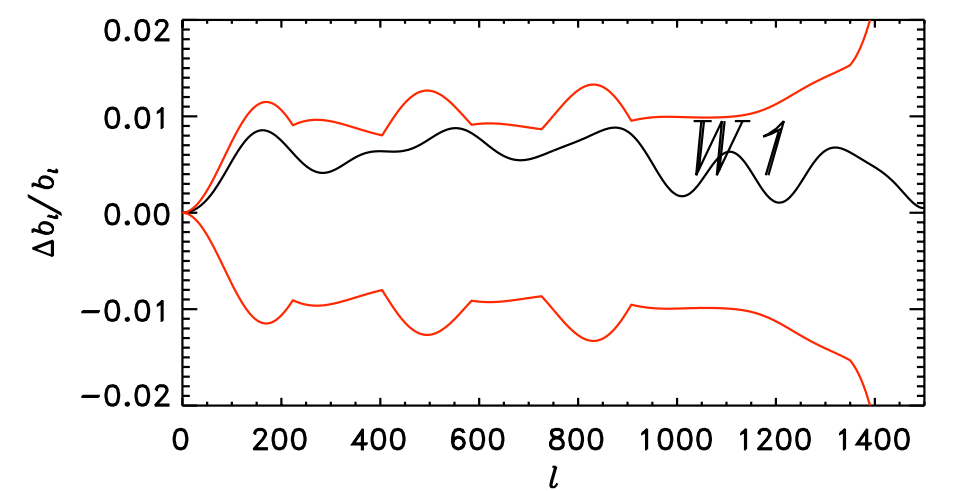
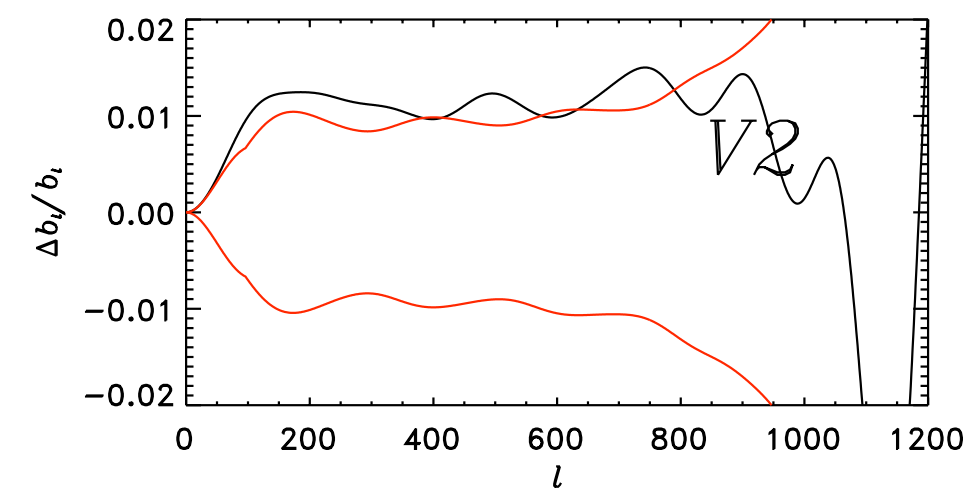
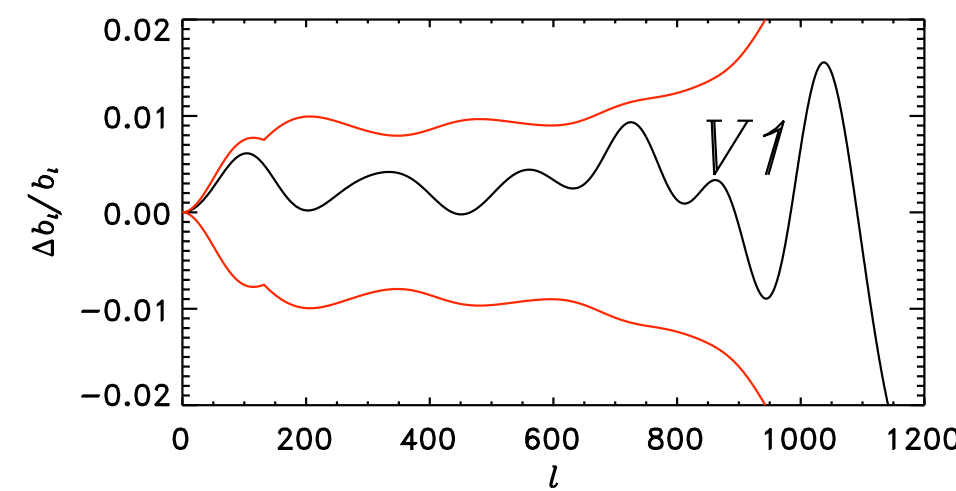
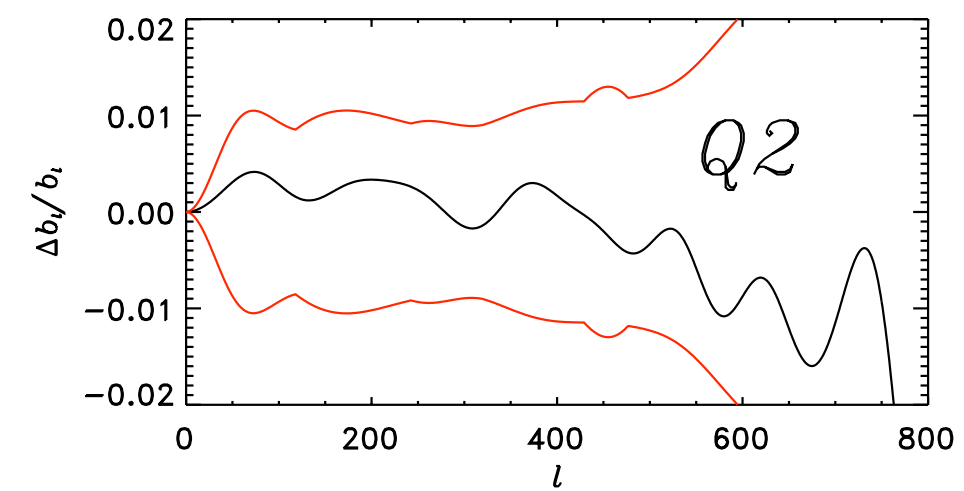
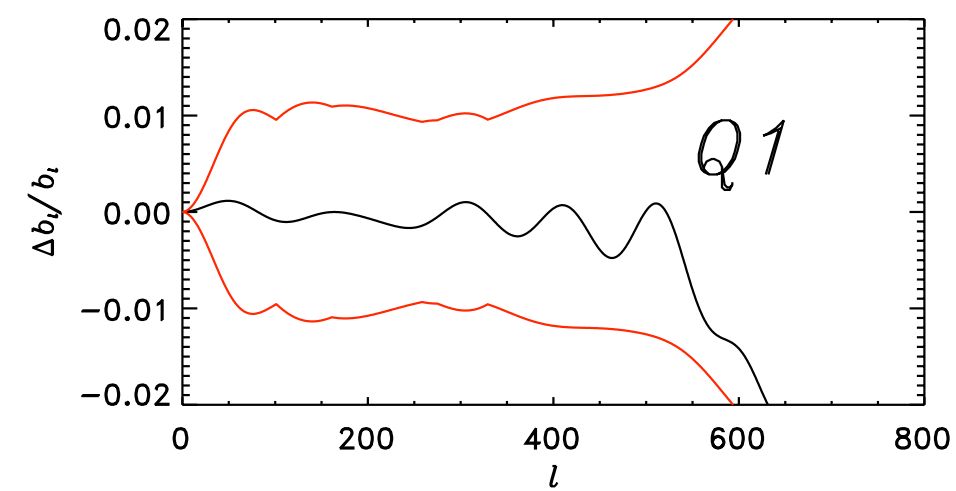
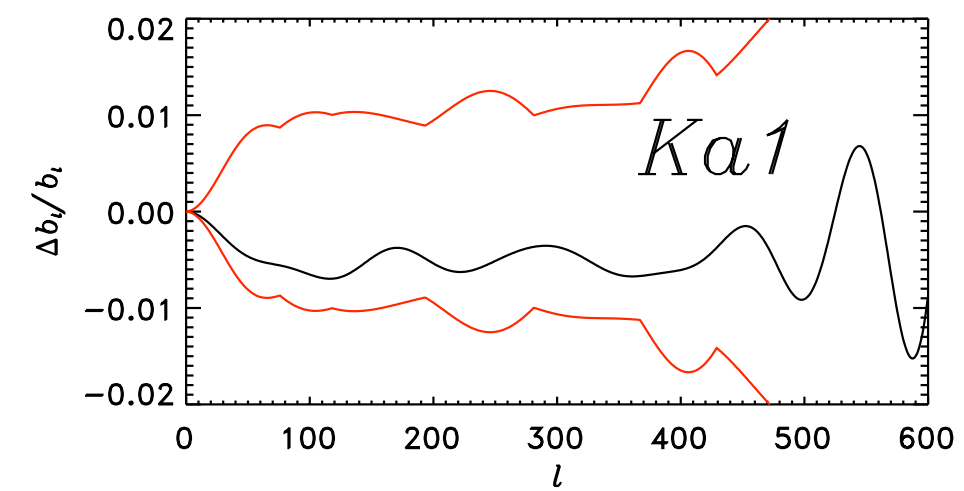
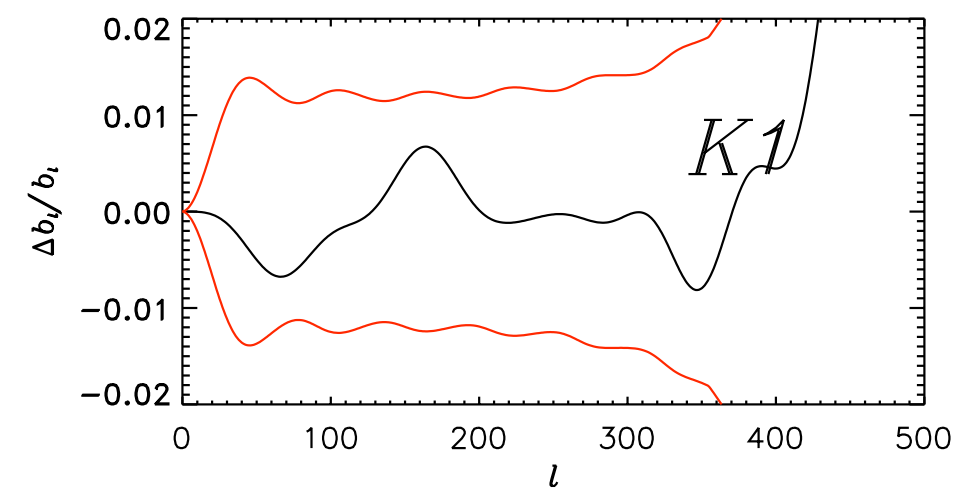


Improved Data/Analysis

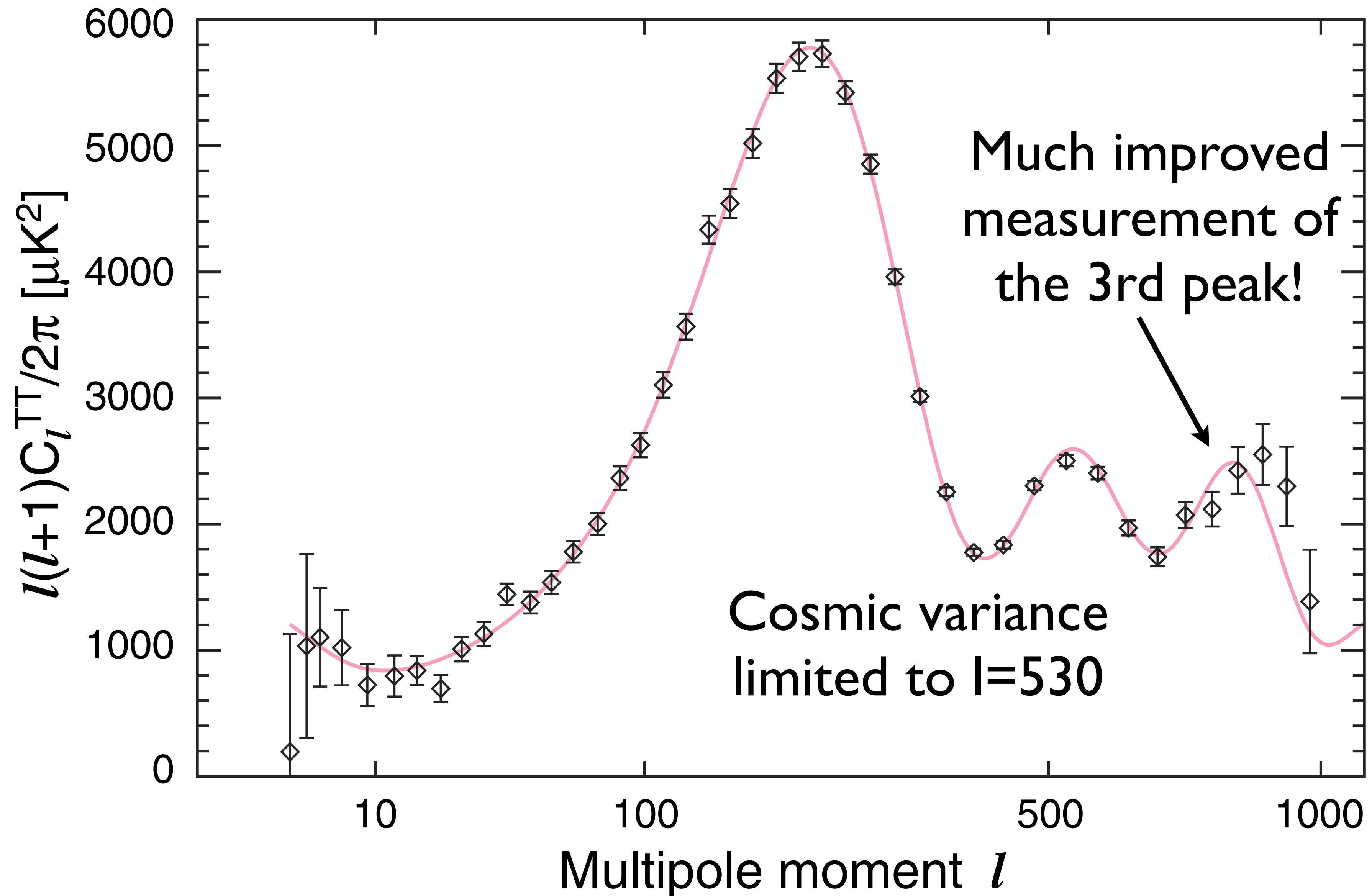
- Improved Beam Model
 - 5 years of the Jupiter data, combined with the extensive physical optics modeling, reduced the beam uncertainty by a factor of 2 to 4.
- Improved Calibration
 - Improved algorithm for the gain calibration from the CMB dipole reduced the calibration error from 0.5% to 0.2%
- More Polarization Data Usable for Cosmology
 - We use the polarization data in Ka band. (We only used Q and V bands for the 3-year analysis.)

New Beam

- The difference between the 5-year beam and the 3-year beam (shown in black: **3yr minus 5yr beam**) is within ~ 1 sigma of **the 3-year beam errors (shown in red)**
- We use V and W bands for the temperature power spectrum, C_l
 - Power spectrum depends on the beam²
 - **The 5-year C_l is $\sim 2.5\%$ larger than the 3-year C_l at $l > 200$**

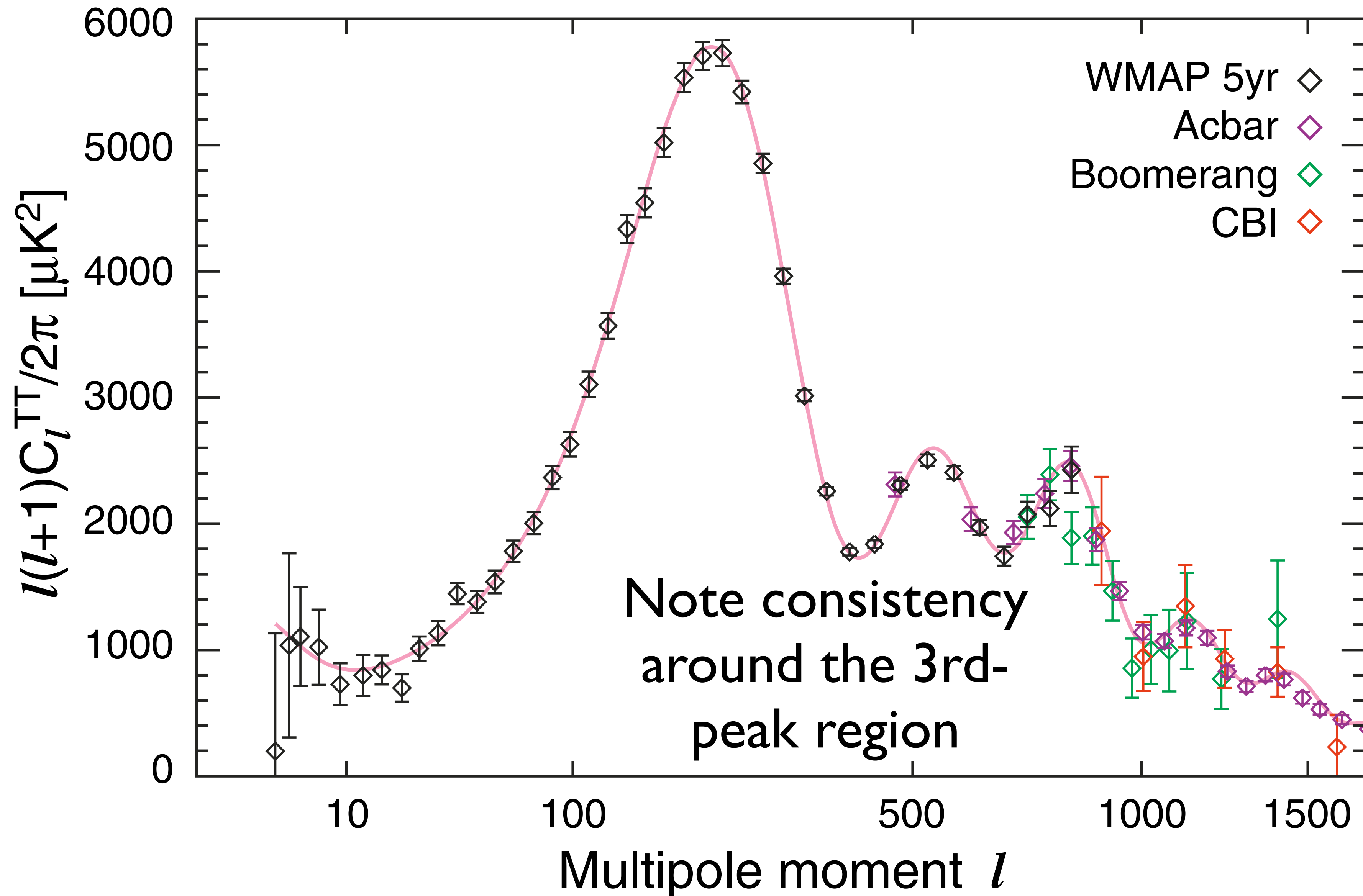


The 5-Year C_l

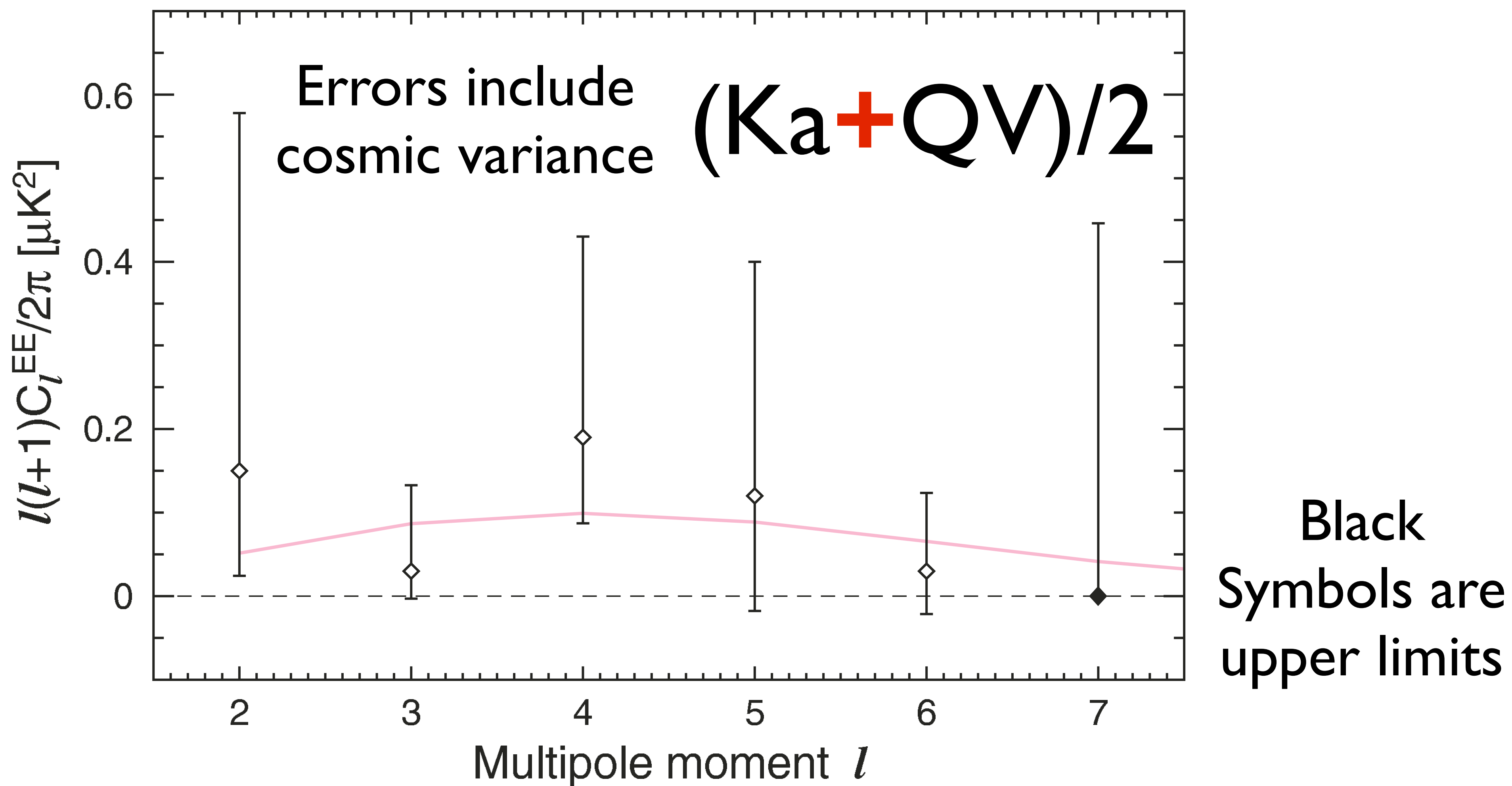


The 5-Year C_l

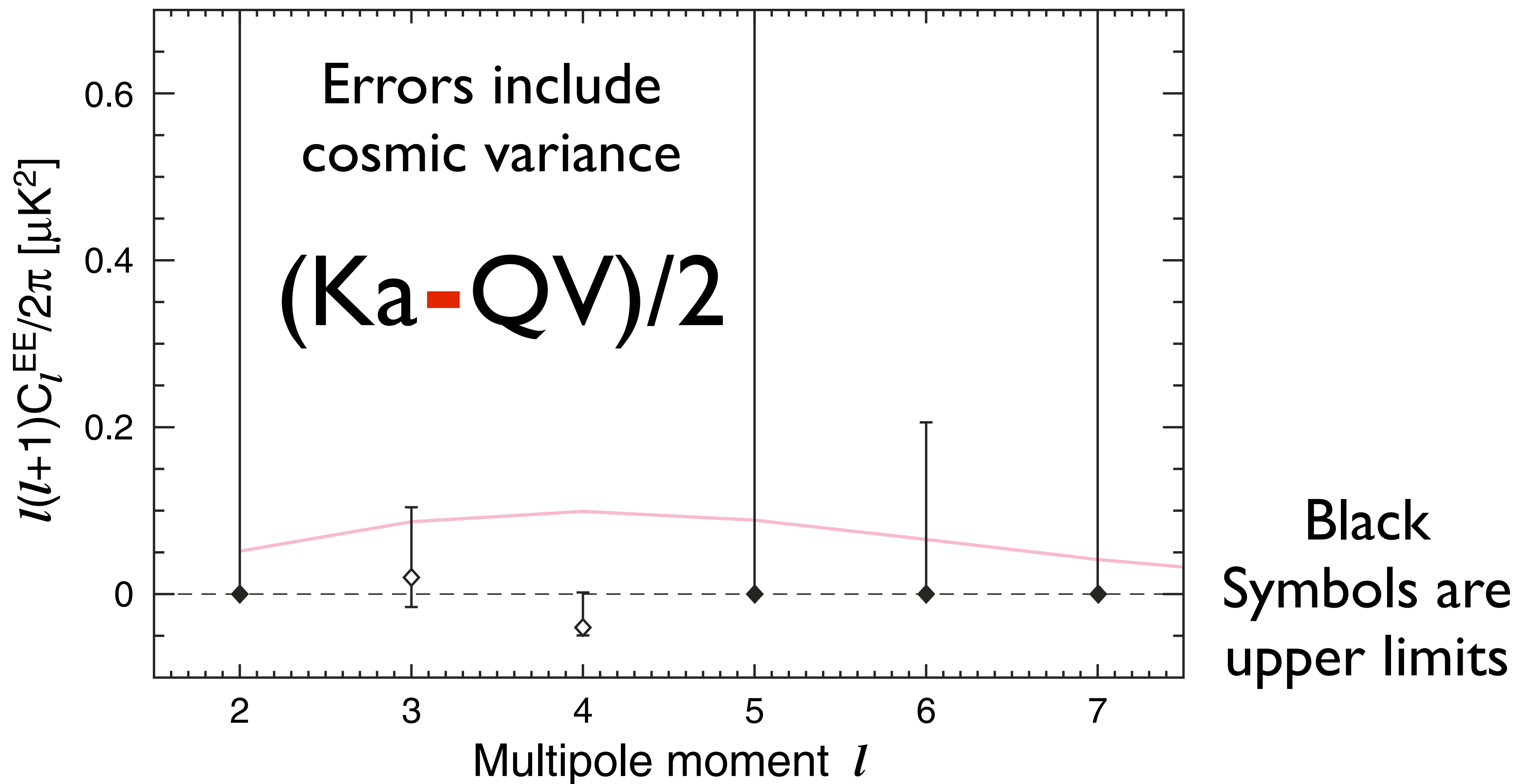
Nolta et al.



Adding Polarization in Ka: OK? Look at C_l^{EE}

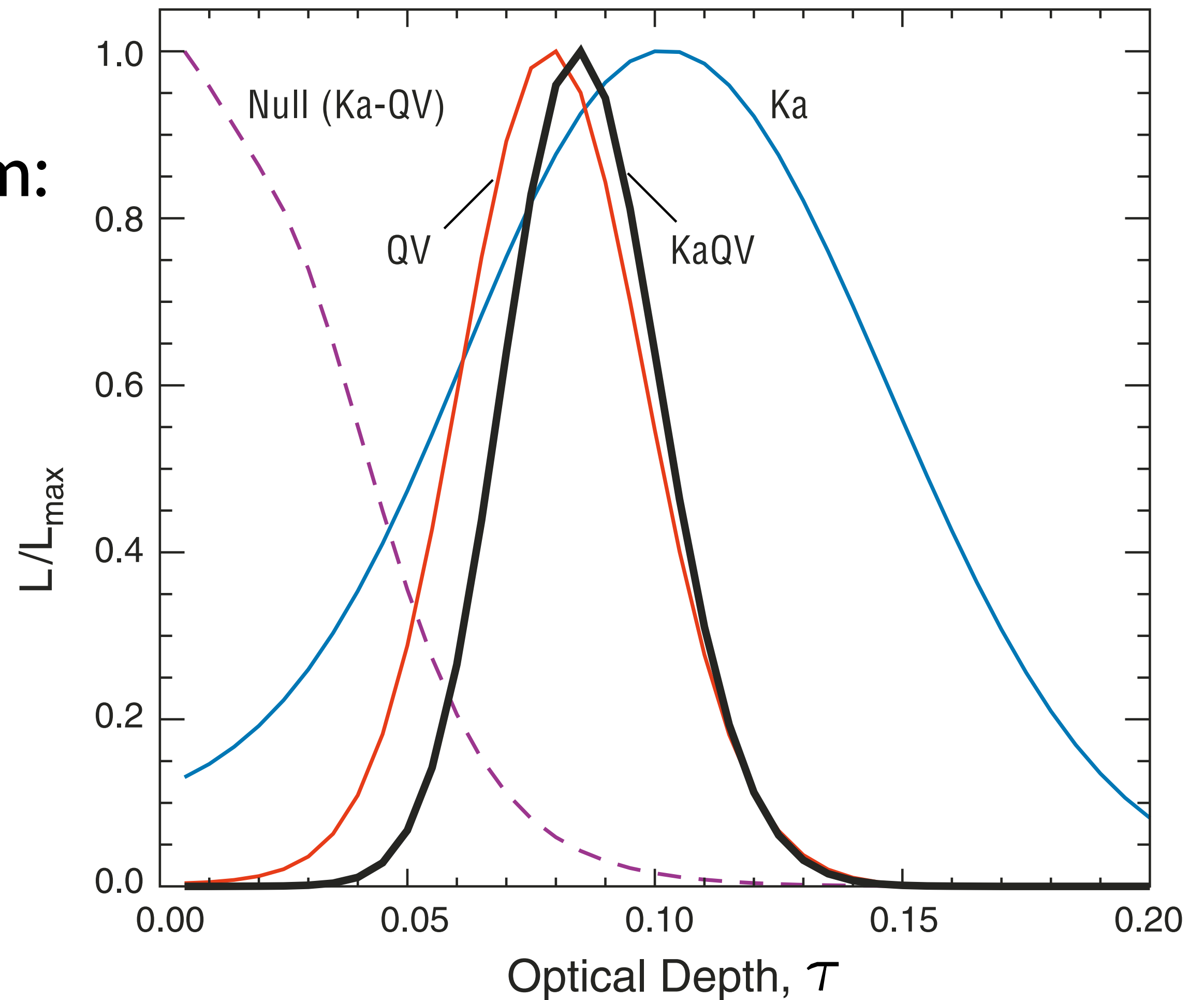


Adding Polarization in Ka: Passed the Null Test



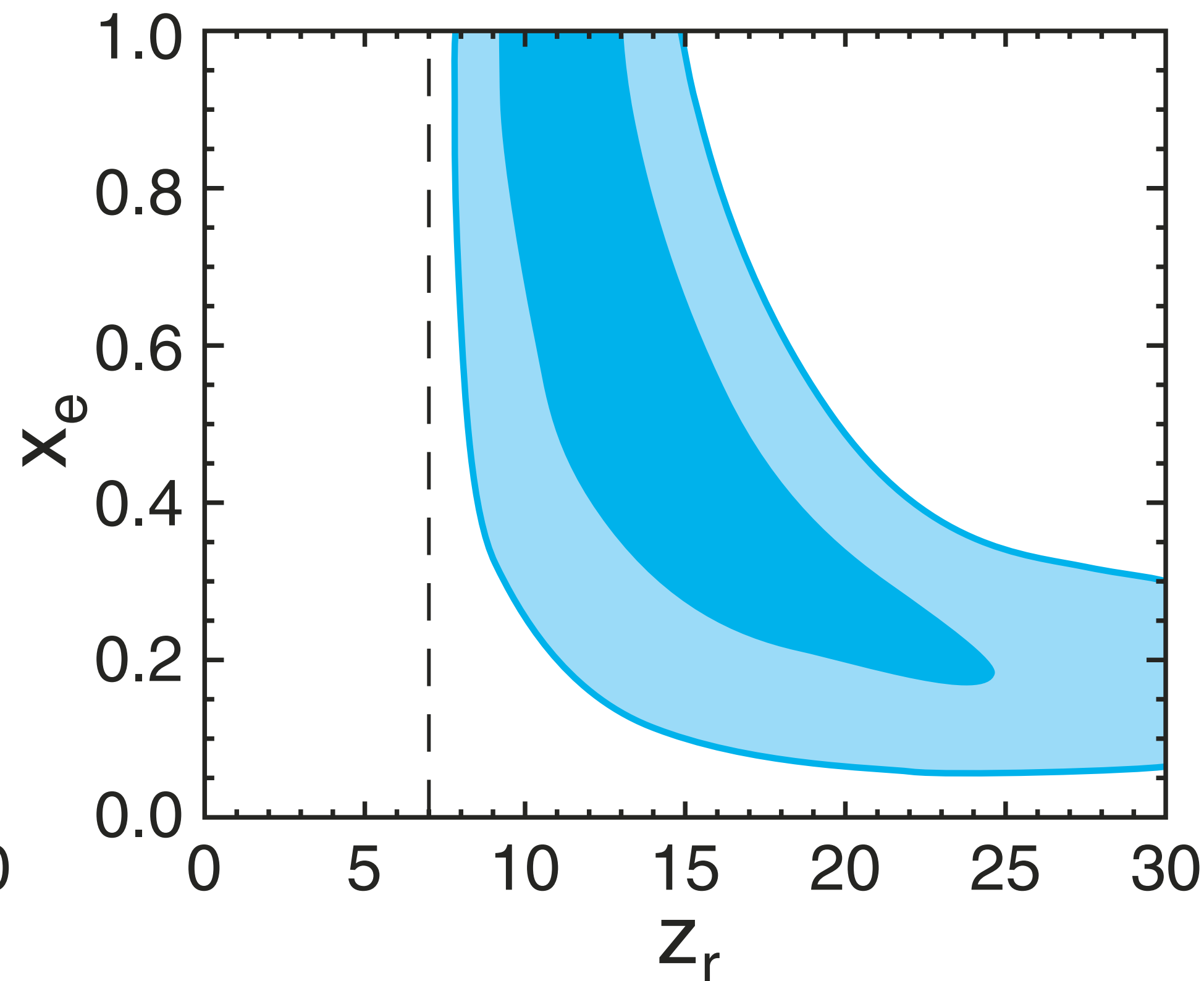
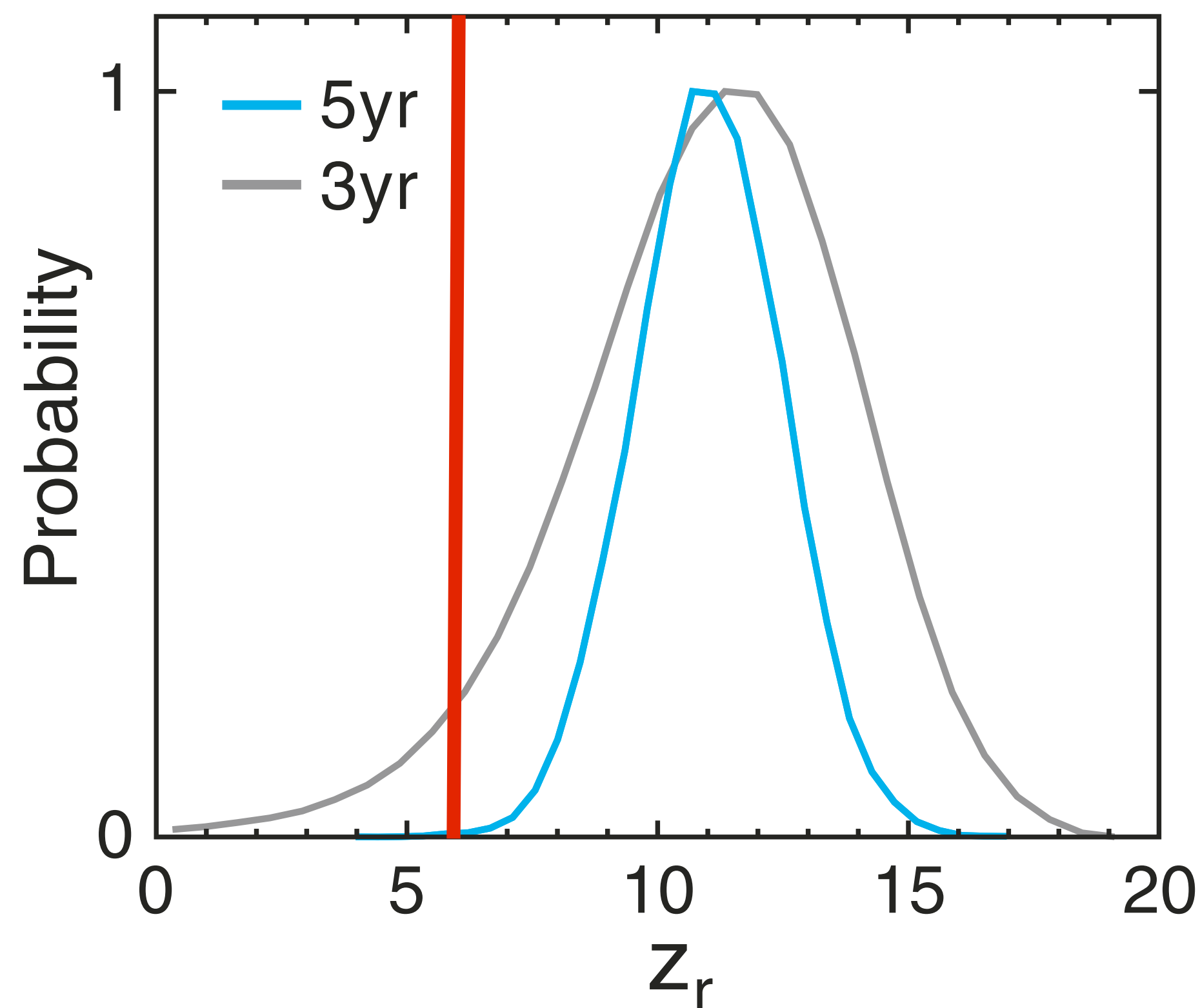
Adding Polarization in Ka: Passed the Null Test!!

- Optical Depth measured from the EE power spectrum:
- $\tau(5\text{yr}) = 0.087 \pm 0.017$
- $\tau(3\text{yr}) = 0.089 \pm 0.030$
(Page et al.; QV only)
- 3-sigma to 5-sigma!
- Tau from the null map (Ka-QV) is consistent with zero



$z_{\text{reion}}=6$ Excluded

Dunkley et al.

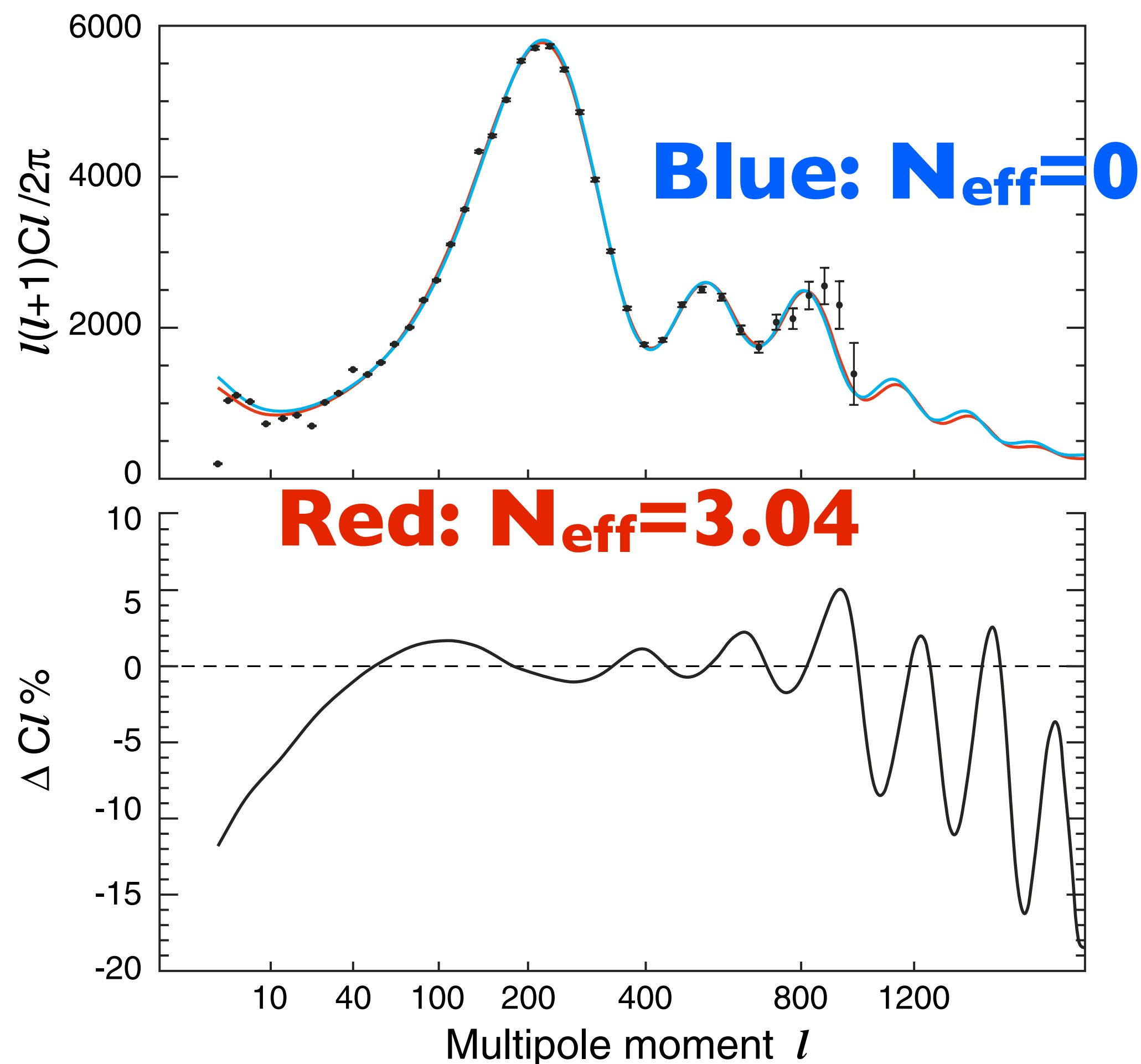


- Assuming instantaneous reionization from $x_e=0$ to $x_e=1$ at z_{reion} , we find **$z_{\text{reion}}=11.0 \pm 1.4$** (68 % CL).
- The reionization was not an instantaneous process at $z \sim 6$. (The 3-sigma lower bound is $z_{\text{reion}} > 6.7$.)

Cosmic Neutrino Background

- How do neutrinos affect CMB?
 - They change the radiation-to-matter ratio. The larger the number of neutrino species is, the later the matter-radiation equality, z_{equality} , becomes.
 - So, this effect is degenerate with the matter density.
 - Neutrino perturbations affect metric perturbations as well as the photon-baryon plasma, through which CMB anisotropy is affected.

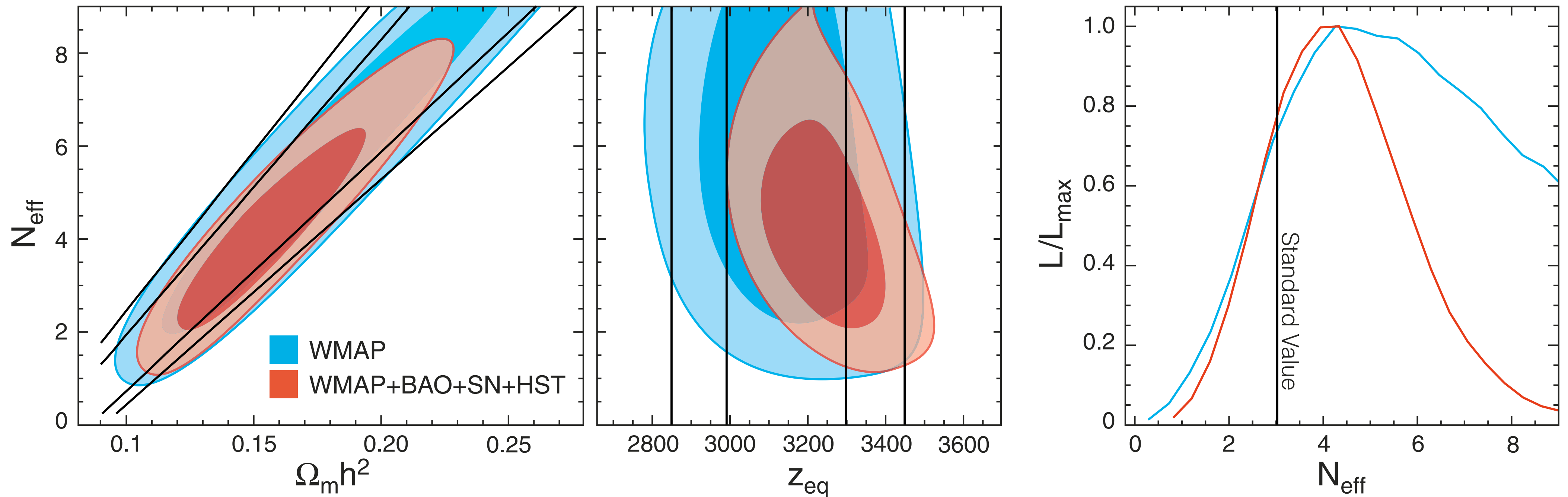
CNB as seen in WMAP



$\Delta\chi^2=8.2 \rightarrow 99.5\% \text{ CL}$

- Multiplicative phase shift is due to the change in z_{equality}
 - Degenerate with $\Omega_{\text{m}}h^2$
- Suppression is due to neutrino perturbations
 - Degenerate with n_s
- Additive phase shift is due to neutrino perturbations
 - No degeneracy (Bashinsky & Seljak 2004)

It's not z_{equality} !



- The number of neutrino species is massively degenerate with $\Omega_m h^2$, which simply traces $z_{\text{equality}} = \text{constant}$.
- But, the contours close near $N_{\text{eff}} \sim 1$, in contradiction to the prediction from $z_{\text{equality}} = \text{constant}$.

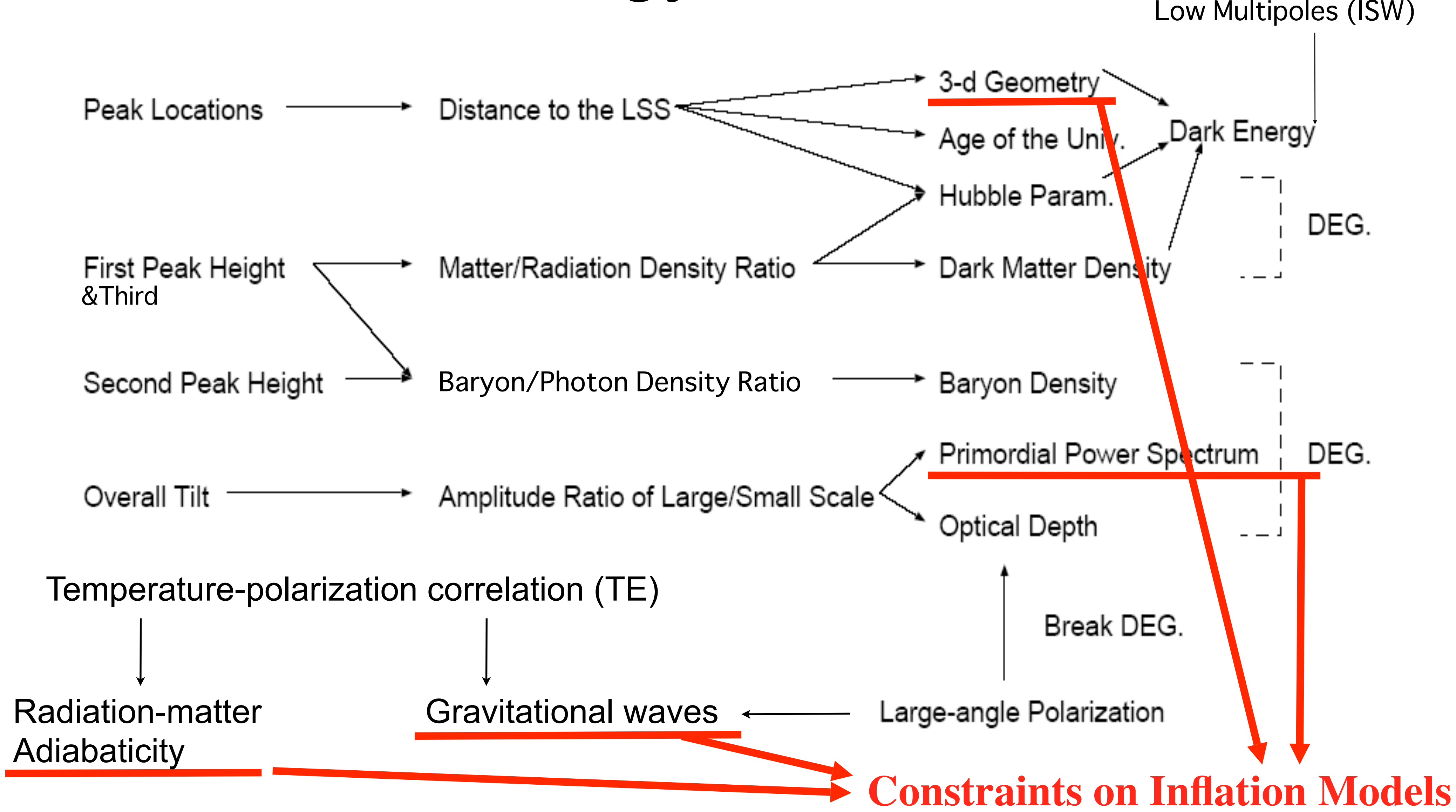
Cosmic/Laboratory Consistency

- From WMAP+BAO+SN (I will explain what BAO and SN are shortly)
 - $N_{\text{eff}}=4.4 \pm 1.5$
- From the Big Bang Nucleosynthesis
 - $N_{\text{eff}}=2.5 \pm 0.4$
- From the decay width of Z bosons measured in LEP
 - $N_{\text{neutrino}}=2.984 \pm 0.008$

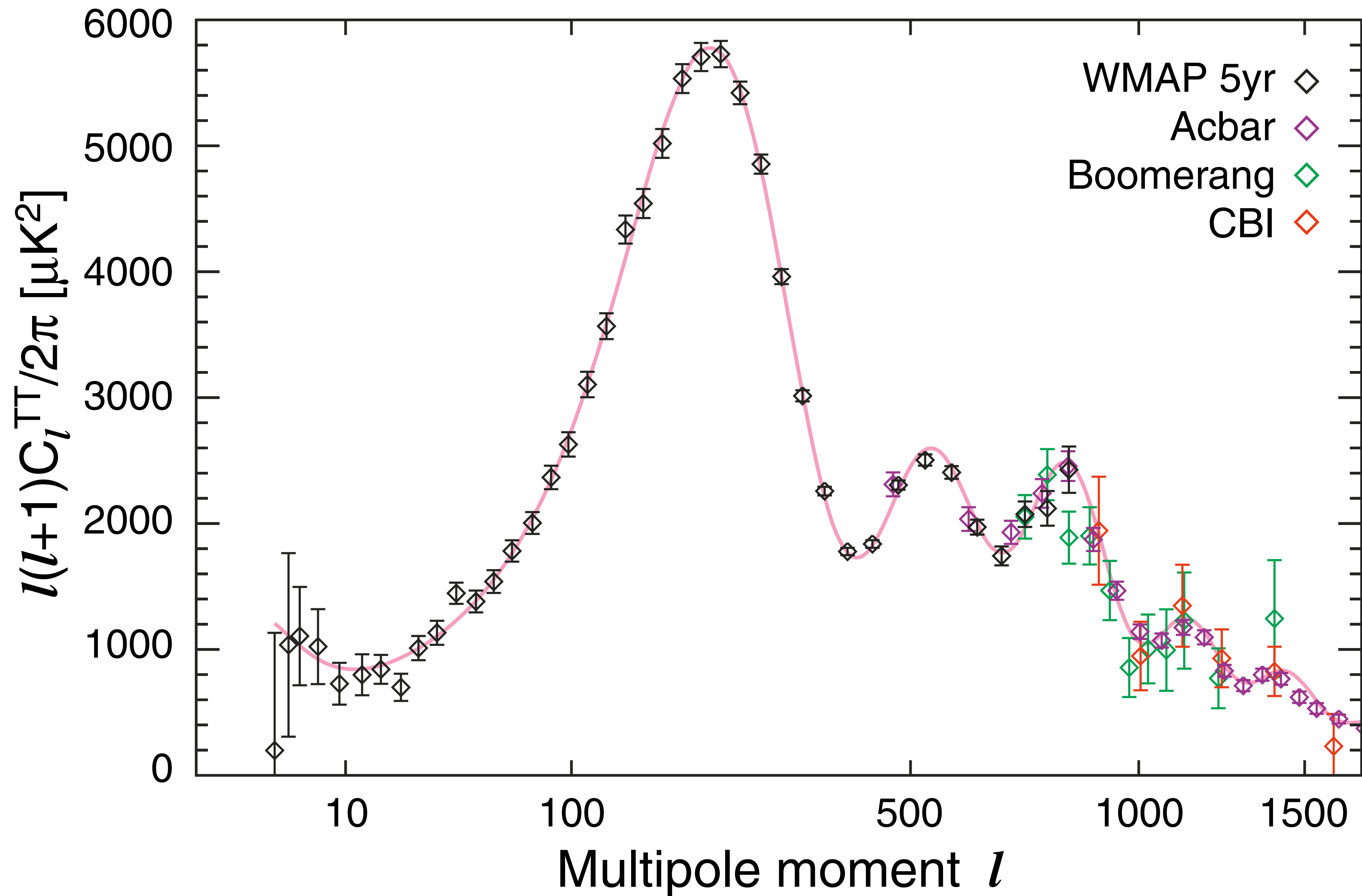
Testing Inflation

- Is the observable universe flat?
- Are the primordial fluctuations adiabatic?
- Are the primordial fluctuations nearly Gaussian?
- Is the power spectrum nearly scale invariant?
- Is the amplitude of gravitational waves reasonable?

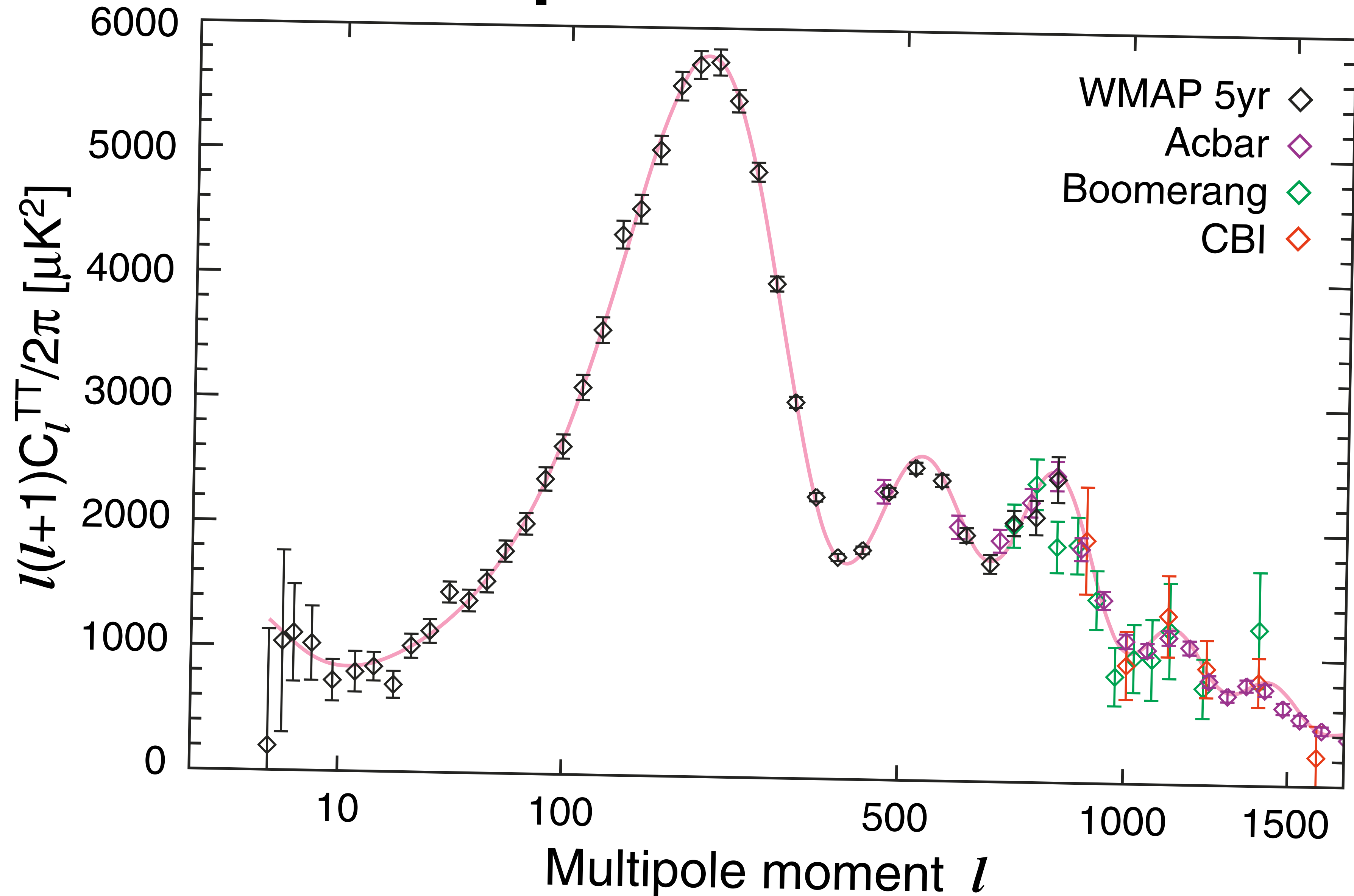
CMB to Cosmology to Inflation



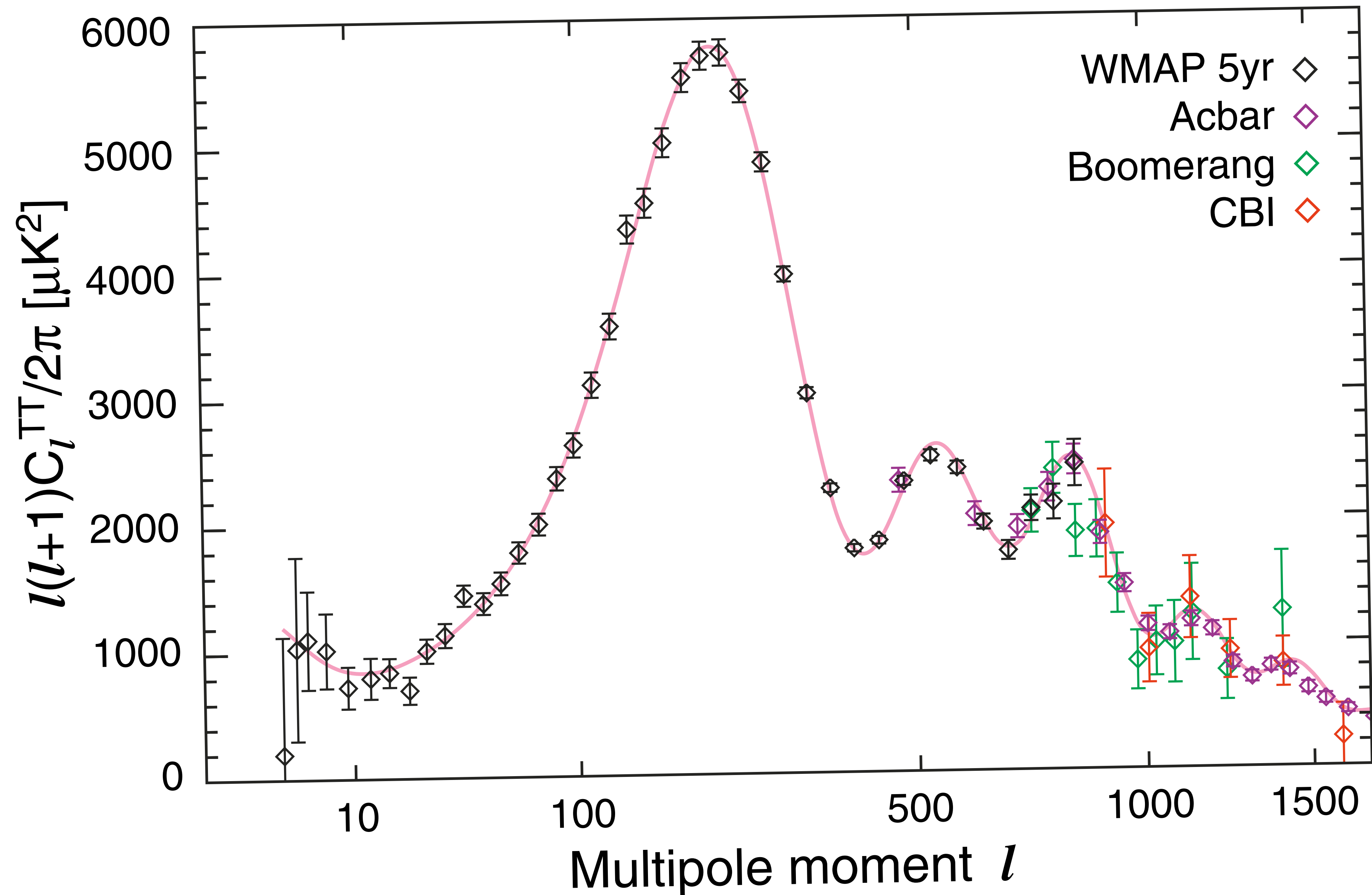
Tilting



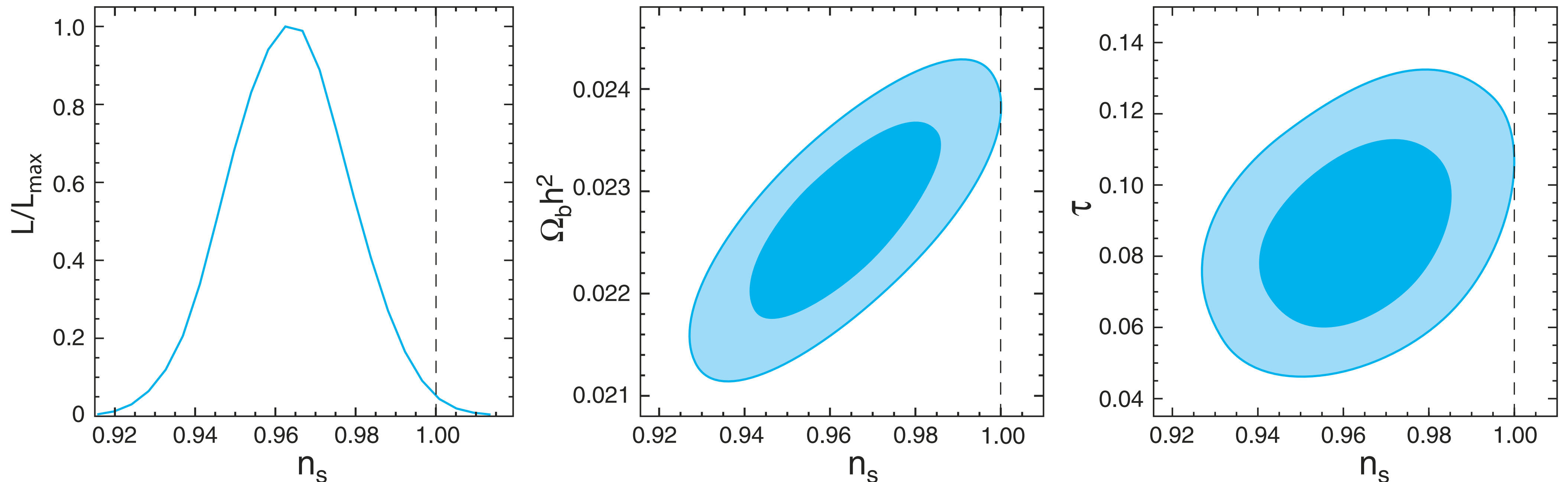
“Red” Spectrum: $n_s < 1$



“Blue” Spectrum: $n_s > 1$



Tau: (Once) Important for n_s *Komatsu et al.*



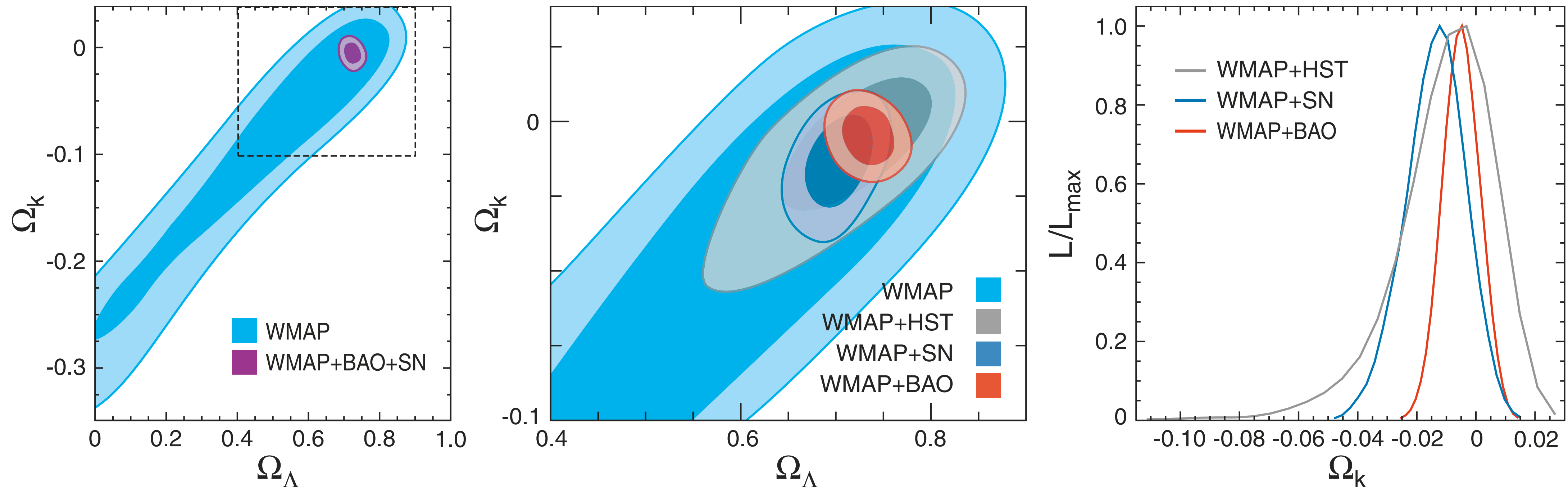
- With the 5-year determination of the optical depth (τ), the most dominant source of degeneracy is now $\Omega_b h^2$, rather than τ .
- WMAP-alone: $n_s = 0.963 (+0.014) (-0.015)$ (Dunkley et al.)
 - 2.5-sigma away from $n_s = 1$

How Do We Test Inflation?

- The WMAP data alone can put tight limits on most of the items in the check list. (For the WMAP-only limits, see Dunkley et al.)
- However, we can improve the limits on many of these items by adding the extra information from the distance measurements:
 - *Luminosity Distances* from Type Ia Supernovae (SN)
 - *Angular Diameter Distances* from the Baryon Acoustic Oscillations (BAO) in the distribution of galaxies

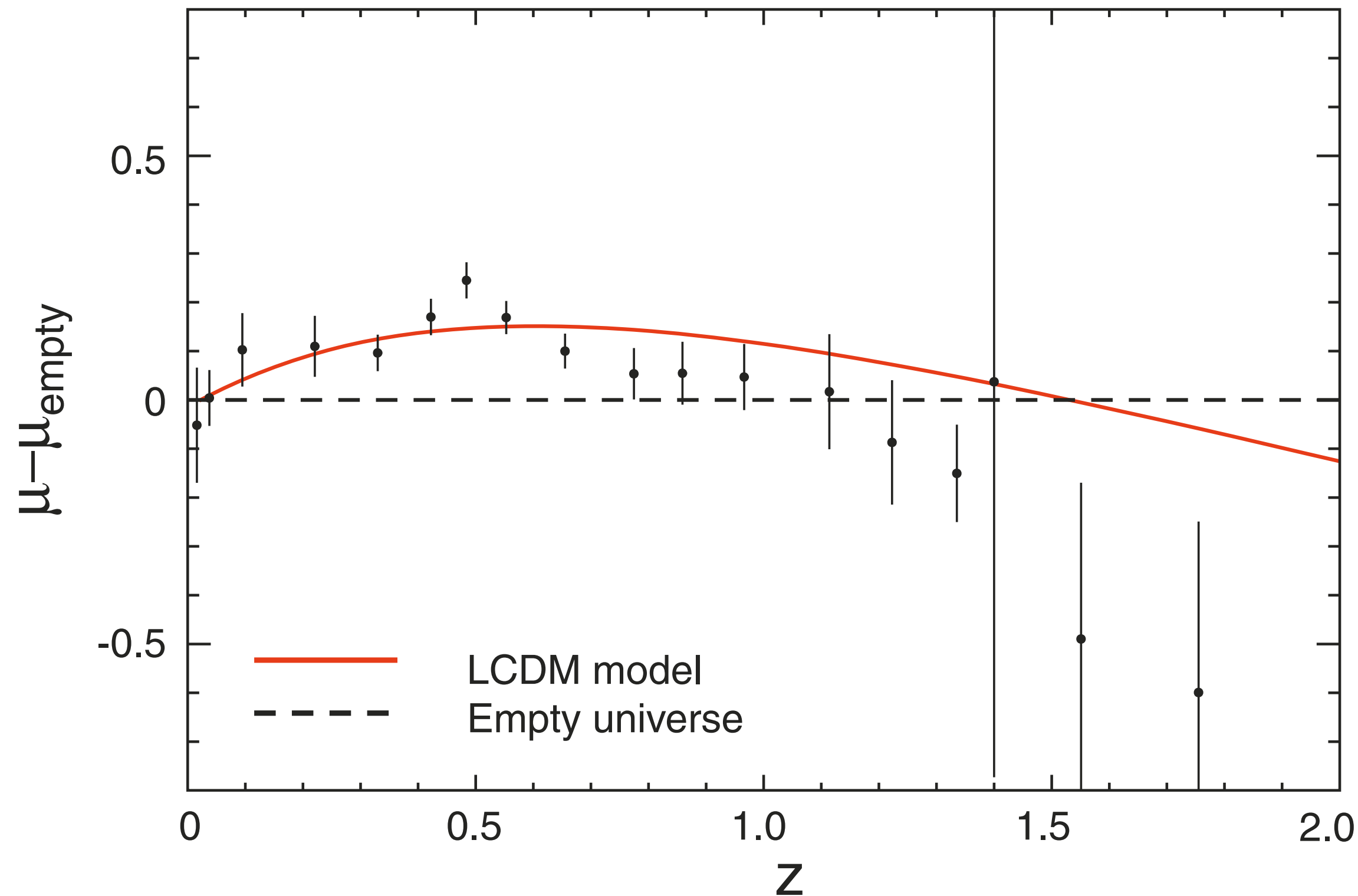
Example: Flatness

Komatsu et al.



- WMAP measures the angular diameter distance to the decoupling epoch at $z=1090$.
- The distance depends on curvature AND other things, like the energy content; thus, we need more than one distance indicators, in order to constrain, e.g., Ω_m and H_0

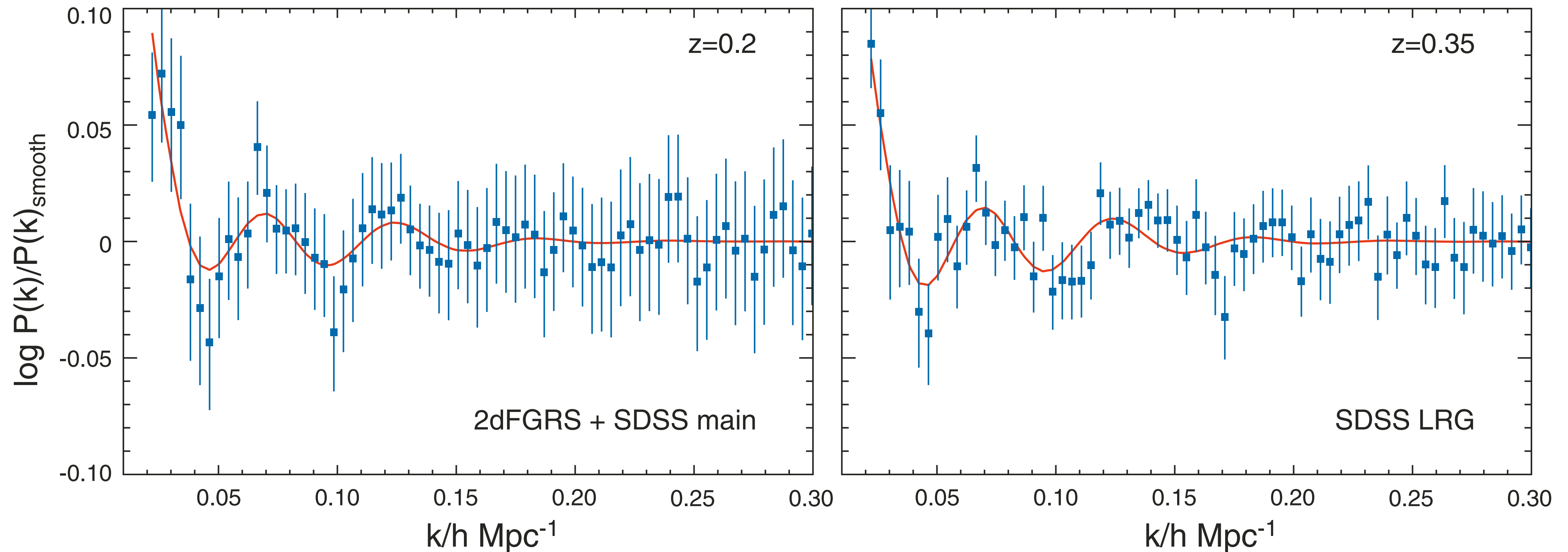
Type Ia Supernova (SN) Data



From these measurements, we get the **relative** luminosity distances between Type Ia SNe. Since we marginalize over the absolute magnitude, the current SN data are insensitive to the **absolute distances**.

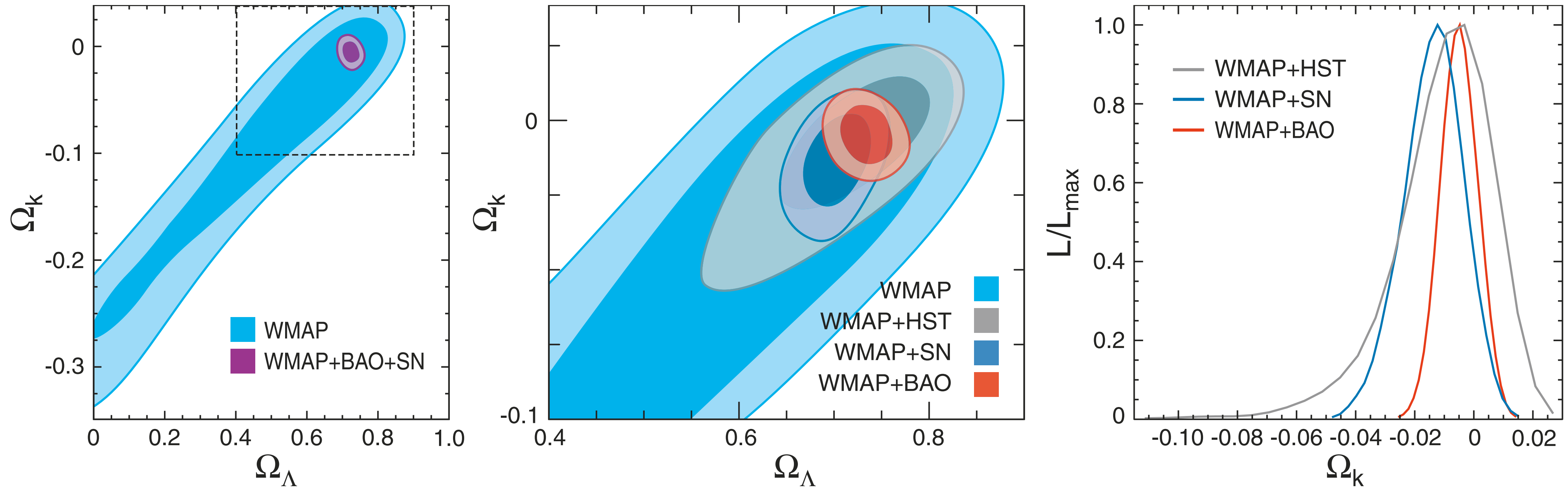
- Riess et al. (2004; 2006) HST data
- Astier et al. (2006) Supernova Legacy Survey (SNLS)
- Wood-Vasey et al. (2007) ESSENCE data

BAO in Galaxy Distribution *Dunkley et al.*



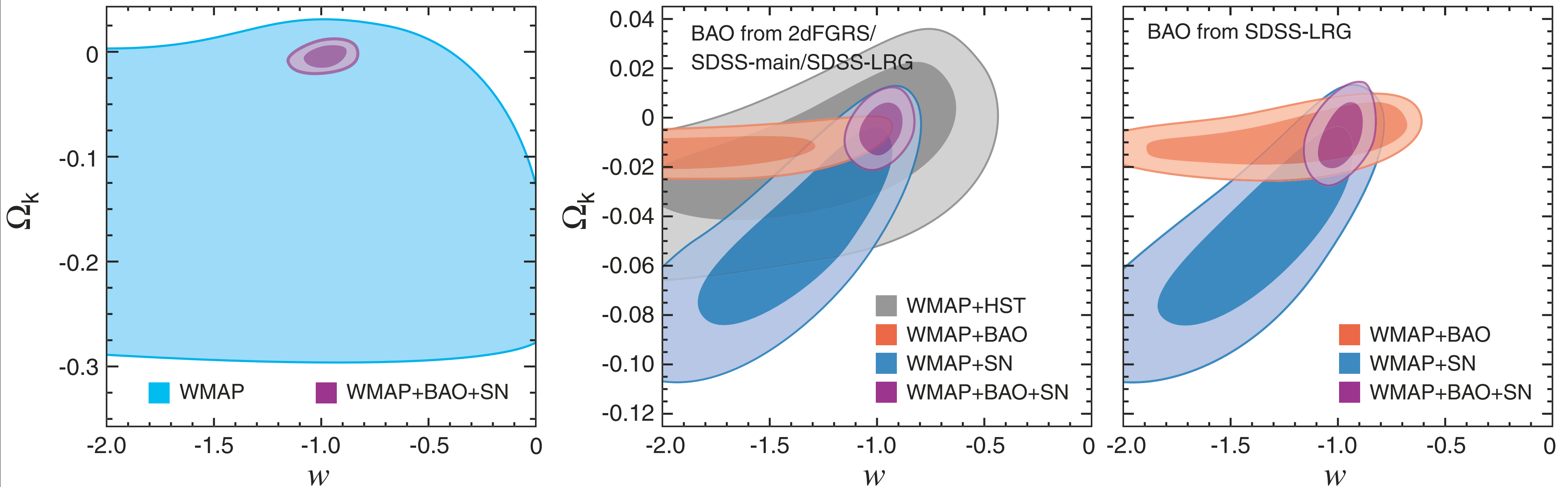
- BAO measured from SDSS (main samples and LRGs) and 2dFGRS (Percival et al. 2007)
- Just like the acoustic oscillations in CMB, the galaxy BAOs can be used to measure the **absolute** distances

As a result..



- **$-0.0181 < \Omega_k < 0.0071$** (95% CL) for $w=-1$
- The constraint driven mostly by WMAP+BAO
- BAOs are more powerful than SNe in pinning down curvature, as they are **absolute** distance indicators.

What if $w \neq -1$...



- WMAP+BAO \rightarrow Curvature
- WMAP+SN \rightarrow w
- WMAP+BAO+SN \rightarrow Simultaneous limit
- $-0.0175 < \Omega_k < 0.0085$; $-0.11 < w < 0.14$ (95% CL)

Fun Numbers to Quote...

- The curvature radius of the universe is given, by definition, by
 - $R_{\text{curv}} = 3h^{-1}\text{Gpc} / \text{sqrt}(\Omega_k)$
 - For negatively curved space ($\Omega_k > 0$): $R > 33h^{-1}\text{Gpc}$
 - For positively curved space ($\Omega_k < 0$): $R > 23h^{-1}\text{Gpc}$
- The particle horizon today is $9.7h^{-1}\text{Gpc}$
 - The observable universe is pretty flat! (Fun to teach this in class)

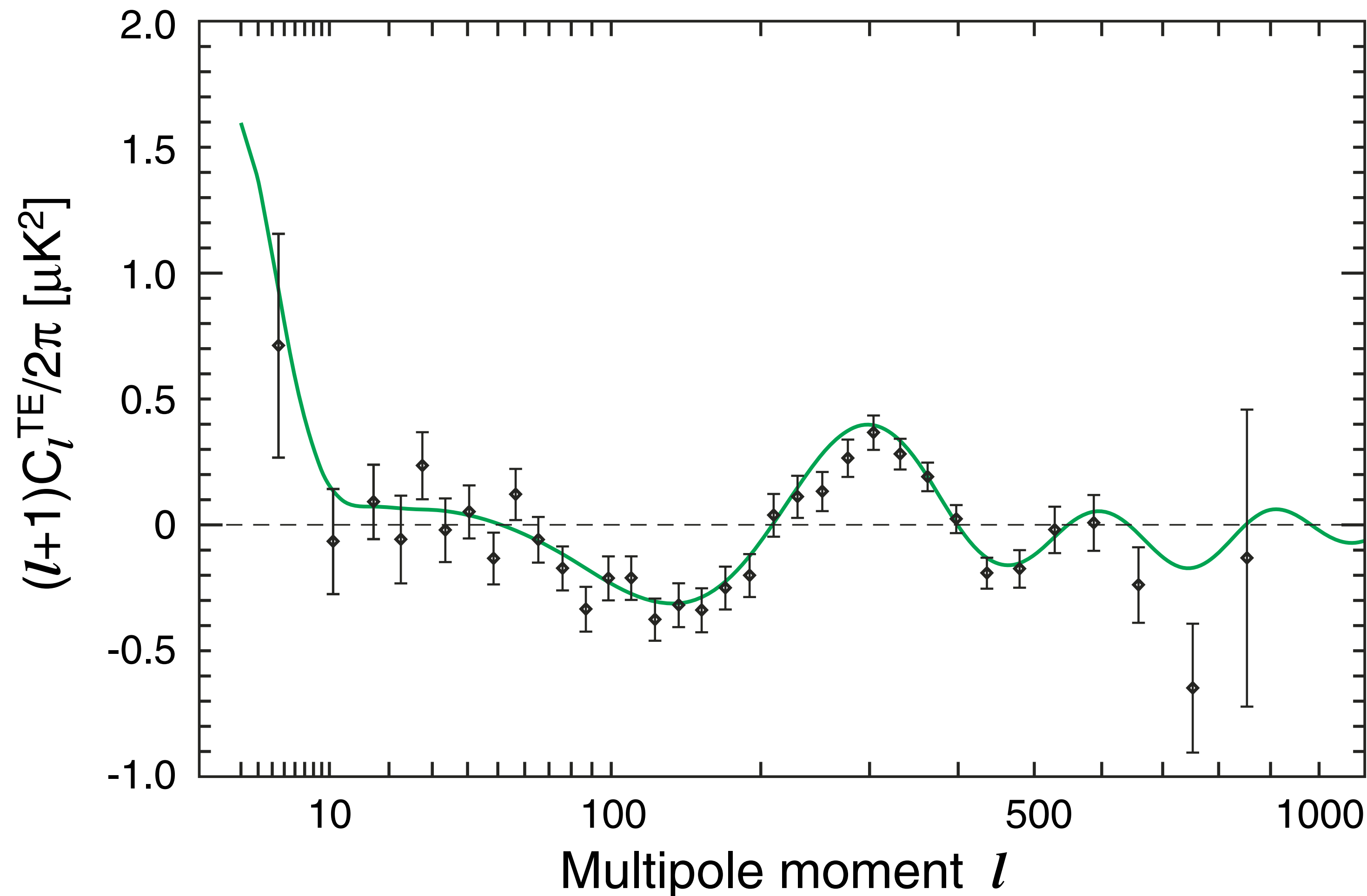
Implications for Inflation?

- Details aside...
 - Q. How long should inflation have lasted to explain the observed flatness of the universe?
 - A. **$N_{\text{total}} > 36 + \ln(T_{\text{reheating}}/1 \text{ TeV})$**
 - A factor of 10 improvement in Ω_k will raise this lower limit by 1.2.
 - Lower if the reheating temperature was $< 1 \text{ TeV}$
- This is the check list #1

Check List #2: Adiabaticity

- The adiabatic relation between radiation and matter:
 - $3\delta\rho_{\text{radiation}}/(4\rho_{\text{radiation}}) = \delta\rho_{\text{matter}}/\rho_{\text{matter}}$
- *Deviation from adiabaticity*: A simple-minded quantification
 - Fractional deviation of A from B = $(A - B) / [(A + B)/2]$
 - $\delta_{\text{adi}} = [3\delta\rho_{\text{radiation}}/(4\rho_{\text{radiation}}) - \delta\rho_{\text{matter}}/\rho_{\text{matter}}] / \{ [3\delta\rho_{\text{radiation}}/(4\rho_{\text{radiation}}) + \delta\rho_{\text{matter}}/\rho_{\text{matter}}] / 2 \}$
 - Call this the “**adiabaticity deviation parameter**”
 - “Radiation and matter obey the adiabatic relation to $(100\delta_{\text{adi}})\%$ level.”

WMAP 5-Year TE Power Spectrum



- The negative TE at $l \sim 100$ is the distinctive signature of super-horizon adiabatic perturbations (Spergel & Zaldarriaga 1997)
- Non-adiabatic perturbations would fill in the trough, and shift the zeros.

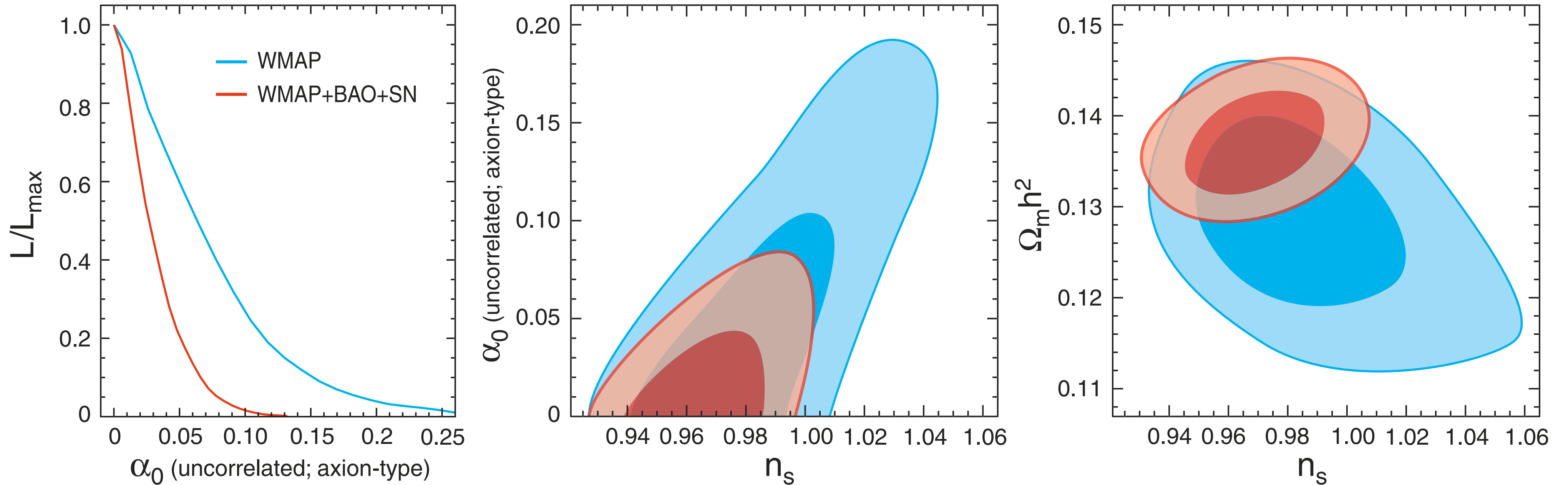
Entropy and curvature perturbations

- Usually, we use the entropy perturbations and curvature perturbations when we talk about adiabaticity.
 - (Entropy Pert.) = $3\delta\rho_{\text{radiation}}/(4\rho_{\text{radiation}}) - \delta\rho_{\text{matter}}/\rho_{\text{matter}}$
 - (Curvature Pert.) = $\delta\rho_{\text{matter}}/(3\rho_{\text{matter}}) = \delta\rho_{\text{radiation}}/(4\rho_{\text{radiation}})$
- Let's take the ratio, square it, and call it α :
 - $\alpha = (\text{Entropy})^2/(\text{Curvature})^2 = 9\delta_{\text{adi}}^2$
 - This parameter, α , has often been used in the literature.

Two Scenarios

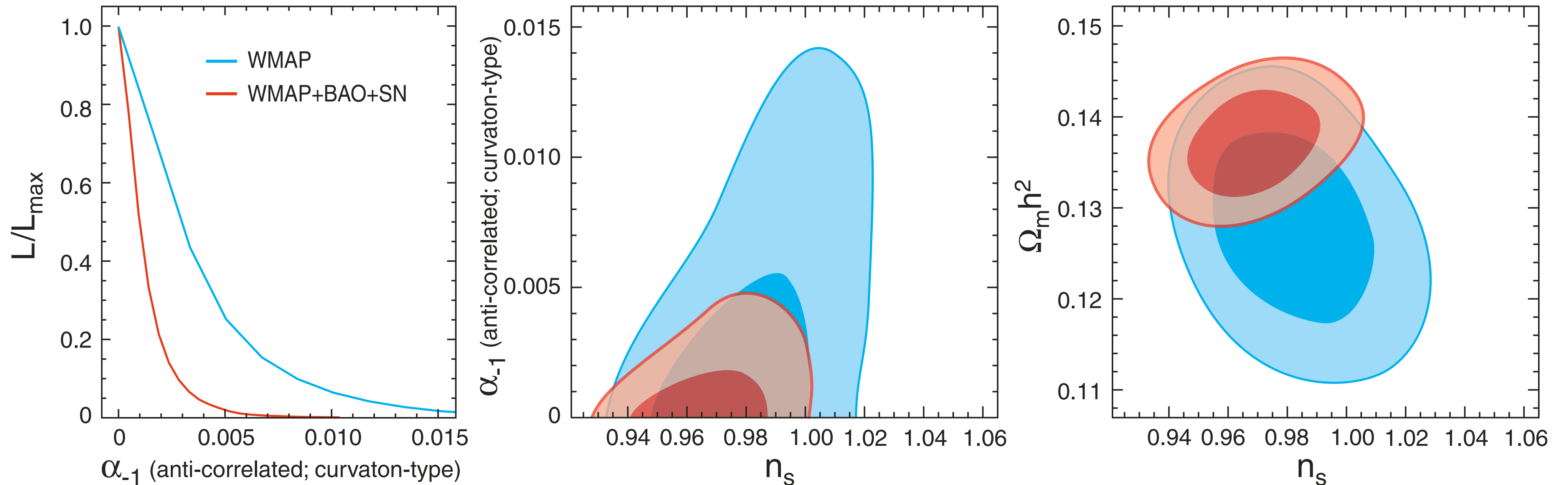
- To make the argument concrete, we take two concrete examples for entropy perturbations.
- (i) “***Axion Type***” Entropy perturbations and curvature perturbations are **uncorrelated**.
- (ii) “***Curvaton Type***” Entropy perturbations and curvature perturbations are **anti-correlated**. (or correlated, depending on the sign convention)
- In both scenarios, the entropy perturbation raises the temperature power spectrum at $l < 100$
 - Therefore, *both contributions are degenerate with n_s .*
How do we break the degeneracy? BAO&SN.

Axion Type



- $\alpha_{\text{axion}} < 0.16$ [WMAP-only; 95% CL]
- $\alpha_{\text{axion}} < 0.067$ [WMAP+BAO+SN; 95% CL]
- CMB and axion-type dark matter are adiabatic to **8.6%**

Curvaton Type



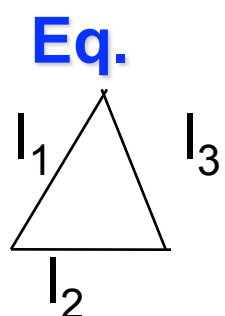
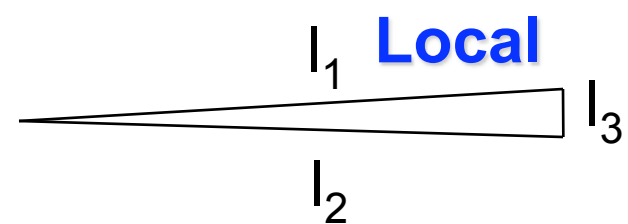
- $\alpha_{\text{curvaton}} < 0.011$ [WMAP-only; 95% CL]
- $\alpha_{\text{curvaton}} < 0.0037$ [WMAP+BAO+SN; 95% CL]
- CMB and axion-type dark matter are adiabatic to **2.0%**

Check list #3: Gaussianity

- In the simplest model of inflation, the distribution of primordial fluctuations is close to a Gaussian with random phases.
- The level of non-Gaussianity predicted by the simplest model is well below the current detection limit.
- A convincing detection of primordial non-Gaussianity will rule out most of inflation models in the literature.

Angular Bispectrum

- Non-zero bispectrum means the detection of non-Gaussianity. It's always easy to look for deviations from zero!
- There are many triangles to look for, but...
 - Will focus on two classes
 - “Squeezed” parameterized by $f_{\text{NL}}^{\text{local}}$
 - “Equilateral” parameterized by $f_{\text{NL}}^{\text{equil}}$



No Detection at $\geq 95\%$ CL

- $-9 < f_{\text{NL}}(\text{local}) < 111$ (95% CL)
- $-151 < f_{\text{NL}}(\text{equilateral}) < 253$ (95% CL)
- These numbers mean that the primordial curvature perturbations are Gaussian to **0.1% level!**

Check List #4: Scale Invariance

- For a power-law power spectrum (no $dn_s/d\ln k$):
 - WMAP-only: $n_s=0.963$ (+0.014) (-0.015)
 - WMAP+BAO+SN: $n_s=0.960$ (+0.014) (-0.013)
 - **2.9 sigma away from $n_s=1$**
 - No dramatic improvement from the WMAP-only result because neither BAO nor SN is sensitive to $\Omega_b h^2$

Running Index?

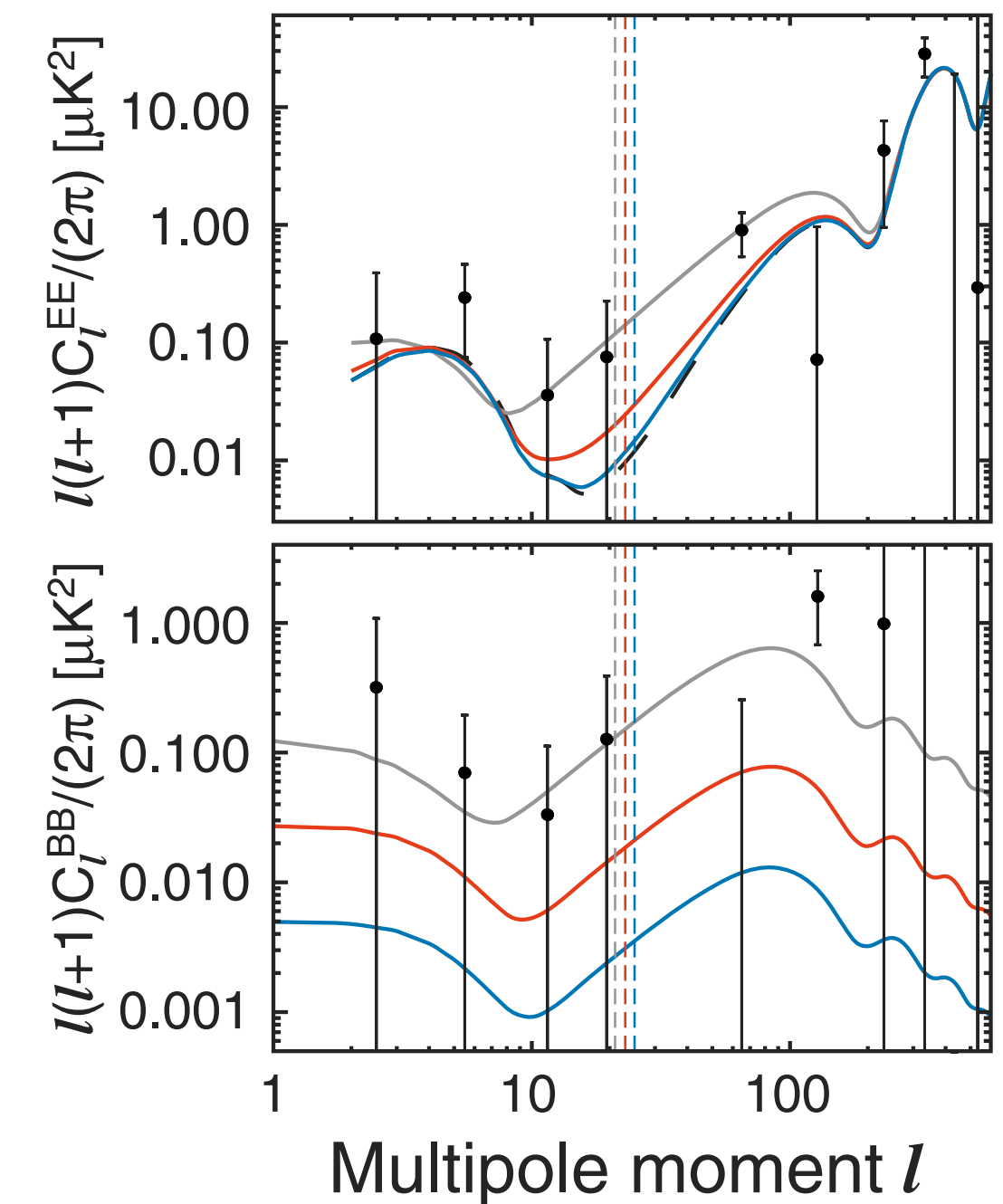
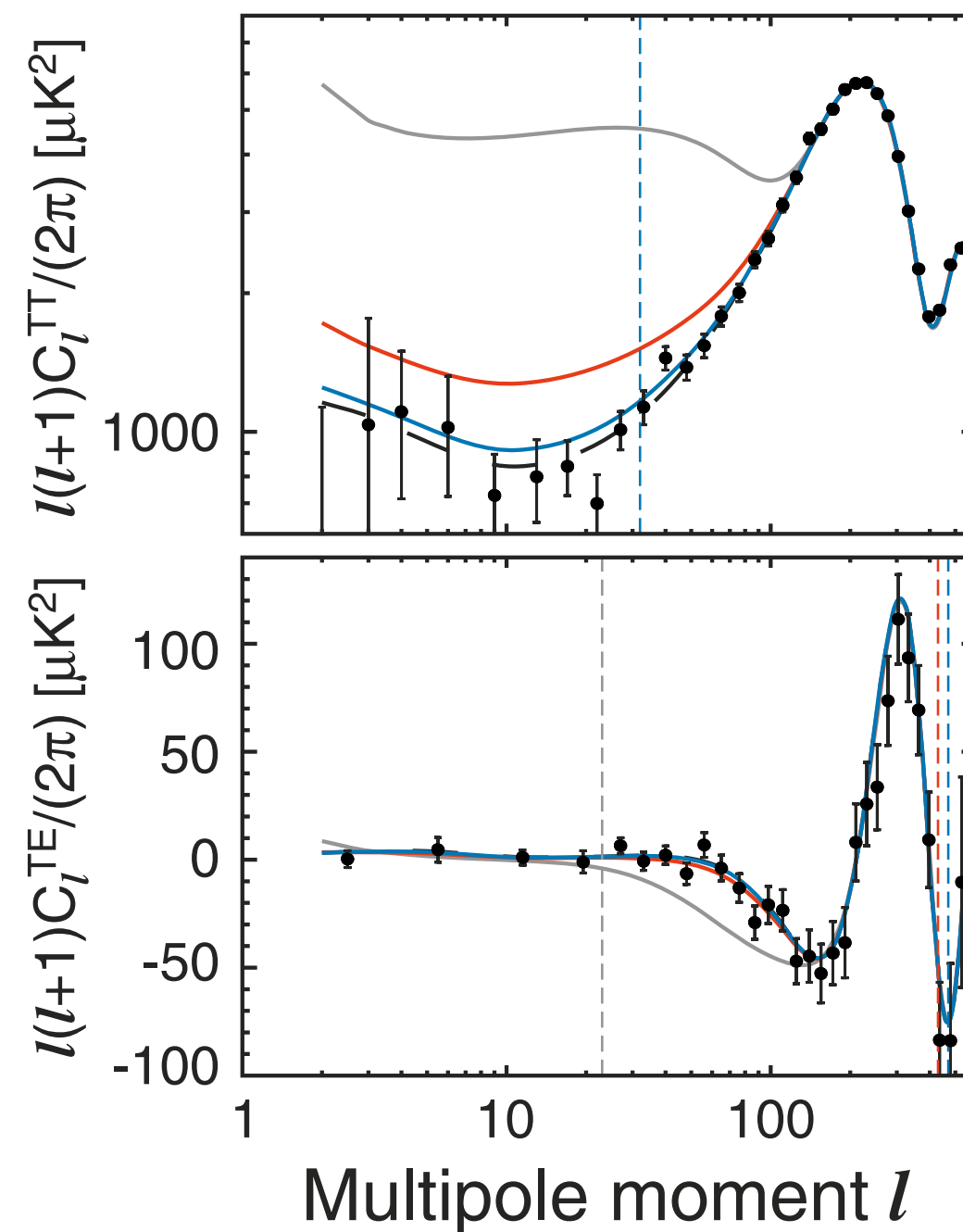
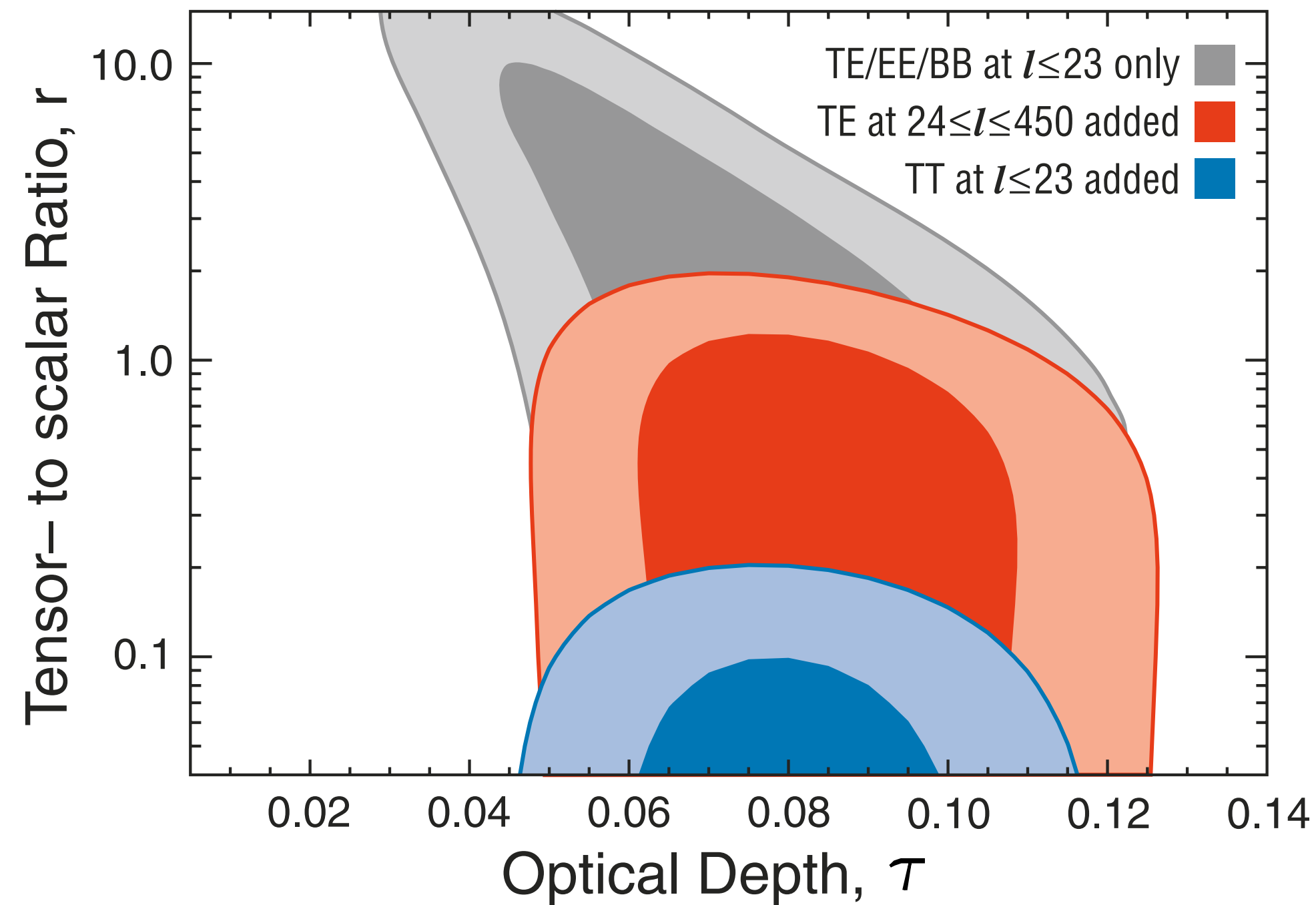
- No significant running index is observed.
 - WMAP-only: $dn_s/d\ln k = -0.037 \pm 0.028$
 - WMAP+BAO+SN: $dn_s/d\ln k = -0.032 (+0.021) (-0.020)$
- **A power-law spectrum is a good fit.**
- Note that $dn_s/d\ln k \sim O(0.001)$ is expected from simple inflation models (like $m^2\varphi^2$), but we are not there yet.

Check List #5: Gravitational Waves

- How do WMAP data constrain the amplitude of primordial gravitational waves?

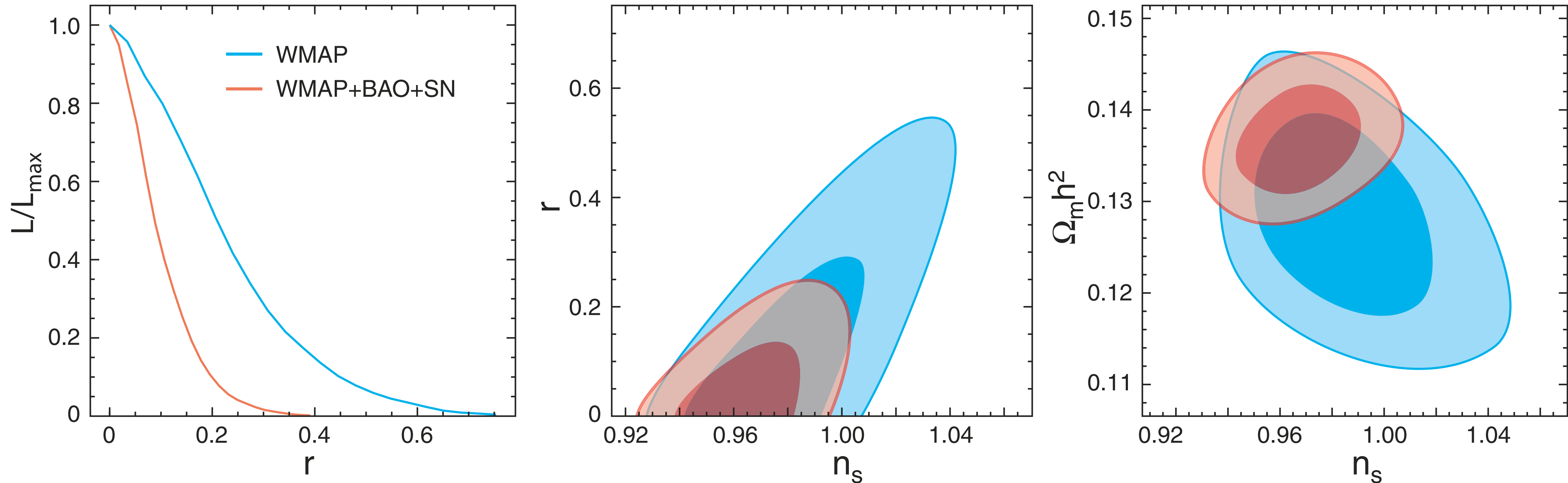
Pedagogical Explanation

Komatsu et al.



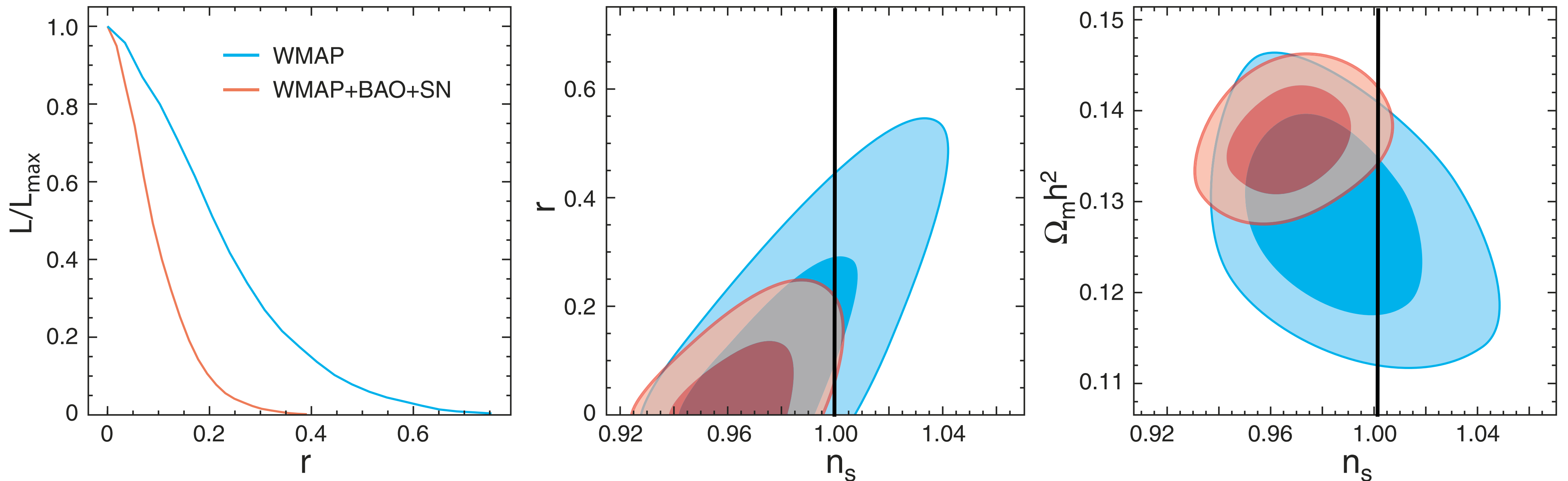
- If all the other parameters (n_s in particular) are fixed...
 - Low- l polarization gives $r < 20$ (95% CL)
 - + high- l polarization gives $r < 2$ (95% CL)
 - + low- l temperature gives $r < 0.2$ (95% CL)

Real Life: Killer Degeneracy



- Since the limit on r relies on the low- l temperature, it is strongly degenerate with n_s .
- The degeneracy can be broken partially by BAO&SN
- $r < 0.43$ (WMAP-only) \rightarrow **$r < 0.20$** (WMAP+BAO+SN)

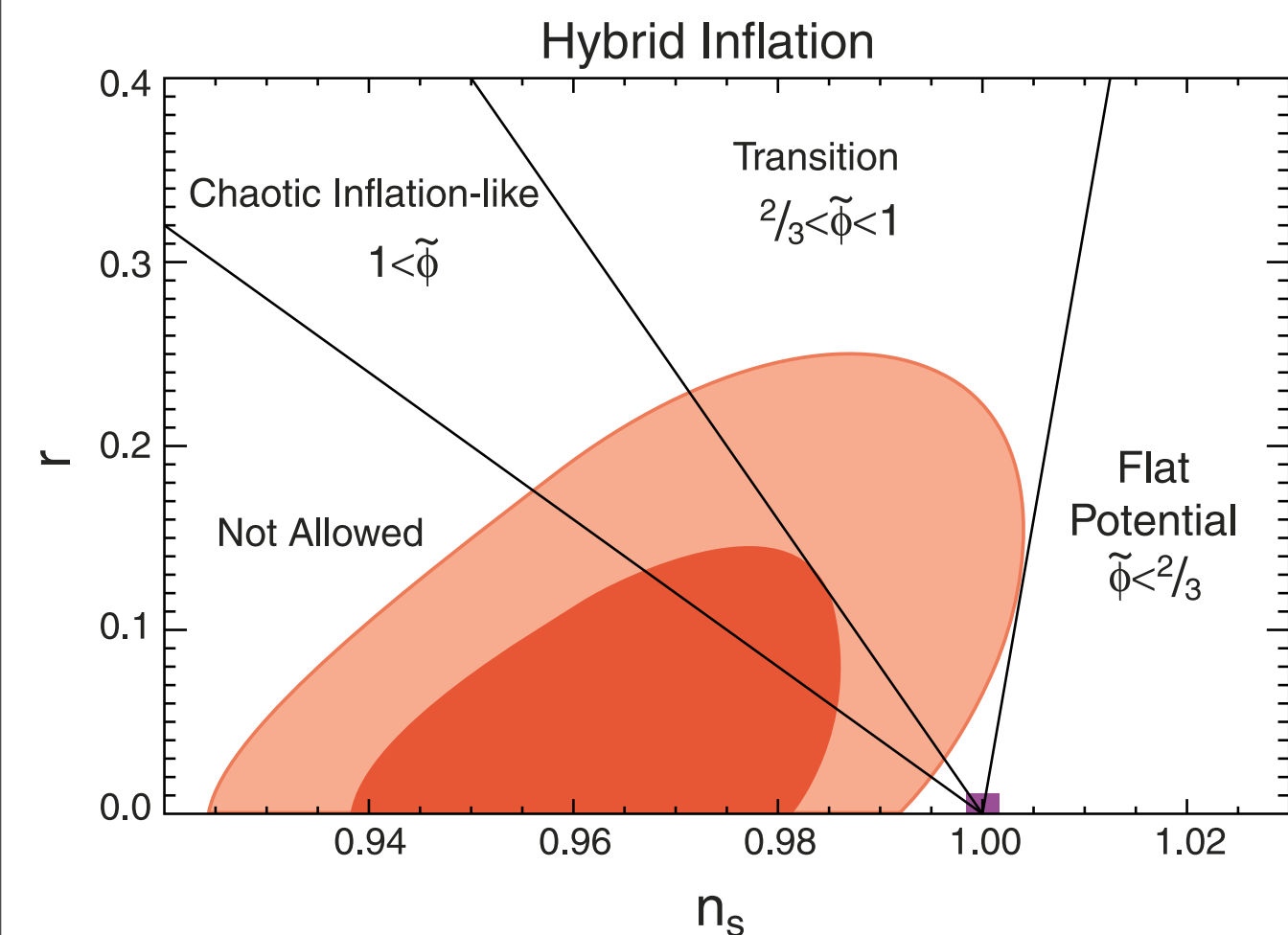
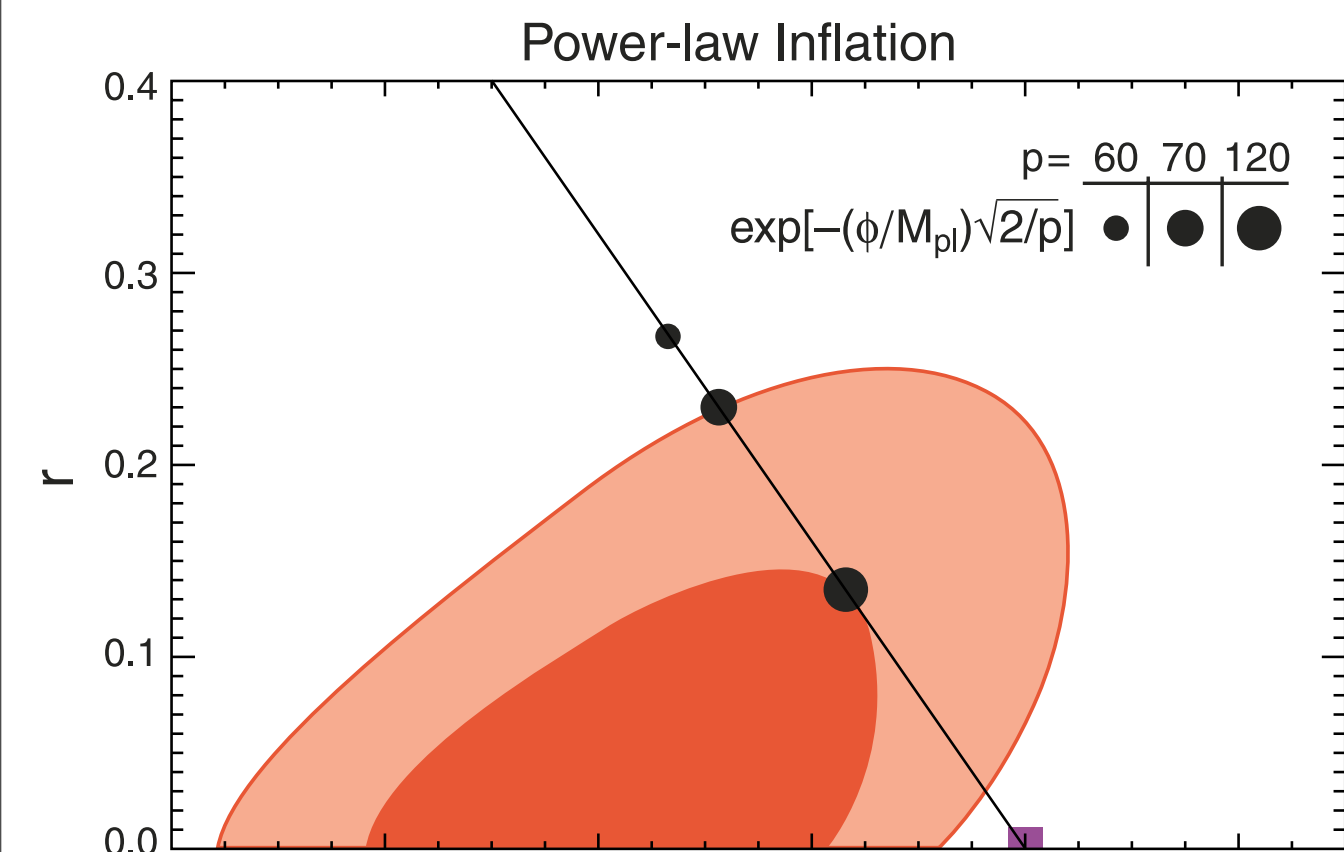
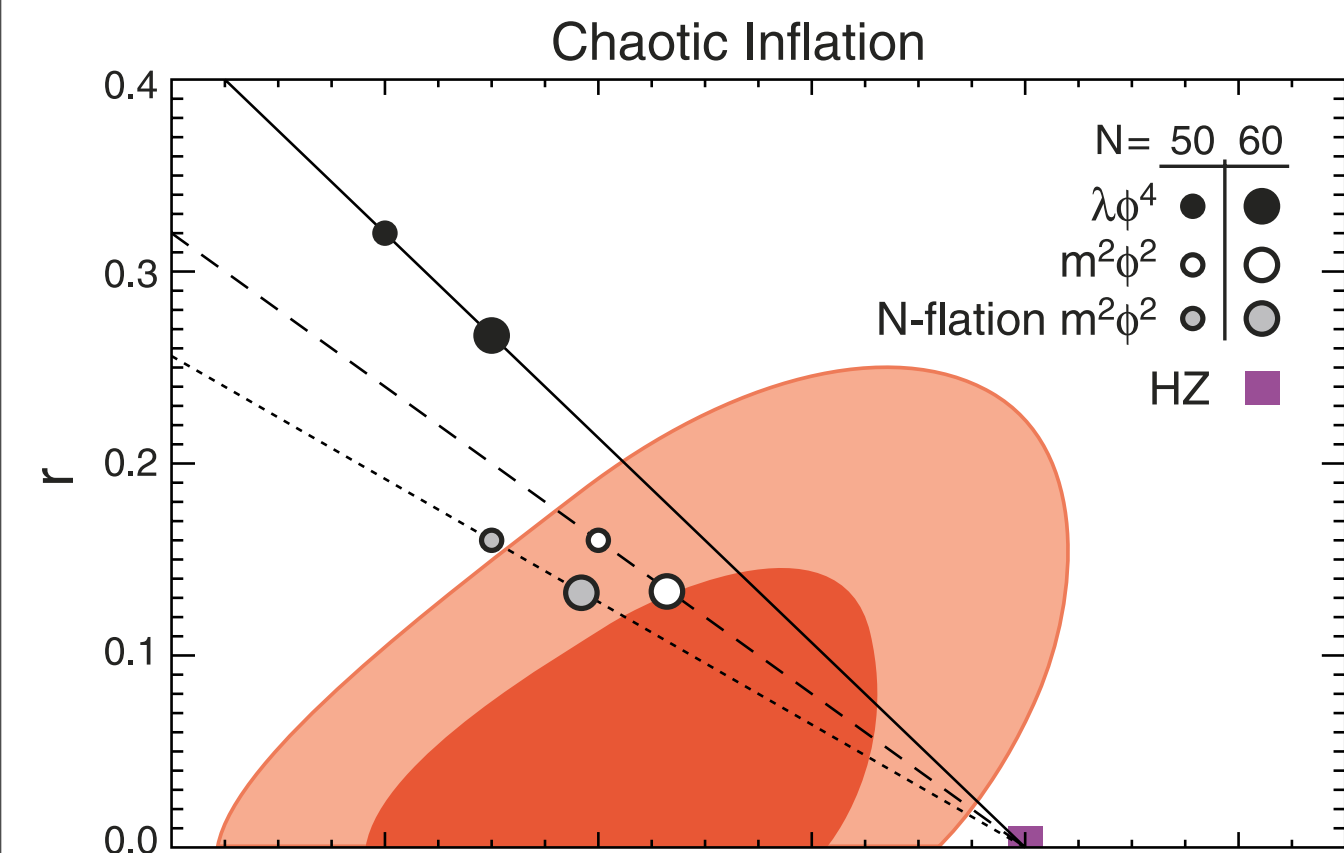
$n_s > 1.0$ is Disfavored, Regardless of r



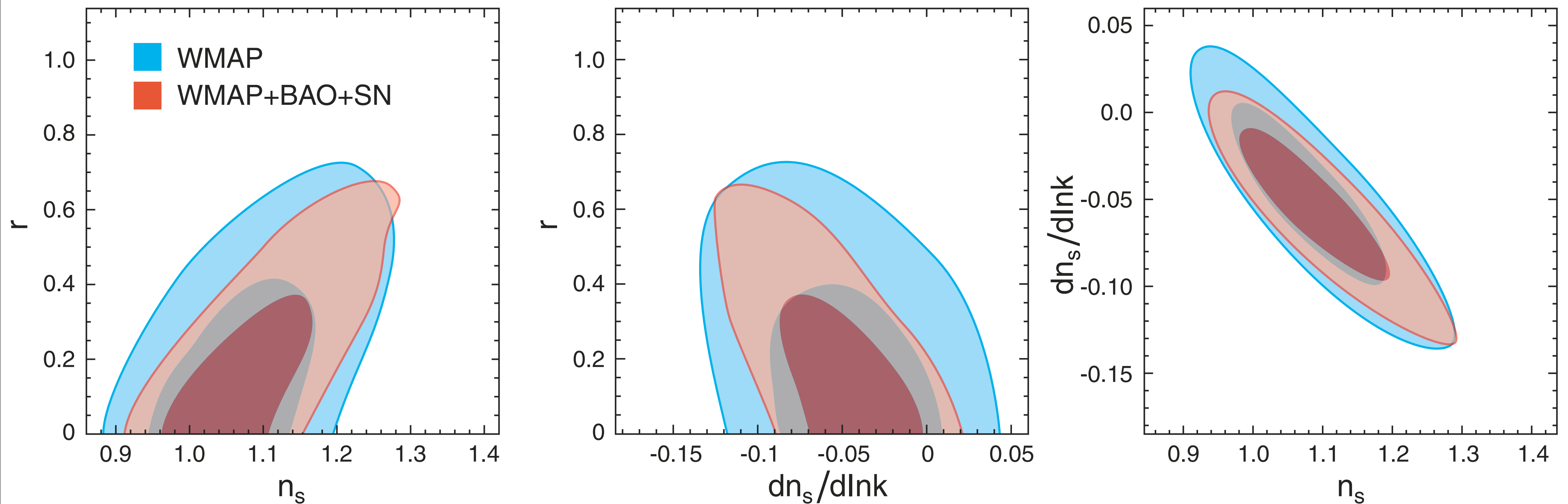
- The maximum n_s we find at 95% CL is **$n_s = 1.005$ for $r = 0.16$.**

Lowering a “Limbo Bar”

- $\lambda\varphi^4$ is totally out. (unless you invoke, e.g., non-minimal coupling, to suppress r ..)
- $m^2\varphi^2$ is within 95% CL.
 - Future WMAP data would be able to push it to outside of 95% CL, if $m^2\varphi^2$ is not the right model.
- N-flaton $m^2\varphi^2$ (Easter&McAllister) is being pushed out
- PL inflation [$a(t)\sim t^p$] with $p<60$ is out.
- A blue index ($n_s>1$) region of hybrid inflation is disfavored



How About Putting Everything (n_s , r , $dn_s/d\ln k$) In?



- Then of course, constraints are weakened.. BAO&SN do not help much anymore.

Grading Inflation

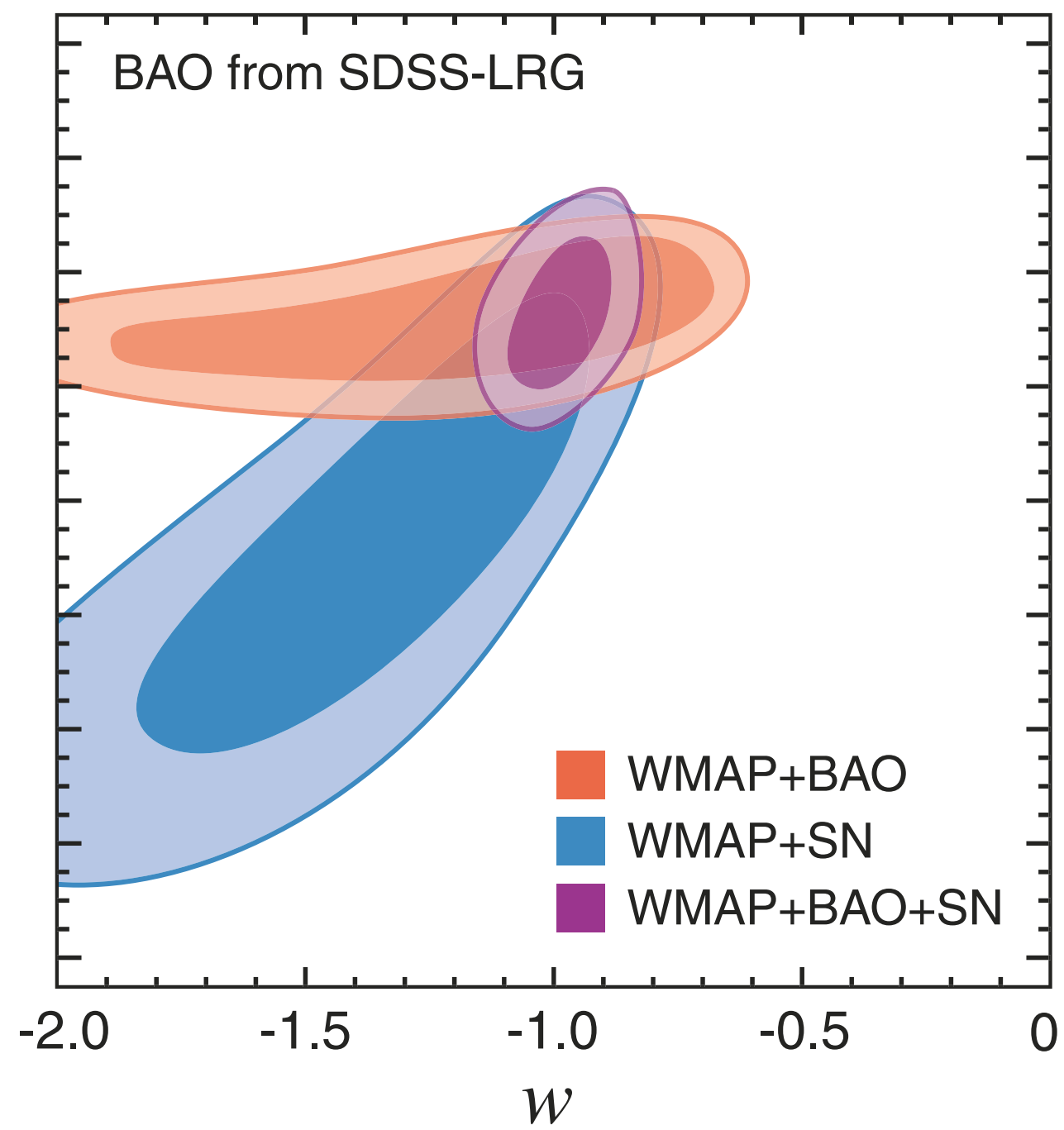
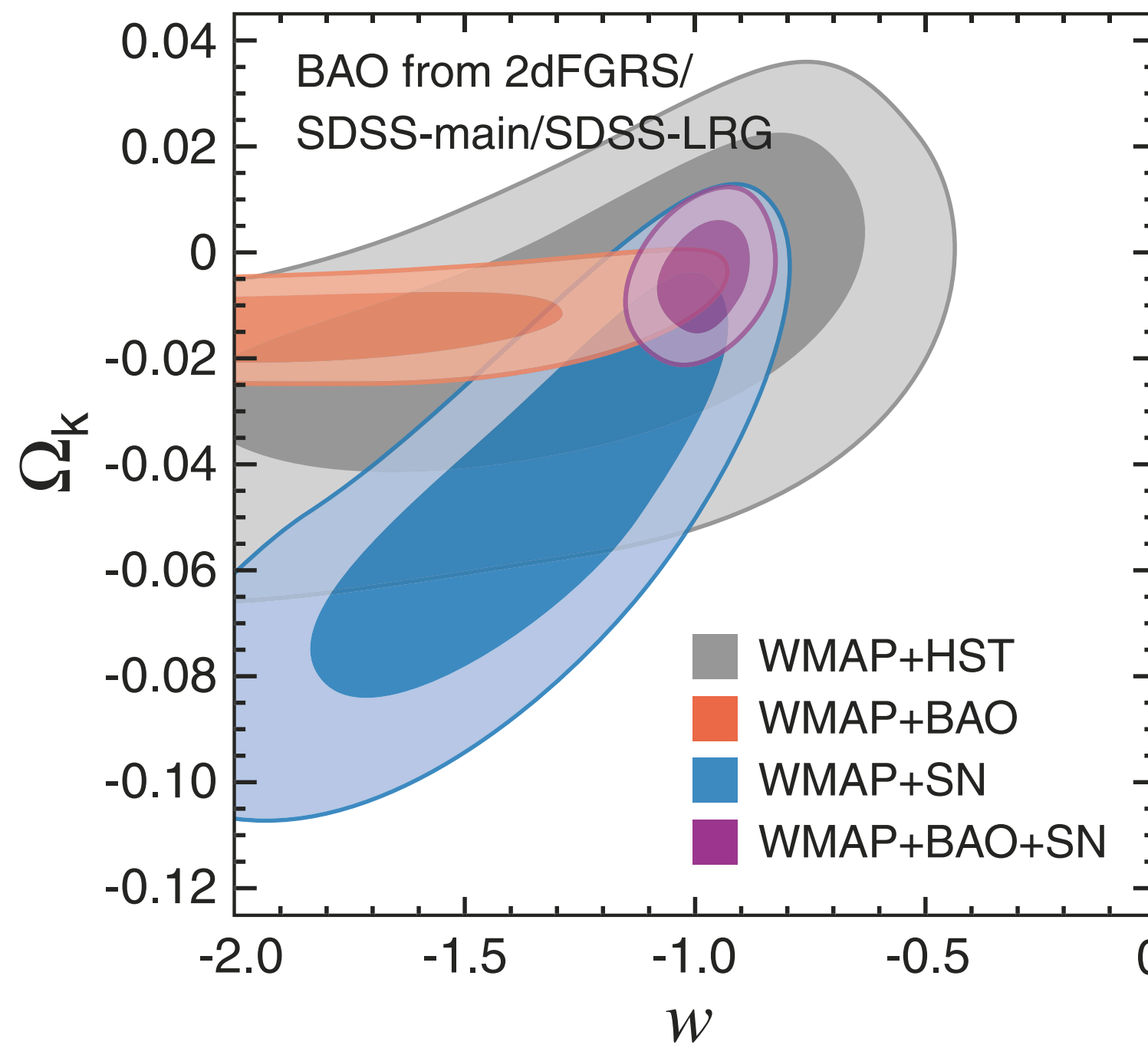
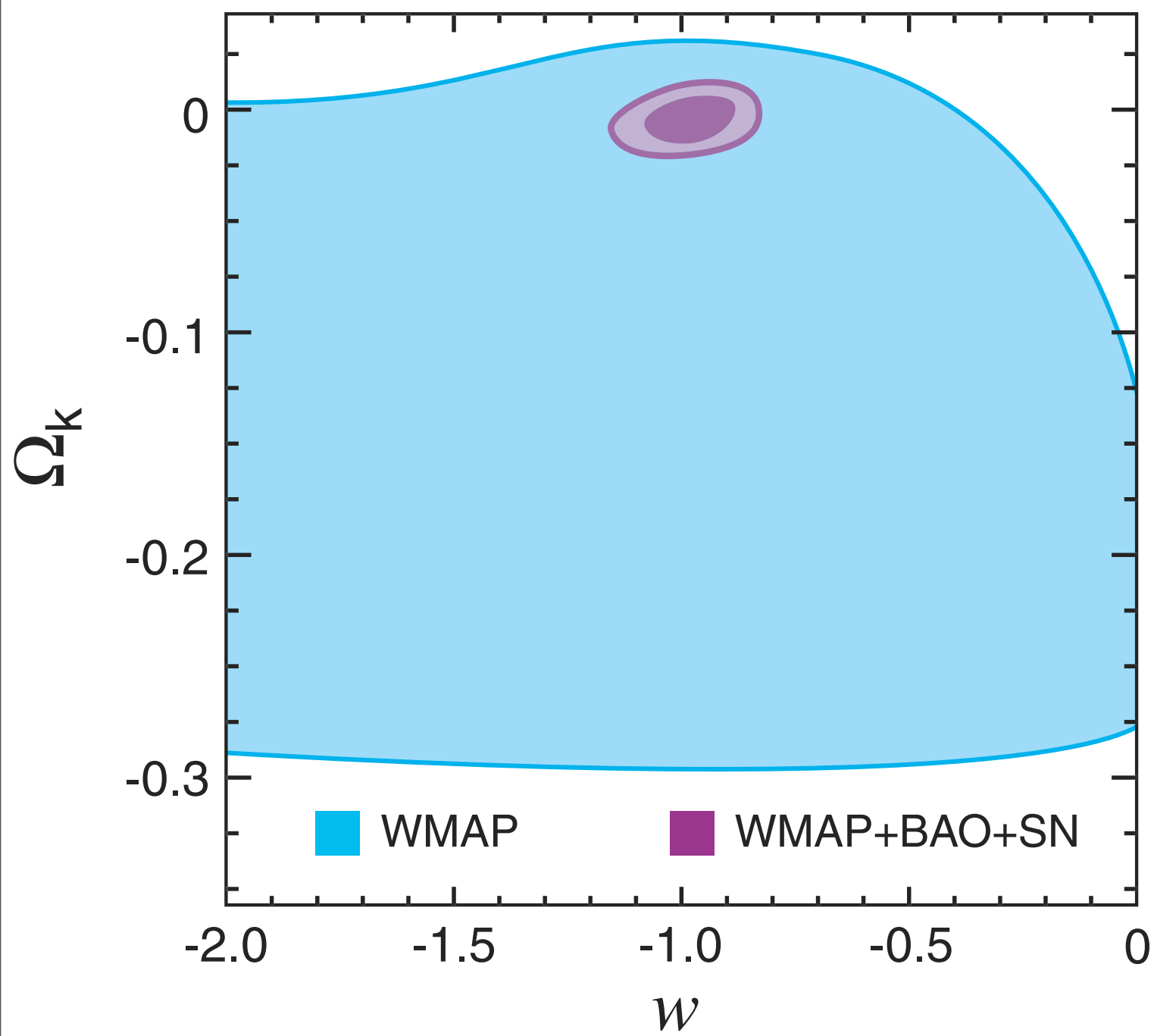
- **Flatness:** $-0.0175 < \Omega_k < 0.0085$ (not assuming $w=-1$!)
- **Non-adiabaticity:** $<8.6\%$ (axion DM); $<2.0\%$ (curvaton DM)
- **Non-Gaussianity:** $-9 < \text{Local} < 111$; $-151 < \text{Equilateral} < 253$
- **Tilt** (for $r=0$): $n_s=0.960 (+0.014) (-0.013)$ [68% CL]
- **Running** (for $r=0$): $-0.0728 < dn_s/d\ln k < 0.0087$
- **Gravitational waves:** **$r < 0.20$**
 - $n_s=0.968 (+/- 0.015)$ [68% CL]
 - **$n_s > 1$ disfavored at 95% CL regardless of r**

What else in the interpretation paper...

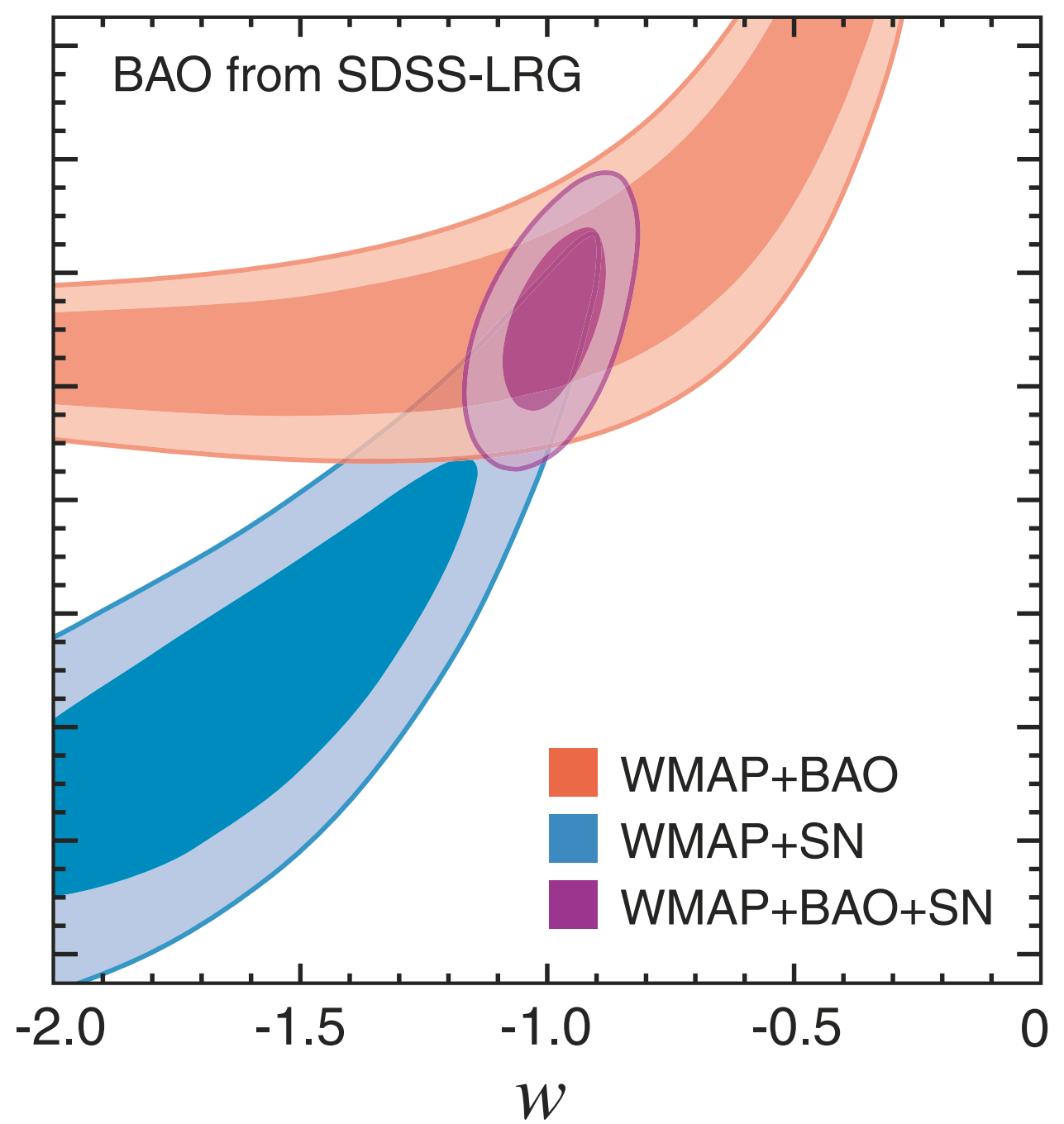
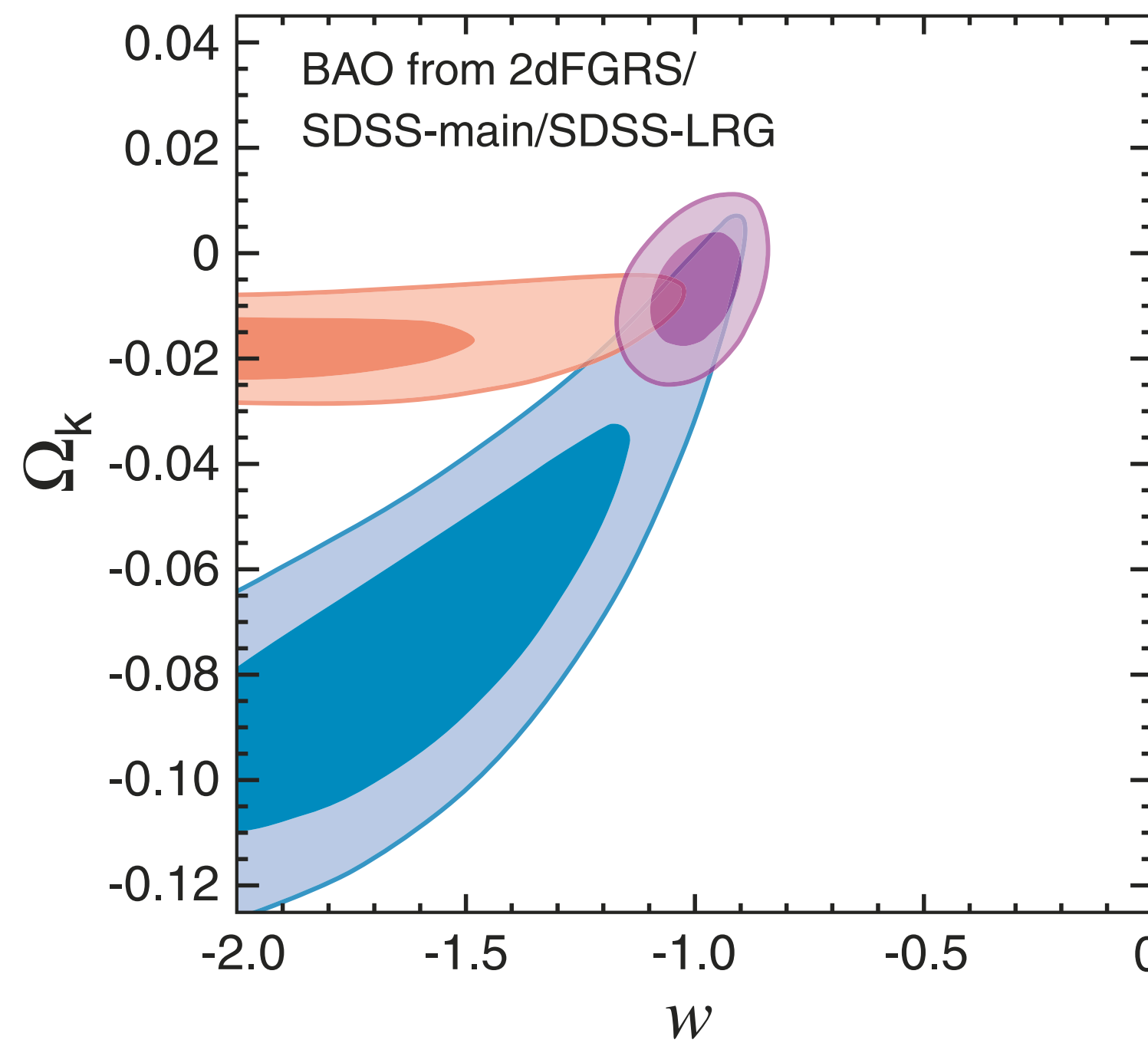
- Basically, we tried everything we could do (*in time before the release*) to find deviations from the simple 6-parameter Λ CDM.
- We failed to find any. A flat Λ CDM is annoying, but it is a good fit to the data!
- The interpretation paper is a journal on the painstaking quest to look for new physics in the WMAP data. While we failed to find any, we report on quantitative, stringent limits on the deviations from the simple Λ CDM.

Dark Energy From Distance Information Alone

- We provide a set of “WMAP distance priors” for testing various dark energy models.
 - Redshift of decoupling, $z^*=1090.04$ (Err=0.93)
 - Acoustic scale, $l_A=\pi d_A(z^*)/r_s(z^*)=302.10$ (Err=0.86)
 - Shift parameter, $R=\text{sqrt}(\Omega_m H_0^2) d_A(z^*)=1.710$ (Err=0.019)
 - Correlations between these three quantities are also provided.

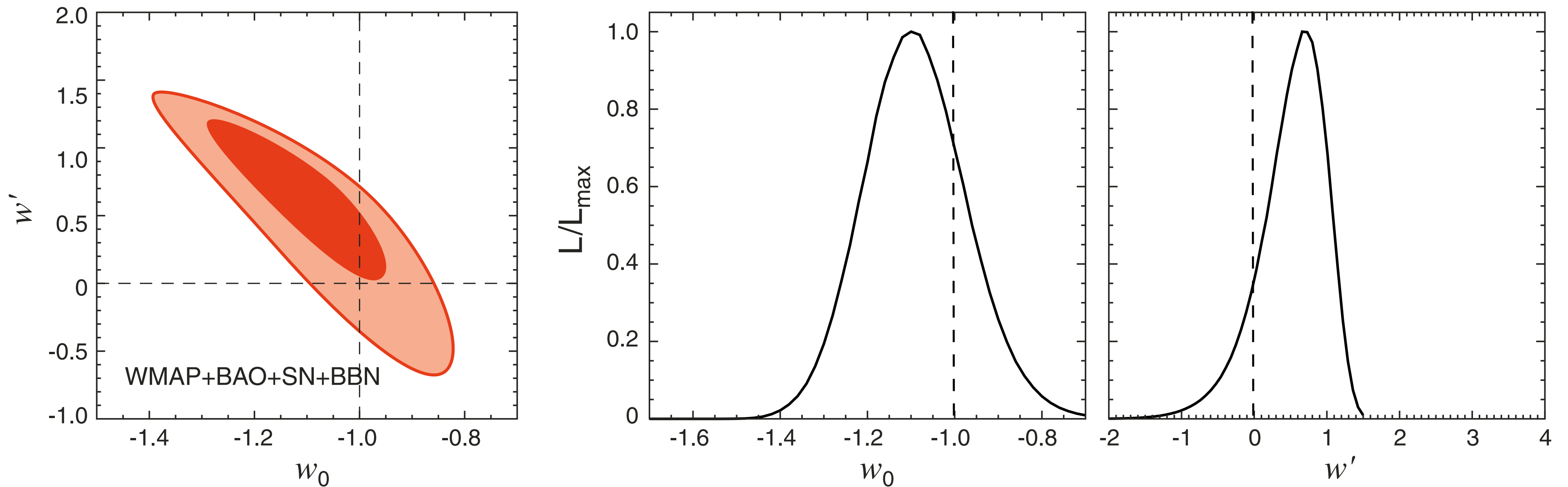


- Top
- Full WMAP Data
- Bottom
- WMAP Distance Priors



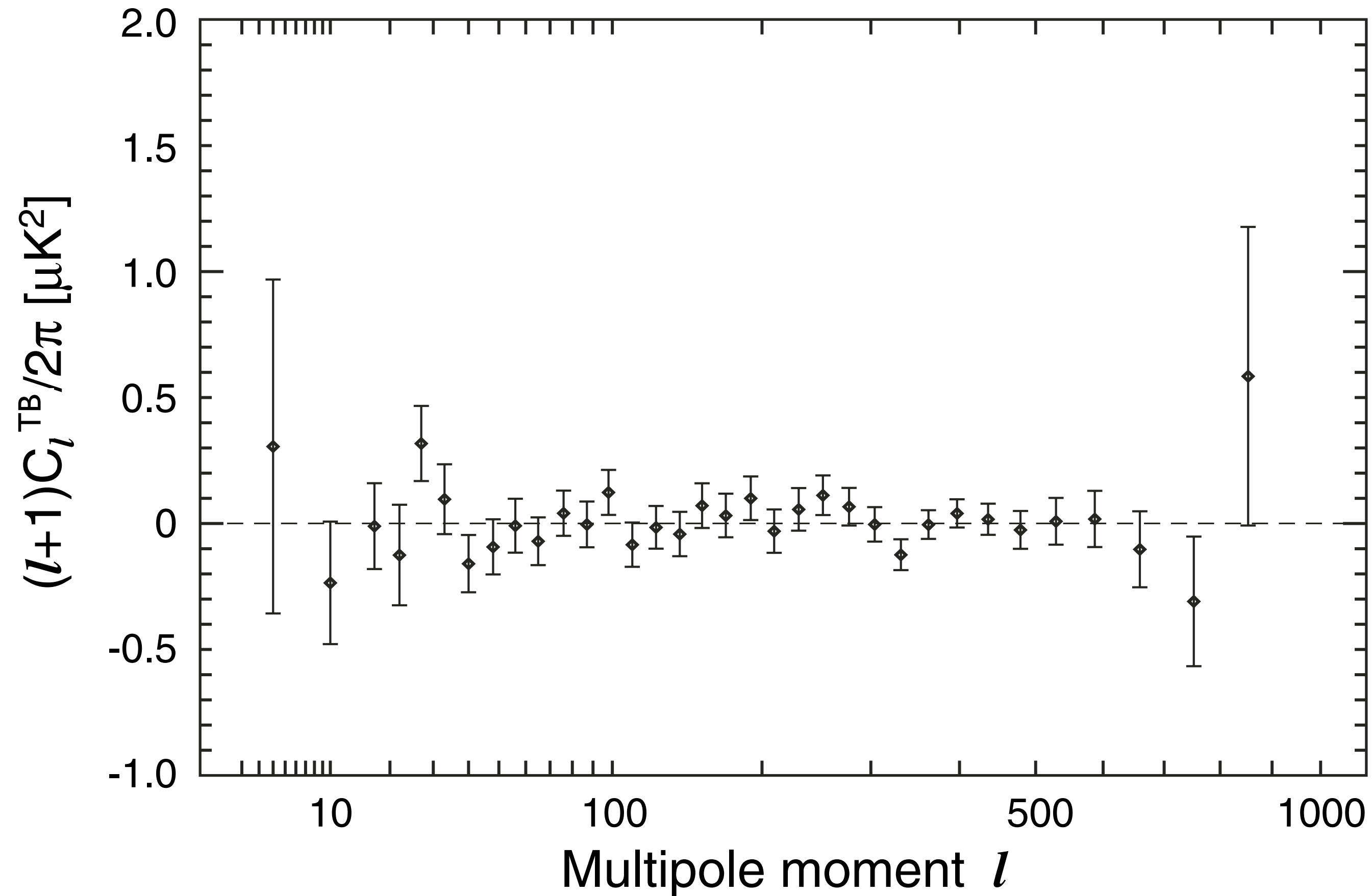
Application:

$$w(z) = w_0 + w'z/(1+z)$$



- Dark energy is pretty consistent with cosmological constant: $w_0 = -1.09 \pm 0.12$ & $w' = 0.52 \pm 0.46$ (68%CL)

Probing Parity Violation



- Parity violating interactions that rotate the polarization angle of CMB can produce TB and EB correlations.

E \rightarrow B

$$C_l^{TE,obs} = C_l^{TE} \cos(2\Delta\alpha),$$

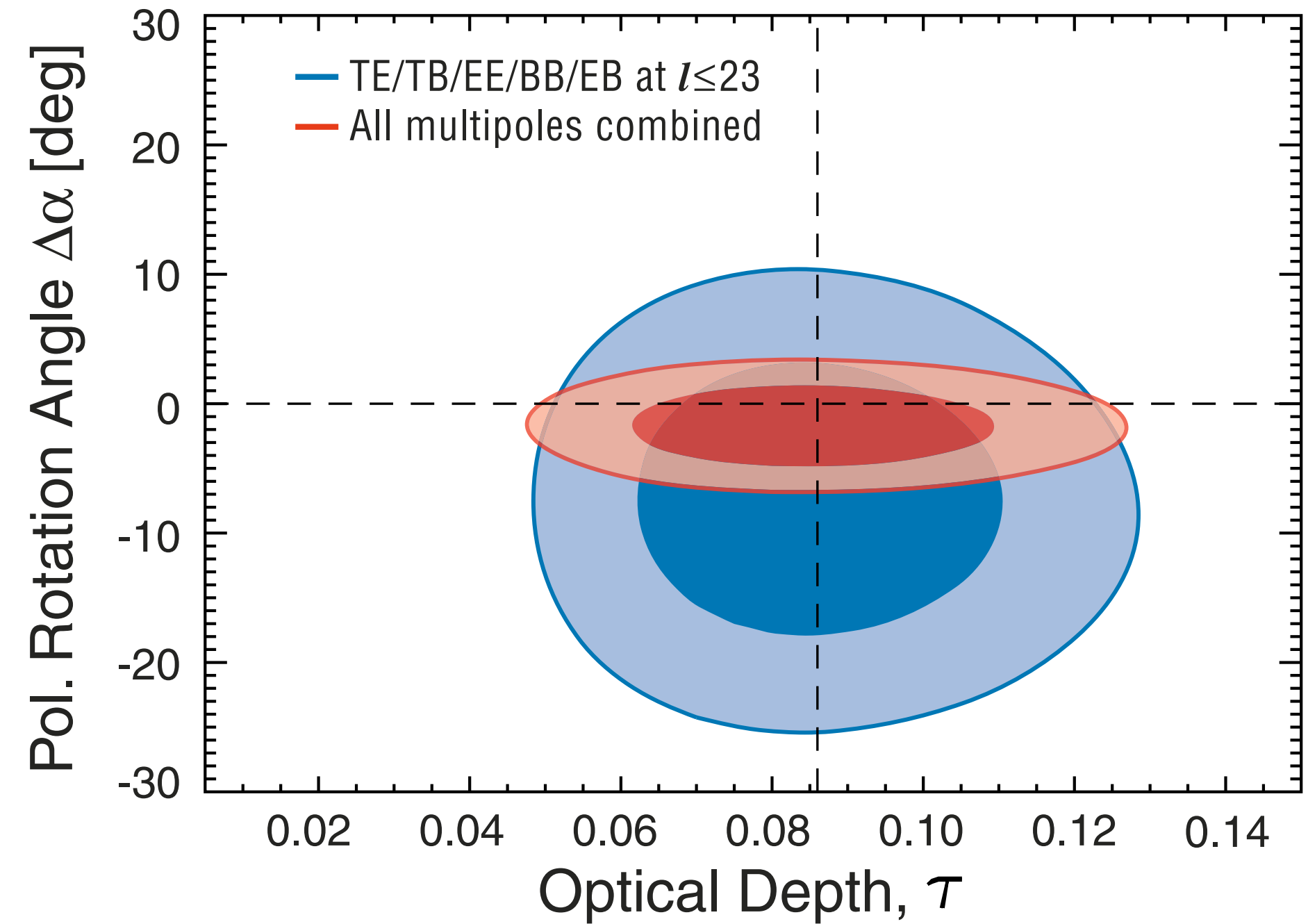
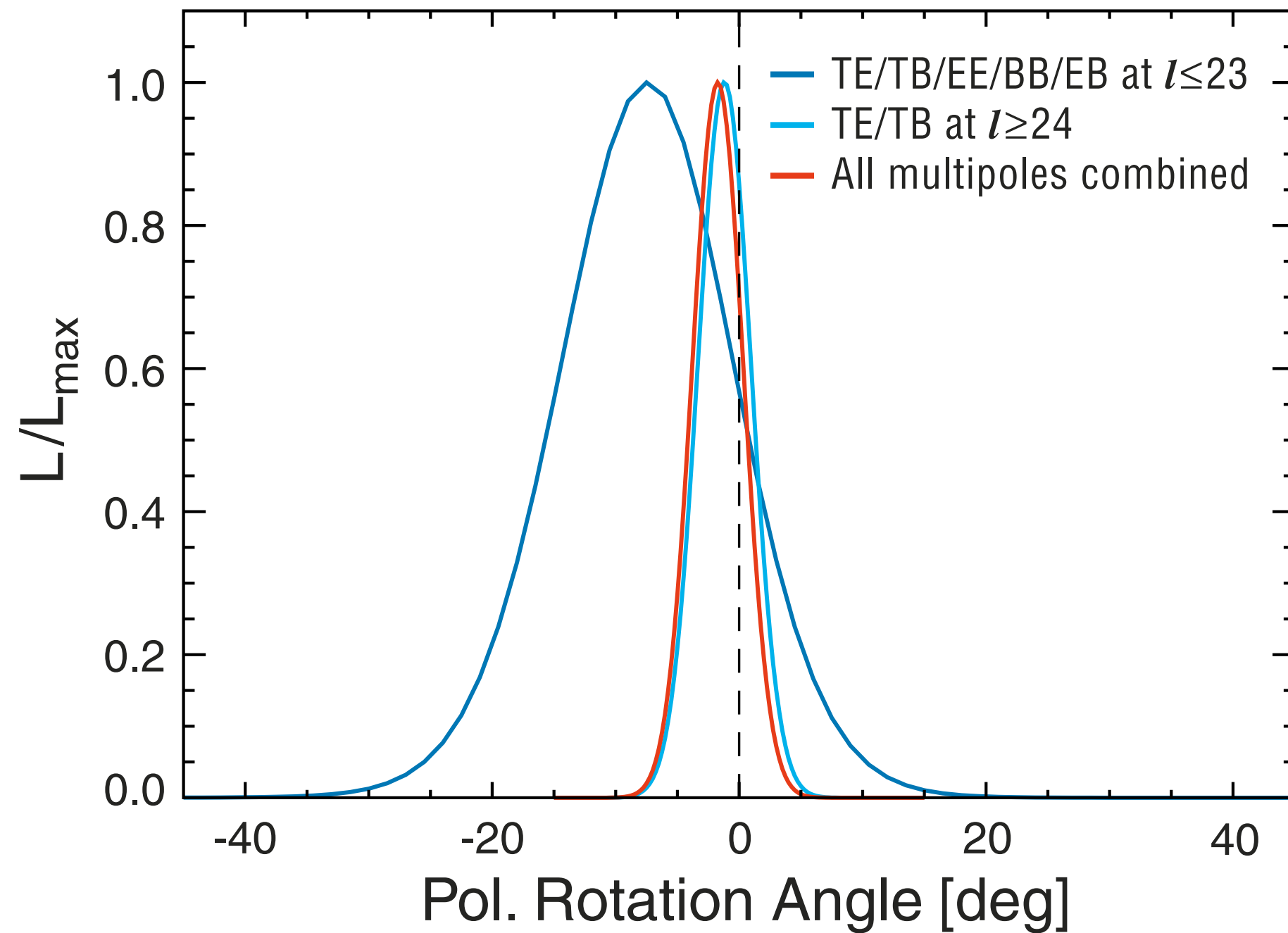
$$C_l^{TB,obs} = C_l^{TE} \sin(2\Delta\alpha),$$

$$C_l^{EE,obs} = C_l^{EE} \cos^2(2\Delta\alpha),$$

$$C_l^{BB,obs} = C_l^{EE} \sin^2(2\Delta\alpha),$$

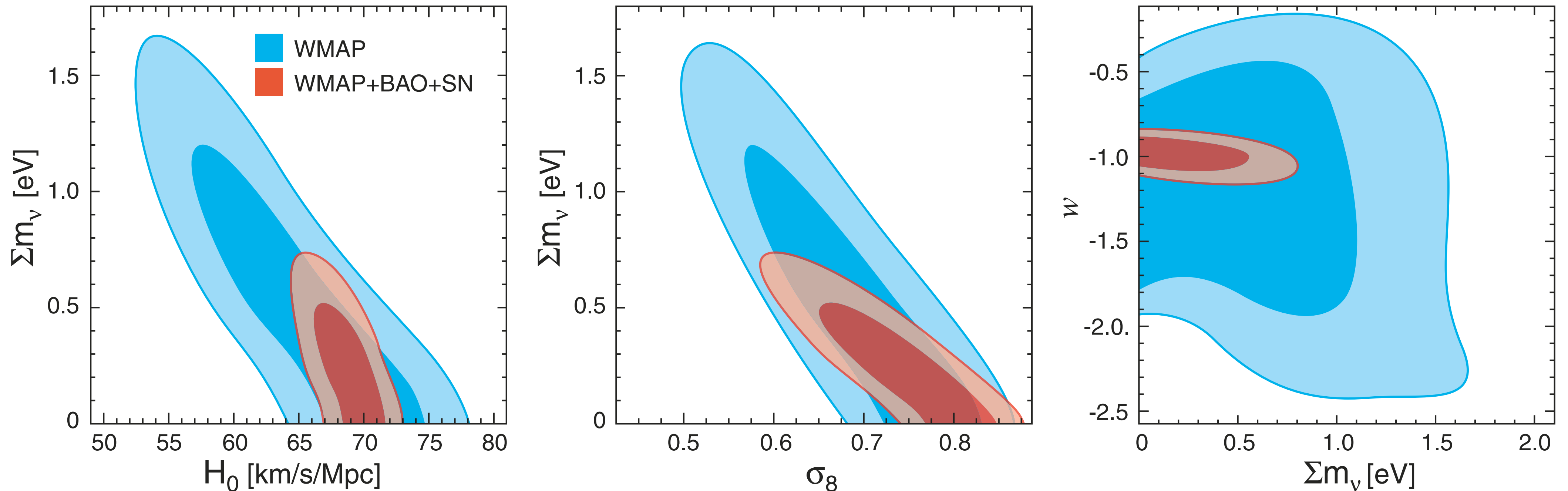
$$C_l^{EB,obs} = \frac{1}{2} C_l^{EE} \sin(4\Delta\alpha).$$

- These are simpler relations when there was no primordial B-mode polarization.
- How much rotation would WMAP allow?



- **$\Delta\alpha = (-1.7 \pm 2.1)$ degrees (68% CL)**
- Comparable to the astrophysical constraint from quasars and radio galaxies
 - $\Delta\alpha = (-0.6 \pm 1.5)$ degrees (68% CL) (Carroll 1998)
- But, note the difference in path length!

Neutrino Mass



- BAO helps determine the neutrino mass by giving H_0 .
- **$\text{Sum}(m_\nu) < 0.61 \text{ eV}$** (95% CL) -- independent of the normalization of the large scale structure.

After the quest in the dark forest...

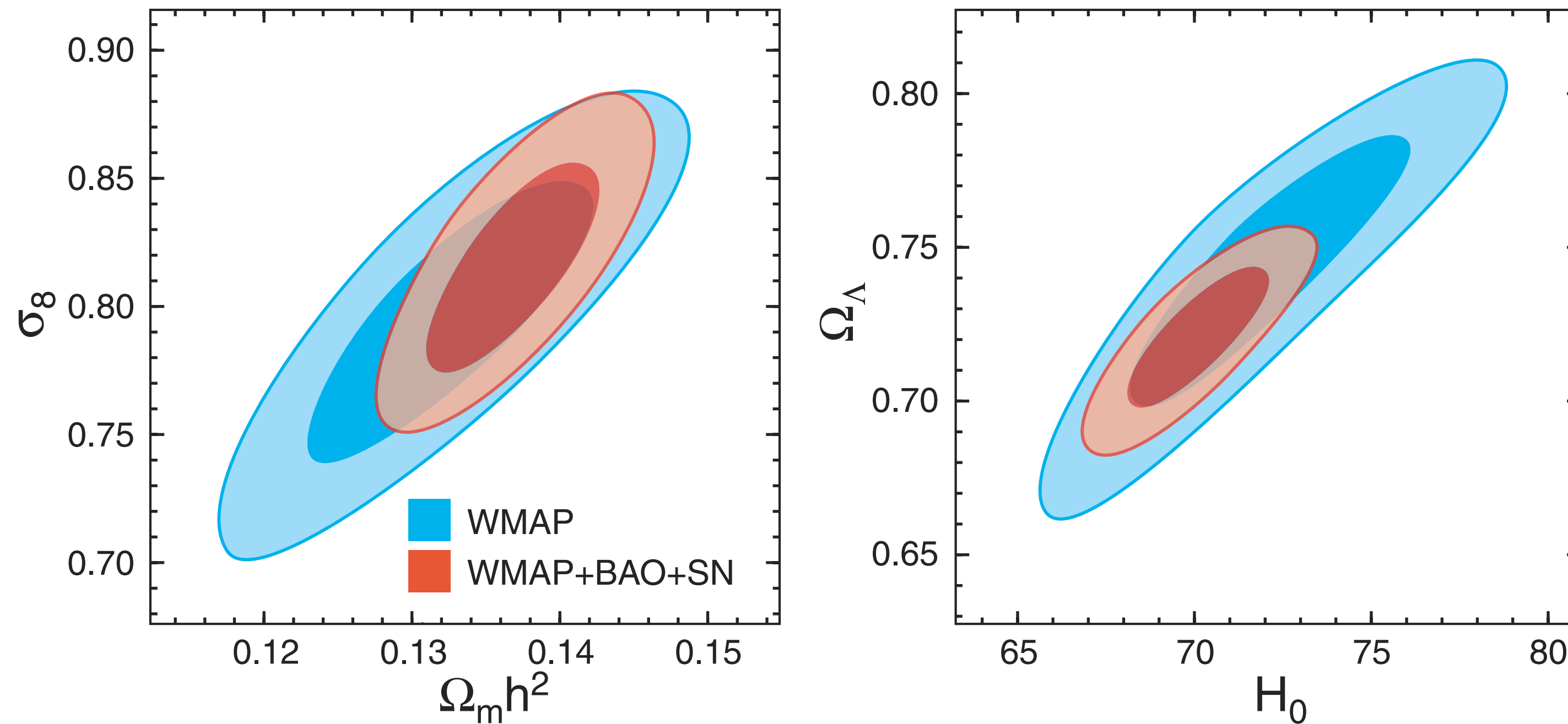
TABLE 2

SUMMARY OF THE 95% CONFIDENCE LIMITS ON DEVIATIONS FROM THE SIMPLE (FLAT, GAUSSIAN, ADIABATIC, POWER-LAW) Λ CDM MODEL

Section	Name	Type	WMAP 5-year	WMAP+BAO+SN
§ 3.2	Gravitational Wave ^a	No Running Ind.	$r < 0.43^b$	$r < 0.20$
§ 3.1.3	Running Index	No Grav. Wave	$-0.090 < dn_s/d \ln k < 0.019^c$	$-0.0728 < dn_s/d \ln k < 0.0087$
§ 3.4	Curvature ^d		$-0.063 < \Omega_k < 0.017^e$	$-0.0175 < \Omega_k < 0.0085^f$
	Curvature Radius ^g	Positive Curv.	$R_{\text{curv}} > 12 h^{-1} \text{Gpc}$	$R_{\text{curv}} > 23 h^{-1} \text{Gpc}$
		Negative Curv.	$R_{\text{curv}} > 23 h^{-1} \text{Gpc}$	$R_{\text{curv}} > 33 h^{-1} \text{Gpc}$
§ 3.5	Gaussianity	Local	$-9 < f_{NL}^{\text{local}} < 111^h$	N/A
		Equilateral	$-151 < f_{NL}^{\text{equil}} < 253^i$	N/A
§ 3.6	Adiabaticity	Axion	$\alpha_0 < 0.16^j$	$\alpha_0 < 0.067^k$
		Curvaton	$\alpha_{-1} < 0.011^l$	$\alpha_{-1} < 0.0037^m$
§ 4	Parity Violation	Chern-Simons ⁿ	$-5.9^\circ < \Delta\alpha < 2.4^\circ$	N/A
§ 5	Dark Energy	Constant w^o	$-1.37 < 1 + w < 0.32^p$	$-0.11 < 1 + w < 0.14$
		Evolving $w(z)^q$	N/A	$-0.38 < 1 + w_0 < 0.14^r$
§ 6.1	Neutrino Mass ^s		$\sum m_\nu < 1.3 \text{ eV}^t$	$\sum m_\nu < 0.61 \text{ eV}^u$
§ 6.2	Neutrino Species		$N_{\text{eff}} > 2.3^v$	$N_{\text{eff}} = 4.4 \pm 1.5^w$ (68%)

- ...here is a report, captain...

What About Λ CDM?



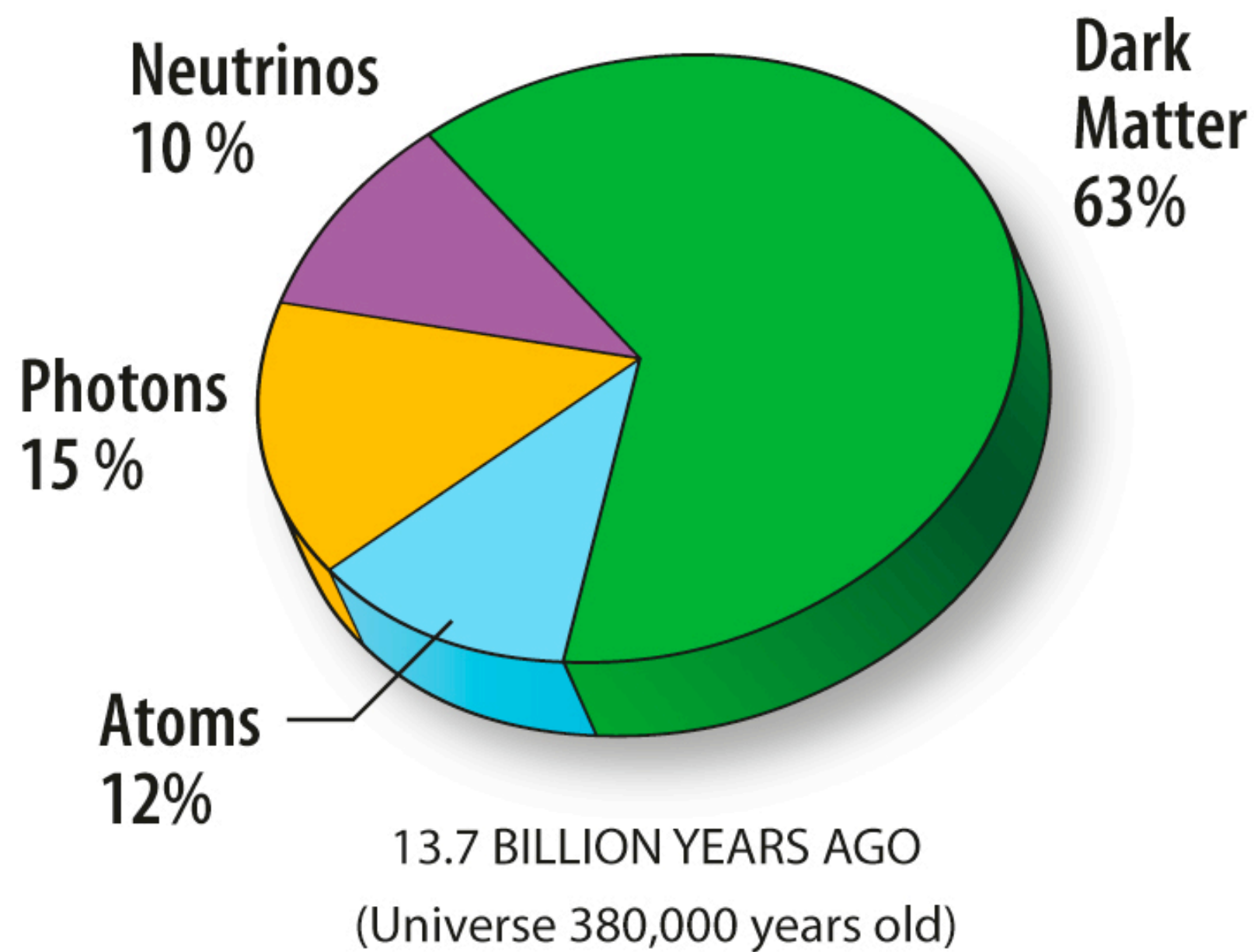
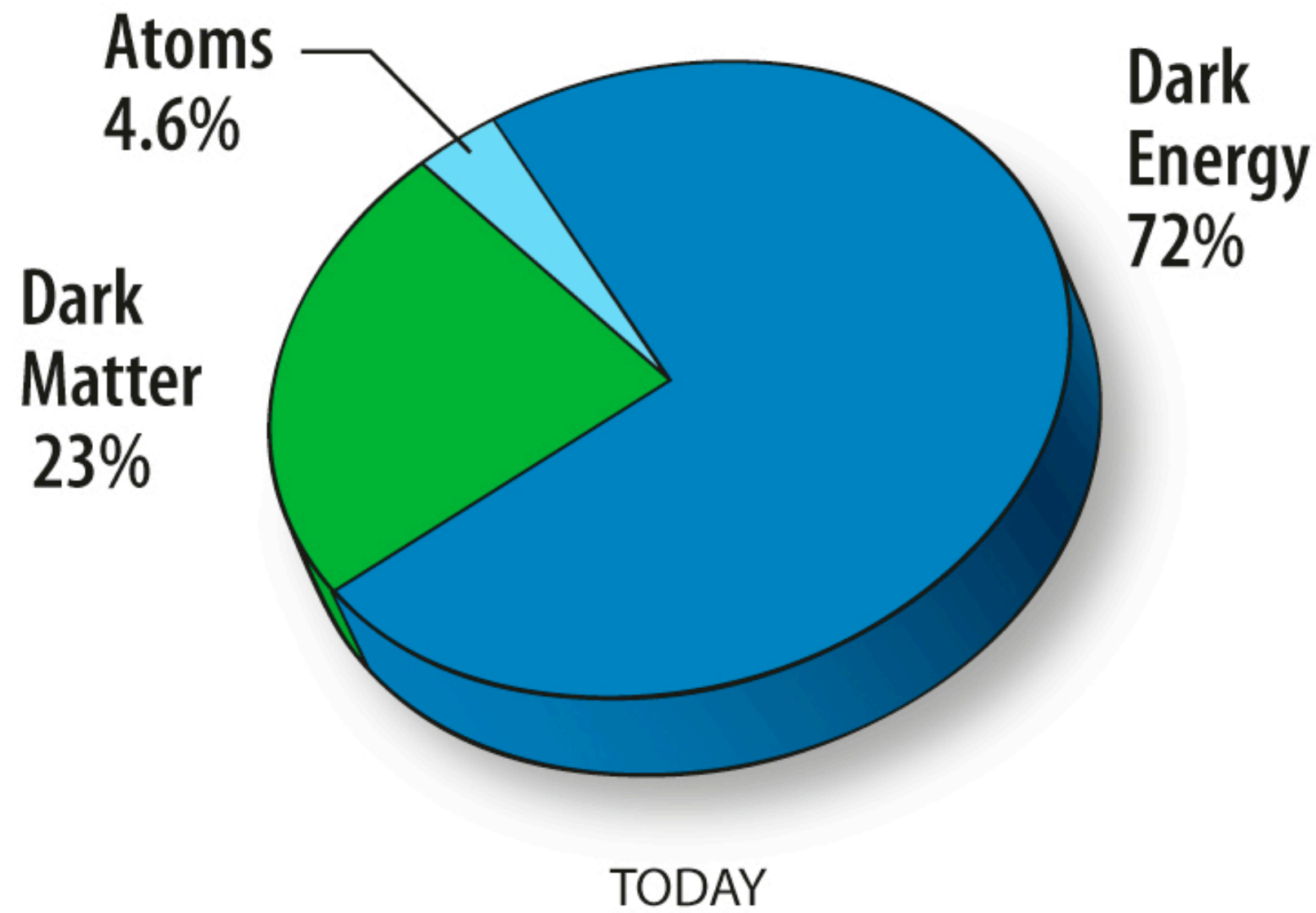
- BAO+SN are very powerful in reducing the uncertainty in several Λ CDM parameters.
- Any parameters related to $\Omega_m h^2$ & H_0 have improved significantly.

And, we ended up here again...

TABLE 1
SUMMARY OF THE COSMOLOGICAL PARAMETERS OF Λ CDM MODEL AND THE CORRESPONDING 68% INTERVALS

Class	Parameter	WMAP 5-year ML ^a	WMAP+BAO+SN ML	WMAP 5-year Mean ^b	WMAP+BAO+SN Mean
Primary	$100\Omega_b h^2$	2.268	2.263	2.273 ± 0.062	2.265 ± 0.059
	$\Omega_c h^2$	0.1081	0.1136	0.1099 ± 0.0062	0.1143 ± 0.0034
	Ω_Λ	0.751	0.724	0.742 ± 0.030	0.721 ± 0.015
	n_s	0.961	0.961	$0.963^{+0.014}_{-0.015}$	$0.960^{+0.014}_{-0.013}$
	τ	0.089	0.080	0.087 ± 0.017	0.084 ± 0.016
	$\Delta_{\mathcal{R}}^2(k_0^e)$	2.41×10^{-9}	2.42×10^{-9}	$(2.41 \pm 0.11) \times 10^{-9}$	$(2.457^{+0.092}_{-0.093}) \times 10^{-9}$
Derived	σ_8	0.787	0.811	0.796 ± 0.036	0.817 ± 0.026
	H_0	72.4 km/s/Mpc	70.3 km/s/Mpc	$71.9^{+2.6}_{-2.7}$ km/s/Mpc	70.1 ± 1.3 km/s/Mpc
	Ω_b	0.0432	0.0458	0.0441 ± 0.0030	0.0462 ± 0.0015
	Ω_c	0.206	0.230	0.214 ± 0.027	0.233 ± 0.013
	$\Omega_m h^2$	0.1308	0.1363	0.1326 ± 0.0063	0.1369 ± 0.0037
	z_{reion}^f	11.2	10.5	11.0 ± 1.4	10.8 ± 1.4
	t_0^g	13.69 Gyr	13.72 Gyr	13.69 ± 0.13 Gyr	13.73 ± 0.12 Gyr

- The latest cosmic pie chart that you should use in your cosmology class is...



- Universe today

- Age: 13.73 +/- 0.12 Gyr

- Atoms: 4.62 +/- 0.15 %

- Dark Matter: 23.3 +/- 1.3%

- Vacuum Energy: 72.1 +/- 1.5%

- Universe at the decoupling epoch

- The density of relativistic neutrinos is given by $3.04(7/8)(4/11)^{4/3} \sim 0.69$ times the photon density.

Summary

- Annoying Λ CDM still fits the WMAP data, as well as the other astrophysical data sets.
- We did everything we could do to find deviations, but failed.
- Significant improvements in limits on the deviations
 - Most notably, $r < 0.2$ (95% CL), and $n_s > 1$ is now disfavored regardless of r . This is new.
- Significant improvements in Λ CDM parameters.

Looking Ahead...

- With more WMAP observations, exciting discoveries may be waiting for us. Two examples for which we might be seeing some hints from the 5-year data:
 - Non-Gaussianity: If $f_{\text{NL}} \sim 50$, we will see it at the 3 sigma level with 9 years of data.
 - Gravitational waves (r) and tilt (n_s) : $m^2\varphi^2$ can be pushed out of the favorable parameter region
 - $n_s > 1$ would be convincingly ruled out regardless of r .